Increased filtration efficiency of attached compared to free-swimming flagellates

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ABSTRACT: Heterotrophic flagellates often attach to surfaces while feeding. A possible fluid dynamic reason is that attachment increases filtration efficiency. This was investigated experimentally and theoretically. The effect of attachment on flow field and clearance was studied by video microscopy in the nanoflagellates *Paraphysomonas vestita* and *Pteridomonas danica*. The flow field around feeding cells was visualised by latex bead suspensions. From a fluid dynamics point of view, it is advantageous to be sessile if the radius of the transectional area of the water flow that is swept for particles is smaller than $1.5 \times$ cell radius. For flagellates with a smooth flagellum, this also requires that the flagellum beats with a large amplitude. For attached *P. vestita*, clearance is ca. 70% higher relative to free-swimming cells and for *P. danica* this value is ca. 34%. The difference between the 2 species accords with the fact that *Pteridomonas* sweeps a wider area of the water flow relative to its cell size than *Paraphysomonas*. Protozoa may attach for other reasons, such as to remain at sites with high food concentrations, but in the case of suspension feeders, it is also advantageous to attach in terms of fluid dynamics. It is likely that a large proportion of the heterotrophic nanoflagellates in plankton are associated with suspended particles that act as drift anchors, thus enhancing clearance.

KEY WORDS: Flagellates · Suspension feeding · Microbial loop · Filtration efficiency · Attachment · Fluid dynamics

INTRODUCTION

Heterotrophic flagellates are important components of the microbial food web. Bacteria are essential for the re-utilisation of decomposed organic matter, including ca. 25% of the planktonic primary production estimated to occur as exudates (e.g. Larsson & Hagström 1979). Heterotrophic flagellates play an important ecological role by forming a link between bacteria and larger suspension feeders; in Limfjorden, Denmark, ca. 20% of the water is cleared for bacteria by flagellates per day (Fenchel 1982c). Although there is a considerable variation in the occurrence of flagellates, the same order of magnitude seems valid for many other aquatic habitats (Fenchel 1986a). Thus, improved knowledge on feeding processes of these organisms could lead to a deeper understanding of the processes involved in the transfer of carbon in marine food webs.

Some flagellate species strain food particles from the water with a filtration apparatus in the form of an array of radial pseudopodia or tentacles. In other species, suspended food particles are intercepted directly by a certain part of the cell surface or by the flagellum. The water flow results from swimming through the water, or—if the cells are attached—by generating feeding currents. In both cases this results from propagation of planar or 3D waves along the flagellum. In smooth flagella this is mediated by a force acting on the fluid, generated by the flagellum itself. If the flagellum is hispid and has rigid projections (mastigonemes) protruding from its side, the force against the fluid is generated by the mastigonemes (Brennen 1976). Most flagellates (and other suspension-feeding protists) tend to attach to particles or surfaces while feeding, and so attachment must be assumed to be important in the feeding process.
An obvious reason for attachment is to remain in areas with a high food concentration. Motile bacteria make up at least 20% of marine planktonic bacterial populations (Fenchel 2001), and it has long been known that motile bacteria exhibit chemotactic responses to chemical gradients (Weibull 1960, Adler 1969). This leads to aggregation of bacteria around sources of dissolved organic carbon (e.g. Bell & Mitchell 1972, Brown et al. 1993), and thus a patchy distribution of bacteria in the water column. Large suspended particles tend to harbour high concentrations of bacteria; the concentration in association with marine snow particles is typically $10^2$ to $10^5$ times higher than that of the surrounding water (Alldredge & Silver 1988). Protozoa are likewise capable of motile responses to chemical stimuli, and aggregate around patches with high food concentration (Fenchel & Blackburn 1999). Further attachment to, e.g., suspended particles ensures that the protozoa remain in such hotspots of food particles.

This could be one reason to attach in the presence of high densities of food bacteria. But the fact that protozoa tend to attach to solid surfaces, irrespective of the presence of chemical cues, implies that other reasons must be important. Starving cells do not attach, but tend to swim continuously (Fenchel 1982a), suggesting that swimming largely serves to find more suitable habitats rather than for feeding.

A possible hydrodynamic reason for attachment is investigated in this paper. When a flagellate is attached to a particle, the drag of the particle is balanced by thrust produced by the flagellum. This generates a water current with direction towards the cell body and opposing the swimming direction. If cells attach to a particle that can be dragged along, this reduces swimming velocity, but the total fluid velocity experienced by the organism may still be higher because of the flow drawn towards the cell. If the particle is so large that the flagellate cannot drag it, there is no forward motion and the entire force produced by the flagellum is used to generate thrust. The flow field experienced by free-swimming flagellates is different from that experienced if it is attached, even when the parameters of flagellar motion remain the same (Fig. 1).

In the present study, general fluid dynamic effects of attachment are discussed theoretically, emphasising flagellates with a single smooth flagellum such as choanoflagellates. This is possible because the theory of smooth flagella has been extensively studied (e.g. Hancock 1953, Gray & Hancock 1955, Lighthill 1975, 1976). The hydrodynamics of hispid flagella have not been adequately studied from a theoretical point of view, so it was not possible to provide a precise analysis of the fluid dynamic effects of attachment specific for these organisms. Instead, experiments were carried out on 2 ecologically important flagellates, Paraphysomonas vestita and Pteridomonas danica, to determine the effect on feeding efficiency of attachment to particles of various sizes, compared to the free-swimming case. Both of these flagellates have hispid flagella, but very different flagellar beat patterns (Christensen-Dalsgaard & Fenchel unpubl.).

In marine systems, flagellates with smooth flagella are primarily represented by choanoflagellates. Most species are permanently attached by a stalk (only propagules swim). The free-swimming, acanthoecid choanoflagellates build a large and complex lorica. This lorica acts as a drift anchor in a manner similar to the situation when other types of flagellates attach to suspended particles. For this reason, we could not compare the effect on clearance between free-swimming and attached cells experimentally for choanoflagellates. Thus the situation for flagellates with smooth flagella was treated only theoretically.
MATERIALS AND METHODS

General information. Batch cultures of *Paraphysomonas vestita* and *Pteridomonas danica* were grown to densities of about $10^4$ cells ml$^{-1}$ in boiled and filtered seawater (salinity 20%), with a suspension of an unidentified bacterium (ca. $10^6$ cells ml$^{-1}$). Schematic drawings of *P. danica* and *P. vestita* are shown in Fig. 1. Both are ubiquitous in seawater, including the water column as well as sediments. The mean size of the latter species is 5.7 µm, and that of the former is 4.9 µm. *P. danica* carries a conical array of tentacles around the flagellum that intercepts suspended bacteria. *P. vestita* has 2 flagella, a short and a long one; the latter is responsible for the generation of water flow. Suspended particles that touch the flagellum (or the mastigonemes) are transported to the mouth, which is situated beneath the base of the small flagellum. Both species are capable of attaching to solid surfaces with a mucous thread secreted from the posterior pole of the cell. All measurements of cell diameters, flagellar lengths, etc., were based on video recordings.

Experiments were conducted at room temperature (20 to 25°C). As this is higher than most ambient seawater temperatures, control experiments were conducted at 6°C. At this temperature (after 48 h incubation), flow velocities were reduced by only 7% for *Paraphysomonas vestita* and 11% for *Pteridomonas danica* compared to room temperature, and so the results of the present study also apply to natural habitats at lower ambient temperatures.

Recordings of water flow, swimming, and attachment were based on cell suspensions in an ‘O-ring chamber’. An O-ring (height: 2 mm, diameter: 15 mm) was attached to a microscope slide with vaseline, and flagellate suspensions were applied inside the ring with a pipette. The O-ring was then covered with a cover slip, avoiding air bubbles, providing an observation chamber with a volume of 0.35 ml. When nothing else is stated, observations and recordings were carried out using dark-field illumination and a 20× objective.

Attachment rates of swimming cells were also studied in an O-ring chamber. After filling the O-ring with a cell suspension, numbers of attached cells within an area (800 x 800 µm) of the cover slips were counted at 2 min intervals. Tests were made with both starved and feeding cells placed either in bacterial suspension or in particle-free water.

Video recordings. Video recordings were made to track flows and estimate flow velocities around feeding cells, both when attached and when swimming. In order to visualise flow fields, suspensions of latex beads were used.Suspensions were prepared by adding 0.2 µm particles to a final concentration of about $10^{10}$ particles ml$^{-1}$. Particles were first suspended in demineralised water and then the flagellate suspension was slowly added. This was done in order to avoid aggregation of the particles. The 0.2 µm particles are not retained by the flagellates, nor do they in any way interfere with their behaviour. They can therefore be considered as neutral indicators of water flow.

Video recordings were made with an EDH© KamPro 02 CCD camera and a Sony digital video recorder at a frequency of 25 Hz, giving a temporal resolution of 0.04 s. Frame-by-frame tracking of the currents was subsequently done, either computationally using the program LabTrack QT (DiMedia), or manually. For manual tracking, the position of cells and particles was plotted directly from the screen to a transparent overlay attached to the screen during frame-by-frame playback of the recordings.

Flow was investigated under the following circumstances: (1) Free-swimming cells and cells dragging particles. Latex spheres (diameter 25 µm) or cornstarch were added to the cultures 24 h prior to recording. Both flagellate species were found to attach to cornstarch particles, which had diameters typically ranging between 5 and 15 µm, but only *Paraphysomonas vestita* attached to latex spheres. During the recordings, cells were swimming freely or attached to and pulling one or more particles. Altogether, 61 recordings were made of *P. vestita*, and 112 recordings of *Pteridomonas danica*. (2) *P. vestita* attached to the surface of the microscope slide and generating a current parallel to the slide (Fenchel 1986b). Altogether, 10 recordings were analysed. (3) Cells attached to large agar spheres. The agar spheres were made by dropping a warm solution of India ink and seawater (salinity 20‰) with 2% agar into paraffin oil overlaying sterile seawater (Fenchel 2001). The India ink was added to make it possible to use the spheres in darkfield illumination without generating too much scattered light. The spheres measured 600 to 1000 µm in diameter. Recordings were made of cells attached halfway up to the surface of the sphere, generating currents perpendicular to the surface. In all, 34 recordings were made of *P. vestita* and 35 of *P. danica*.

The velocity of the water that can be strained for food particles is of particular interest. It was quantified immediately ahead of the cells at the level of the mid-point of the flagellum. For species with a filter, the transectional area of relevance, $A$ (where $R$ is the radius of this area), is that of the aperture of the filter. *Paraphysomonas* does not have a filter, but the area circumscribed by flow lines that just allows particle encounter with the flagellum (the ‘filtration disk’) is approximately equal to the projected area of the cell ($R = a$, where $a$ is the radius of the cell). Measured
quantities and other symbols used in the following text
are summarised in Table 1.

**Force generated by the flagellum.** Video recordings using a 10×
objective were made of *Paraphysomonas vestita* pulling latex spheres with a diameter of 25 µm in
otherwise particle-free water, in order to calculate the
force generated by the flagellum. As *Pteridomonas danica* did not attach to the latex balls, it was only pos-
sible to do these calculations on *P. vestita*. The height of
the sphere above the microscope slide was measured,
and only cells swimming at distances greater than
125 µm from the nearest surface were recorded. This
was done to avoid interference from wall effects; these
should be negligible at distances to the surface greater
than 10 times the radius of the latex sphere (Happel &
Brenner 1973). In total, 15 recordings were made.

**RESULTS**

**Theoretical considerations on the fluid
dynamics of attachment**

Situations that involve generation of thrust as well as
swimming are difficult to analyse. Here we limit our
considerations to the 2 extreme cases: (1) where only
negligible thrust and motion of the water are pro-
duced, so that all force is used for forward motion (zero
thrust swimming); and (2) where there is no forward
motion, and so the entire force is used in generating
thrust and a large-scale flow field.

In Case (1), the flow of the fluid experienced by the
organism is uniform everywhere, and with a velocity of
equal magnitude to, but in opposite direction of, the
swimming velocity (ignoring a slight lateral displace-
ment around the cell as it translates through the
water). The flow $Q \text{L}^3\text{T}^{-1}$ through a filtration disk with
radius $R$ perpendicular to the swimming direction can
be calculated from:

$$Q = \pi R^2 U \quad (1)$$

where $U$ is the swimming velocity. If the organism is
considered to be spherical with radius $a$, the swimming
speed is given by Stokes’ equation as:

$$U = \frac{F}{6\pi \eta a} \quad (2)$$

where $\eta$ is the viscosity of the fluid (10$^{-3}$ Ns m$^{-2}$), and $F$
the force generated by the flagellum. This corresponds
to:

$$Q = \frac{FR^2}{6\eta a} \quad (3)$$

In Case (2), the thrust generates a velocity gradient
and thus a pressure gradient in the fluid. This results in
a more complicated flow pattern around the organism.
If we assume that the force is a point force in an
unbounded fluid, and that the cell body does not inter-
fere significantly with the flow, the velocity field of the
fluid can be modelled by singularity analysis (e.g.
Lighthill 1975):

$$U_r = \frac{F \cos \theta}{4\pi \eta} \quad U_\theta = -\frac{F \sin \theta}{2\pi \eta} \quad (4)$$

where the position in the fluid relative to the force is
given in polar coordinates ($r, \theta$); $U_r$ is the radial com-
ponent of the velocity and $U_\theta$ the transverse velocity com-
ponent. The resultant flow field can be seen in Fig. 2.
The velocity component relevant for the feeding cell is
the one parallel to the cellular axis through the filtra-
tion disk. By integration over the radial velocity gradi-
ent (Fenchel 1986b), the flow through the filtration
area, if positioned at the centre of the flagellum, is
found to be:

$$Q = \frac{FR}{4\eta} \quad (5)$$

It can easily be seen, comparing Eqs. (2) & (4), that
the velocity of the fluid at the centre of the flow field

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Definition</th>
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<tr>
<td>$a$</td>
<td>Cell radius</td>
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<tr>
<td>$l$</td>
<td>Length of undulating flagellum from base to tip (= $N\lambda$ where $N$ is number of waves and $\lambda$ is wave length)</td>
</tr>
<tr>
<td>$L$</td>
<td>Stretched length of flagellum</td>
</tr>
<tr>
<td>$R$</td>
<td>Radius of transectional area $A$ of flow in front of the cell (filtration disk) within which particles are intercepted</td>
</tr>
<tr>
<td>$R^*$</td>
<td>Maximum radius of $R$ allowing for increasing flow when attached</td>
</tr>
<tr>
<td>$Q$</td>
<td>Flow through $A$</td>
</tr>
<tr>
<td>$V_t$</td>
<td>Total velocity through $A$</td>
</tr>
<tr>
<td>$V_s$</td>
<td>Component of $V_t$ caused by swimming</td>
</tr>
<tr>
<td>$V_c$</td>
<td>Component of $V_t$ caused by drag</td>
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<tr>
<td>$U$</td>
<td>Velocity</td>
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<tr>
<td>$F$</td>
<td>Force</td>
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<tr>
<td>$\eta$ ($10^{-3}$ N s m$^{-2}$)</td>
<td>Viscosity</td>
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will be of larger magnitude than the velocity with which the same force can pull a cell of any given size. However, in Case (1), \( Q \) is directly proportional to the filter area, and thus to \( R^2 \). In Case (2), because the magnitude of the velocity of the fluid decreases proportionally to distance from the point force, \( Q \) is only proportional to \( R \). Thus, it is more effective to be sessile than free-swimming only with a filtration area below a certain size. We denote the critical maximum radius of the filter disk, \( R^* \). From Eqs. (3) & (5), this radius can be calculated to be:

\[
R^* = \frac{3a}{2}
\]

As it is of no consequence whether the force is produced by a flagellum or by other means in the above calculations, the results are valid for any organisms for which the Reynolds number, \( \text{Re} \), is \(<1 \). This is the case for most protozoa, and so Eq. (6) could explain, for example, why most suspension-feeding ciliates also attach themselves while feeding. However, care should be taken in applying Eq. (6) too literally, as a number of factors have not been taken into account. The assumption of the organism not having any significant drag, and thus not producing thrust in Case (1), becomes increasingly invalid with increasing cell size. In reality some thrust will always be generated and the total velocity of particles towards the filtration area experienced by the cell will therefore be higher than indicated by Eq. (2), potentially making the value of \( R^* \) slightly smaller. The exact value of \( R^* \) depends on a number of factors related to how the force is produced, many of which could also make \( R^* \) larger under specific circumstances.

In the case of real flagellates, the situation becomes complex since the power needed to propel the spherical cell has been shown theoretically to be only a fraction of the power needed for the flagellum to push itself through the fluid (Brennen 1976, Higdon 1979a,b,c). One could imagine that this would allow for a larger \( R^* \), but as a large part of the power consumption is due to the added drag of the flagellum which produces thrust, the picture is not clear.

The fact that for flagellates only a small fraction of the total power is used to propel the cell body makes it more valid to neglect the cell body than to neglect the flagellum in theoretical considerations. Lighthill (1976) made an analysis of the motion generated by an infinitely long smooth flagellum. He first calculated the zero-thrust swimming speed: the speed with which the flagellate would swim if it had no hydrodynamical drag to overcome. He then calculated the change in swimming speed and fluid motion that was the result of drag, and thus thrust. In the presence of drag the organism is moving slower than the zero-thrust swimming speed, and so can be said to drift backwards with respect to zero-thrust swimming. Thrust can then be seen as the resistance opposing that backwards drift. In the case of sessile cells attached to particles too large for them to pull, there is no forward motion, and thus compared to the zero-thrust swimming speed, the cells drift backwards with the zero-thrust swimming speed itself. From the resulting thrust, Lighthill calculated the flow through a filtration disk with radius \( R \):

\[
Q = \frac{U R^2 K}{4 x} \ln \left( \frac{2l}{R} \right)
\]

Here \( x = \frac{N \lambda}{L} \), where \( N \) is the number of waves, \( \lambda \) the wavelength and \( L \) the total (stretched) length of the flagellum, and \( l = N \lambda \), where \( l \) is the length of the undulating flagellum. \( K \) is a crude estimate of a thrust coefficient based on calculations of the resistance coefficients by Gray & Hancock (1955). It has the form \( K = \frac{2 \pi \eta}{(2q/\lambda)} \), where \( q \) is a somewhat arbitrary coefficient of a magnitude equal to approximately 0.11, and \( b \) is the radius of the flagellum. From Eqs. (1) & (7):

\[
R^* = \frac{2l}{\ln \left( \frac{2l}{b} \right)}
\]

It is seen that \( R^* \) is a function of \( l \), which for a given organism of known flagellar length and diameter is the only variable in the above equation. \( l/L \) is an indication of the length of the flagellum along the axis of the waveform in proportion to its total (stretched) length, and so is inversely related to the amplitude. In Fig. 3, Eq. (8) is plotted for the known parameters of the sessile choanoflagellate *Codonosiga* sp. with a flagellar.

![Stream lines and velocity vectors calculated by singularity analysis for F = 10^{-11} N as function of distance from a point force.](image)
length $L$ of ca. 28 µm (Sleigh 1964). The figure shows that it is more beneficial for organisms to be sessile when the flagellar waves have large amplitudes. This accords with calculations by Lighthill (1976), showing that for sessile flagellates the most effective amplitude of the flagellar motion is much greater than for free-swimming flagellates. With an estimated filter radius of 5 to 6 µm, and $l$ ca. 21 µm (Sleigh 1964), it would not — according to Lighthill — be fluid-dynamically beneficial for Codonosiga to be sessile, and so one would assume this to have other causes.

This should not be given too much emphasis, however, since the calculations of Lighthill (1976) were based on the fairly arbitrary variable $q$, and he stated himself that $K_0$ is a very crude estimate. The more accurate slender-body theory, based on calculations of Stokeslets and dipoles along a body with a radius that is extremely small compared to other relevant lengths, was initiated by Hancock (1953). The intense complexity of models of this type made progress impossible without the aid of computers.

Higdon (1979a,b,c) used the approach to set up systems of singular integral equations to model the swimming motion of whole organisms with smooth flagella moving in a helical (Higdon 1979c) and a planar wave (Higdon 1979a), and the fluid motions generated by planar waves if the organism is sessile (Higdon 1979b). There is no analytical solution to the problems; a complex analytical-numerical approach is required. This makes it impossible to make direct comparisons between the sessile and free-swimming cases without complex computations, although it would be interesting to see the result of such calculations. However, these accurate calculations can be used to test the validity of Lighthill’s (1976) model. The numerical results obtained generally showed that Lighthill underestimated swimming speed by ca. 20 to 25%, potentially making the values of $R^*$ greater than those shown in Eq. (8). The fact that the force is not a point force, but laterally distributed over an area equivalent to the flagellar amplitude, could also increase $R^*$. However, the tendencies of his calculations were correct. It is predicted that the optimal flagellar amplitude for sessile flagellates is about the size of the filtration disk (Higdon 1979b). It is interesting to note that the flagellar amplitudes of sessile choanoflagellates are indeed very large and in accordance with what could be expected from the theoretical models (Higdon 1979b, T. Fenchel pers. obs.).

### Experimental results

#### Attachment to cover slip

Almost all cells taken from growing *Paraphysomonas vestita* cultures attached to surfaces in the O-ring chamber within 15 to 20 min ($T_{1/2} = 3$ to 6 min), as illustrated in Fig. 4. Attachment took place under all tested circumstances. Starved cells in particle-free water attached with lower efficiency, but this was not critically tested. Similar experiments were not performed on *Pteridomonas danica*. (A close relative, *Actinomonas mirabilis*, attaches only in the presence of bacteria in the water or on bacteria-coated slides. Under such circumstances 72 to 92% of cells attach with $T_{1/2} = 2$ to 5 min; T. Fenchel pers. obs.)

![Fig. 4. Attachment of Paraphysomonas vestita to the walls of an O-ring chamber (2 replicate experiments were done as indicated by the 2 different symbols). Data are fitted to $n(t) = 100[1 - \exp(-\alpha t)]$, with $\alpha$ (probability of a flagellate to attach per unit time) = 0.145 min$^{-1}$. See Table 1 for definitions](image-url)
Feeding currents

For swimming cells, trackings were redrawn to show the flow experienced by the cell; examples of these current systems are shown in Fig. 5, with the flagellate

as a reference frame. Free-swimming flagellates experience parallel flow lines with the same speed, but opposite direction of the swimming velocity and only insignificant water currents are generated as compared to the swimming velocity. Cells that attach to particles that they are able to pull forward as they swim simultaneously pull a current towards the cell body, balancing the drag caused by the particle.

The current velocity through the filtration disk caused by swimming is denoted $V_s$. The velocity of the current generated by the thrust of the flagellum was measured within the area perpendicular to the flow within which food particles are intercepted, and at a distance of 1 to 2 cell diameters ahead of the cell. This is denoted $V_c$. The total velocity $V_t$ with which water moves towards the cell is the sum of the velocity at which the cell swims and the velocity with which water is pulled towards the filtration disk, so that $V_t = V_s + V_c$. If the cell is attached to a particle that is too large for it to pull, $V_s = 0$, then $V_t = V_c$. Measurements $V_c$ and $V_s$ (µm s$^{-1}$) were all done on recordings (Fig. 6). When measuring $V_c$, it was often not possible to decide the exact size of the filter of *Pteridomonas danica* cells. In these cases, the radius of the cells was measured and estimates of the radius of the filtration area estimated as $2\pi a^2$. *Paraphysomonas vestita* does not have a filter; food particles must make contact with the flagellum, which fans them to the appropriate area of the cell surface (Christensen-Dalsgaard & Fenchel unpubl.). The effective area of the fluid flow cleared by the flagellum was estimated to be equivalent to the radius of the cell, $a$ (for food particles with a mean radius of 0.75 µm). Clearance $C$ (ml h$^{-1}$), and thus filtration efficiency, is directly proportional to $V_t$:

$$V_t \pi R^2 \times 3.6 \times 10^{-9}$$  \(9\)

Fig. 5. Flow lines (with the flagellates as reference frame) represented by the position of suspended particles at time intervals of 0.04 s. Arrows indicate the main direction of flow; scale bar = 10 µm. (a) *Paraphysomonas vestita* cell attached to an agar sphere. (b) A *P. vestita* cell dragging a 25 µm latex bead. (c) A *P. vestita* cell attached to a microscope slide drawing water parallel to the slide; also included are isolines (lines of constant velocity) for the vertical velocity component, representing 100, 40, and 20 µm s$^{-1}$. (d) A free-swimming *Pteridomonas danica* cell

Fig. 6. *Paraphysomonas vestita* and *Pteridomonas danica*. Velocity of induced flow ($V_c$) as function of swimming velocity ($V_s$). Regression lines for the data are also shown
$V_t$ is plotted as function of swimming speed in Fig. 7. Since both $V_c$ and $V_s$ are directly proportional to force, it can be seen that the proportion of the force $F_{th}$ used to generate thrust is proportional to $V_c/V_t$, and so $V_c/V_t$ was used as a measure of $F_{th}$. To clarify tendencies, the average $V_t$ was taken from measurements at intervals of 0.1 for $V_c/V_t$. The average velocity for *Paraphysomonas vestita* cells generating currents parallel to the surface of the microscope slide was around 125 µm s$^{-1}$, a value well in accordance with the 120 µm s$^{-1}$ measured by Fenchel (1986b). This value is much smaller than the approximate 265 µm s$^{-1}$ observed for *P. vestita* generating currents normal to the surface of agar balls. This difference is due to wall effects, and since the generation of currents parallel to a smooth surface is a situation that would rarely arise in nature, the calculations on sessile cells are based solely on recordings made of cells attached to agar balls. All the average values for $V_t$ were plotted as a function of $V_c/V_t$ from 0 (free-swimming) to 1 (stationary cells). From these values it can be seen that for free-swimming *P. vestita*, $V_t$ is 176 µm s$^{-1}$ and this increases to ca. 300 µm s$^{-1}$ for cells attached to very large particles, or an increase of ca. 70%. For attached *Pteridomonas danica* the increase in clearance is ca. 34% relative to free-swimming cells. The values of $R$ are 5 and 2.5 µm for *P. danica* and *P. vestita*, respectively. The clearance for free-swimming and attached *P. danica* is 6.39 × 10$^{-5}$ and 8.62 × 10$^{-5}$ ml$^{-1}$ h$^{-1}$, respectively and for *P. vestita* the corresponding values are 1.24 × 10$^{-5}$ and 2.12 × 10$^{-5}$ ml$^{-1}$ h$^{-1}$.

**Estimates from force calculations**

The recordings of *Paraphysomonas vestita* pulling 25 µm spheres showed a mean $V_c$ value of 35 ± 6 µm s$^{-1}$. From this, and Eq. (2), assuming the diameter of the cell to be 5 µm, the force generated by the flagellum was calculated to be $F_f = 9.9 ± 1.6 × 10^{-12}$ N, with a minimum of 7.6 × 10$^{-12}$ N, and a maximum of 13.0 × 10$^{-12}$ N. Using Eqs. (4) & (5), and assuming an effective radius of the filtration disk of 2.5 µm, this results in a theoretical average velocity through the filter $V_t$ of 315.0 ± 49.5 µm s$^{-1}$, if the force had been used only in producing thrust. For comparison with the experimental results, this calculated value of $V_t$ is plotted in Fig. 7 (open triangle).

To be able to estimate whether wall effects were of importance to the filtering efficiency of attached cells, the length of the attachment thread of *Paraphysomonas vestita* was measured as distance from cell to sphere on cells pulling the 25 µm spheres horizontally. It was found to be 8.2 ± 2.5 µm, min. 4.4 µm, and max. 13.2 µm. The diameter of the *P. vestita* cells ranged between 3 and 8 µm.

**DISCUSSION**

Earlier estimates of maximal clearance based on direct measurements have given values of $1.7 × 10^{-5}$ ml h$^{-1}$ for *Paraphysomonas vestita* (Fenchel 1982a) and $7.9 × 10^{-5}$ ml h$^{-1}$ for *Pteridomonas danica* (Fenchel 1986a). These values are close to, but slightly lower than, those found for attached cells in the present study.

With the exception of *Paraphysomonas vestita* pulling 25 µm spheres, it was not possible to determine the length of the attachment thread on the recordings. The attachment thread of *Pteridomonas danica* can be very long, and it might make up a significant part of the total drag. Also, it was not possible to determine the dimensions of the particles (starch grains) to which
the flagellates attached due to glare caused by dark-field illumination, and this rendered it impossible to calculate drag. However, since \( V_c \) is directly proportional to thrust, it is seen from the linear relationship between \( V_c \) and \( V_t \) (Fig. 6) that a large part of the reduction in swimming speed observed was indeed a result of increased drag. The observed scatter could not be caused by cell size since increased cell size would also mean an increase of the thrust, and therefore simply displace the organism along the line. We believe the large deviations are caused by intraspecific variation in force generation. This variation was shown for the calculated force that is generated by the flagella of *P. vestita*; these values vary by a factor of 2. Since the radius of the sphere is much larger than that of the cell, even a variation in cell radius from 1.5 to 4 \( \mu \text{m} \) would not explain the observed variation, and so it can be concluded that cells differ with respect to the force generated by the flagellum. The scatter in Fig. 6 is somewhat larger for *P. danica* than for *P. vestita*, indicating a larger variation in force of the flagellum for this species.

*Paraphysomonas vestita* attached under all recorded circumstances, indicating that attachment does not depend on chemotactic responses. This accords with the increase in filtration efficiency experienced by the cell as a function of \( V_c/V_t \) (Fig. 7). The average flow velocity was observed to increase as much as 70% for attached cells so that it is clearly adaptive to attach.

Values of \( V_c/V_t \) from 0.1 to 0.5 are absent for *Paraphysomonas vestita* in Fig. 7. This was because the cells were either entirely free-swimming or attached to particles above some minimum size. Thus it was not possible to investigate cells attached to very small particles. Possibly this is because the cells are only free-swimming when dispersing from one attachment site to another, and only remain attached to particles large enough to produce a significant thrust when feeding.

It is interesting to note that the highest feeding flow is not observed for sessile cells attached to the surface of agar spheres, but for cells attached to the largest particles that are still small enough for the cells to be able to pull them (diameter ca. 25 \( \mu \text{m} \)). This is judged to be a result of wall effects caused by the proximity of the surface of the agar sphere. Calculations can be done on the flow through a circular filter level with the point force of a Stokeslet as a function of the distance \( D \) from the filter to a solid surface (Fenchel 1986b). Using the measured length of the attachment thread of 8.2 \( \mu \text{m} \), assuming a cell diameter of 5 \( \mu \text{m} \), and the centre of force of the flagellum to be placed ca. 4 \( \mu \text{m} \) above the cell surface, the distance between the point force and the attachment surface can be estimated as \( D = 17 \mu \text{m} \). With radius of the filtration disk \( R = 2.5 \mu \text{m} \), \( D/R = 6.8 \). From the model by Fenchel (1986b), the reduction of flow as a result of a presence of a surface at this relative distance should be ca. 10%, which, within the standard errors, explains the observed decrease. The wall effects being a reason for the decrease is further supported by the fact that the calculated value of \( V_t \) for an attached cell is somewhat higher than the observed value and in accordance with the general trend observed for *Paraphysomonas vestita*.

*Pteridomonas danica* did not show as high an increase in \( V_t \) as *Paraphysomonas vestita* when being attached; the maximal average increase in velocity was ca. 34%. It is consistent with the theoretical considerations that the relative gain in clearance by attachment is higher for *P. vestita* than for *P. danica* because the latter has a much larger filtration area relative to cell radius. The estimate of the effect of attachment in *P. danica* is less certain due to the great variations seen for this organism in \( V_t \) for any given value of \( V_c/V_t \). As \( R > 3a/2 \) for *P. danica*, it is interesting to see that there still seems to be an increase in filtration efficiency, though relatively small. This shows the uncertainty in the theoretical determination of \( R^* \) by simplified assumptions, as calculated in Eq. (6).

It is likely that the theoretical results for smooth flagella, that is, that the flagellar parameters are important in terms of relative advantage of attachment, also hold for hispid flagella, although the calculations and thus probably the exact tendencies would be different. The differences seen with respect to the fluid-dynamic response of *Paraphysomonas vestita* and *Pteridomonas danica* to attachment (Fig. 7) may also be related to the fact that the motility patterns of the flagellum are different in the 2 species (Christensen-Dalsgaard & Fenchel unpubl.).

Fig. 5 shows that in the presence of the nearby surface, perpendicular to the flow, the flow becomes deformed by the formation of viscous eddies, an effect that is often observed for flows in close proximity to boundaries (e.g. Liron & Blake 1981). Wall effects also reduce the velocities along the axis of the cell. The velocities are not reduced as much laterally, probably because the flagellum is not a point force; rather, forces act over a larger area proportional to flagellar amplitude and curvature. This could result in higher velocities further from the centre of the force than those predicted theoretically, which could oppose the reduction in velocity from wall effects. In other cases, good agreement between the theoretical (Fig. 2) and observed flow patterns (Fig. 5) can be seen. The observed flow almost has a fore-aft symmetry, indicating that the cell body does not interfere significantly with the flow. This again indicates that theoretical considerations based on the Stokeslet analysis are indeed valid to some approximation, in spite of the fact that the flagellum is not a point force. In general,
it is therefore likely that attachment is advantageous for suspension-feeding organisms with relatively small filters, because this generates a higher velocity of the fluid through the filter, while using the same force.

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