Individual growth model for the appendicularian *Oikopleura dioica*

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ABSTRACT: A model of individual growth simulating the development of the main compartments and processes involved in the ecophysiology of the appendicularian *Oikopleura dioica* is presented. *O. dioica* is one of the 5 most frequent larvacean species inhabiting European seas, and laboratory studies are available for comparison with model outputs. Individual growth and interactions with the external medium are described by state variables and fluxes of C and N, using the stoichiometric approach. Three forcing variables control the animal's growth: temperature, food quantity, and food quality (i.e. C:N ratio and size of particles). Model outputs are compared to experimental data to analyse (1) the effect of food quantity and quality on trunk length; (2) the influence of temperature on trunk length, generation time, respiration, excretion and house production rate; (3) the variability of the filtration rate under different conditions of temperature, food quantity and food quality. Results of the model are coherent with most observations, and validation of the model was successful.

KEY WORDS: Appendicularia · Ecophysiology · Modelling · Carbon · Nitrogen

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INTRODUCTION

Appendicularians are thought to play an important role in the flux of material throughout the water column. This recent view emerges from the following characteristics: (1) most appendicularian species are capable of high grazing rates on a wide spectrum of particles, including microbial phytoplankton, bacteria and small detritus, and they are also able to utilise dissolved organic matter (DOM) (Nakamura et al. 1997, Gorsky & Fenaux 1998, Gorsky et al. 1999); (2) their growth rates may be very high *in situ* (>10 up to 23 d⁻¹; Hopcroft & Roff 1995), i.e. 1 order of magnitude greater than those of copepods of equivalent body size; (3) appendicularians may outcompete copepods in regenerative and microbial food web-based systems (Deibel 1998, Gorsky et al. 1999); (4) they could significantly increase and accelerate the export of carbon and associated elements (abandoned houses, fecal pellets, cadavers, and detritus (e.g. Alldredge 1976, Gorsky et

al. 1984, López-Urrutia & Acuña 1999); (5) dense populations of pelagic tunicates may deplete available food in a few days (Alldredge 1981, Deibel 1985); and (6) pelagic tunicates represent a single-step shunt between their small prey and their potential predators (chaetognaths, medusae, ctenophores, and fishes; e.g. Azam et al. 1983, Fortier et al. 1994, Gorsky & Fenaux 1998).

The overall objective of the EURAPP program (EUROPEAN APPendicularians: www.obs-vlfr.fr/~eurapp/) was to improve our knowledge about the ecological role of distinct appendicularian species in representative marginal seas of Europe, in relation to the flux of colloidal and particulate organic matter, and in relation to the structure, dynamics and resilience of important components in the marine plankton community as a whole.

The specific objectives of the present paper are to (1) describe the functioning of 1 appendicularian species at the organism level in controlled conditions; (2) build an individual growth model to simulate the

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Fig. 1. (a) *Oikopleura dioica* (Fol 1872) inside its house (photograph by R. Fenaux; www.obs-vlfr.fr/~eurapp/). (b) *Oikopleura labradoriensis*. Diagram showing the internal structure and seawater circulation in the house; black arrows indicate water flow through the house before, and white arrows after its passage through the food concentrating filter. The flow of trapped particles towards the mouth of the animal is indicated by the dotted arrows (after Flood & Deibel 1998)

evolution of compartments and processes involved in the ecophysiology of the individual; and (3) study the role of the individual in the transformation of elements and organic matter.

The species *Oikopleura dioica* (Fol, 1872; Fig. 1a) was selected for 2 reasons; (1) it is one of the 5 most representative species found in the European seas (Fenaux 1961, Acuña & Anadón 1992, Acuña et al. 1995), (2) it is one of the best known appendicularian species from

both *in situ* and laboratory studies. Given the possibility to maintain successive generations of this species in the laboratory (Fenaux & Gorsky 1985, Gorsky et al. 1987), experimental results are now available to build, calibrate and validate an individual growth model for this species.

Details concerning the internal structure of the oikopleurid house (Fig. 1b) and its functioning can be found in Flood & Deibel (1998) and references therein.

Oikopleura dioica uses its house to filter and concentrate food particles from the surrounding water. Undulating tail movements cause seawater to circulate through the house. During the feeding process ciliated spiracles on the floor of the pharyngeal cavity create the inflowing current that facilitates the introduction of food items into the pharynx (Gorsky 1980, Deibel & Powell 1987, Acuña et al. 1996). Before reaching the stomach, food particles undergo 3 different filtering processes. Large particles are excluded by the inlet filters, the digestible size particles are concentrated by the food-concentrating filter and are transported to the stomach by the pharyngeal filter. The inlet filter pore size of *O. dioica* is ca. 18 μm with a maximum observed between 20 and 25 μm (Galt 1972, Deibel & Turner 1985, Flood & Deibel 1998). These filters, which are subject to clogging (the house must be abandoned in this case; Deibel & Lee 1992, Acuña et al. 1999), prevent large and potentially harmful particles from entering the house. The pore size of the food-concentrating filter is much smaller (0.15–0.98 μm ; Flood 1981), and this system is designed to concentrate the particles several hundredfold (Morris & Deibel 1993). Collected particles are then drained into the pharynx via the food collecting tube (Fig. 1b). Before being ingested, particles must be captured by the pharyngeal filter which is continuously secreted by the endostyle. Surprisingly, the pore size of this filter was observed to be larger than that of the food-concentrating filter in *O. vanhoeffeni* (Acuña et al. 1996). However, according to the latter authors, particles smaller than the pharyngeal filter pore size could be retained not only by direct interception, but also by diffusional deposition.

Fig. 2. *Oikopleura dioica*. Overview of growth and of the development periods (P1 to P3) modelled, which are delimited by 4 events: hatching, shift of the tail, maturation of gonads, and release of gametes

The size of particles that are potentially ingested by *Oikopleura dioica* ranges from 0.1 to approximately 25 μm (e.g. Flood 1978, Fenaux 1986), and the retention efficiency generally exceeds 90% for particles $>3 \mu\text{m}$ (Deibel & Lee 1992, Gorsky et al. 1999). Dissolved organic matter (DOM), bacteria, flagellates, pico- and nano-phytoplankton, amorphous particles (Alldredge 1981, Flood et al. 1992) are all potential food items for these animals which filter non-selectively (e.g. Gorsky 1980, Deibel & Turner 1985, Bedo et al. 1993). *O. dioica* individuals pump seawater continuously, except when a new house is deployed (Deibel 1988, Gorsky & Palazzoli 1989), and they do not show any evidence of a diel feeding rhythm (Alldredge 1981).

METHODS

Overview of the *Oikopleura dioica* life cycle

The life cycle of appendicularians is simple compared to other zooplankton organisms such as copepods or other gelatinous organisms. Small differences among species exist, but the overall sequence of the life cycle remains the same. The simplicity and similarity of appendicularian life histories are advantageous when modelling their individual growth, population dynamics, and competition for resources.

Details concerning the life cycle of the genus *Oikopleura* can be found in Galt (1972), Fenaux (1976, 1998b), Paffenhöfer (1976), and Fenaux & Gorsky (1983). *O. dioica* is dioecious, in contrast to all other appendicularians, which are hermaphrodite. According to Fenaux (1976), its life cycle is marked by 3 periods separated by 4 significant events: fertilization, hatching, shift of the tail, and release of gametes. For this modelling study we consider, however, that the life of an individual is marked by hatching, shift of the tail, maturation of gonads and release of gametes (Fig. 2). Fertilization is not considered since we do not intend to model the population dynamics. The event termed 'maturation of gonads' corresponds to the period in the life cycle after which most of the available resources will be allocated to gametogenesis.

During Period P1, the trunk and the tail of the individual develop progressively; the individual is not able to filter seawater and consequently cannot ingest food particles. Its growth is negative, but the loss in weight is very small (Fenaux & Gorsky 1983). This period is also characterized by construction of the first house rudiment around the trunk. The mucus of this rudiment is secreted by the oikoplastic epithelium that occupies a large area (the oikoplastic region) above the mouth of the animal.

The shift of the tail is an important event in the life cycle, after which the pre-built house rudiment is deployed around the animal. The house is then used to filter seawater and concentrate particles prior to their ingestion. In the model, the duration of house deployment is considered to be insignificant, which is a reasonable approximation given the fact that it takes only a few dozen seconds (Fenaux 1985, Gorsky & Palazzoli 1989). At the beginning of Period P2, the somatic cells reach their definitive number. The animal will thereafter gain additional weight by increasing the volume of these polyploid cells, and by investing new materials into the construction of gonads and production of gametes.

Development of the gonads accelerates during Period P3. Maturation of the reproductive cells is a priority, since autolysis phenomena of oikoplastic and digestive cells have been observed at this stage. Autolysed material is apparently re-invested into the gonads (Gorsky 1980, Fenaux & Gorsky 1983). When gonads are mature, house rudiment secretion ceases since most oikoplastic cells are autolysed. The last house is abandoned just before the release of reproductive cells, a strategy that favours the dispersion of gametes. The sperm of male individuals is released through a spermiduct, whereas the oocytes of females are released by rupture of the ovary and genital cavity walls (Fenaux 1998a). In all cases, the death of animals occurs shortly after this event.

To survive during P1 and maximize reproductive potential at the end of P3, Periods P1 and P3 should be very short. In cultures of *Oikopleura longicauda* at 20°C, Fenaux & Gorsky (1983) showed that Periods P1, P2, and P3 last approximately 0.5, 6.16, and 1 d, respectively.

The symbols, descriptions and units of the 18 state variables of the present model are shown in Table 1, and information relative to the model parameters is given in Table 2. The model is built using several principles of the stoichiometric approach (see e.g. Sterner 1990, Touratier et al. 1999, 2001), which combines at least 2 elemental units (carbon and nitrogen in the present study) to compute variables and flows. The main advantage of this multi-currency approach is that both food quantity and food quality (C:N ratio) influence the computation of the most important processes in the model.

Whatever the period considered thereafter, all C and N, continuous or discrete flows linking the state variables of the model are represented in the connectivity matrix (Table 3).

Modelling Period P1

During Period P1, the animal must survive without feeding and build the first house rudiment from its own reserves. The state variables and processes used to

Table 1. Variables of the growth model of *Oikopleura dioica*. Units are in $\mu\text{g} \times \text{ind.}^{-1} \text{ bottle}^{-1}$ (x stands for C or N)

Symbols	Descriptions	Elemental unit x
D_C	Carbon weight of detritus accumulated on the inner wall of the working house	C
D_N	Nitrogen weight of detritus accumulated on the inner wall of the working house	N
E_C	Carbon weight of the gametes	C
E_N^a	Nitrogen weight of the gametes	N
F_C	Carbon weight of the food outside the house	C
F_N	Nitrogen weight of the food outside the house	N
FP_C	Carbon weight of fecal pellets accumulated in the medium	C
FP_N	Nitrogen weight of fecal pellets accumulated in the medium	N
G_C	Carbon weight of the gonads	C
G_N^a	Nitrogen weight of the gonads	N
H_C	Carbon weight of the working house	C
H_N^a	Nitrogen weight of the working house	N
HF_C	Carbon weight of the food inside the house	C
HF_N	Nitrogen weight of the food inside the house	N
HR_C	Carbon weight of house rudiment	C
HR_N^a	Nitrogen weight of house rudiment	N
OD_C	Carbon weight of detritus accumulated on the inner wall of old houses	C
OD_N	Nitrogen weight of detritus accumulated on the inner wall of old houses	N
OH_C	Carbon weight of old houses	C
OH_N^a	Nitrogen weight of old houses	N
R_C	Carbon weight of respired products	C
R_N	Nitrogen weight of excreted products	N
SB_C	Carbon weight of structural biomass without the gonads	C
SB_N^a	Nitrogen weight of structural biomass without the gonads	N

^aNot a state variable

Table 2. *Oikopleura dioica*. Growth model parameters. Wd: without dimension

Description	Symbols	Values	Units
Coefficient of the allometric equation for food intake at 0°C	a	52.54 ^a	pgC ^{0.25} d ⁻¹
Carbon assimilation coefficient	ac	0.67 ^b	Wd
Nitrogen assimilation coefficient	an	0.72 ^b	Wd
Slope of the regression line between trunk length and temperature	atl	-50 ^c	µm (°C) ⁻¹
Exponent of the allometric equation for food intake	b	-0.25 ^d	Wd
Gonad construction rate from structural biomass at 0°C during P3	cg3	0.02	d ⁻¹
House rudiment construction rate at 0°C during P1	chr1	0.15	d ⁻¹
C:N ratio for the structural biomass, the gonads, and the gametes	cnb	5.3 ^e	µgC (µgN) ⁻¹
C:N ratio for the house rudiment, the working and the old houses	cnh	250 ^f	µgC (µgN) ⁻¹
Fraction of food intake available for ingestion	ffi	0.95	Wd
Fraction of fecal pellet production released in the medium	ffp	0.95	Wd
Fraction of biomass production available for construction of the gonads during P2	fg2	0.1	Wd
Fraction of biomass production available for construction of the house rudiment	fhr	0.65	Wd
Fraction of biomass production available for construction of the structural biomass during P2	fsb2	0.25	Wd
Fraction of the house volume unoccupied by the organism	fv	0.66 ^g	Wd
Maximum net growth efficiency when assimilated food C:N ratio is equal to cnb	k2m	0.44 ^h	Wd
Half-saturation constant for the relationship representing the effect of forcing E on ingestion	ke	10000	µgC l ⁻¹
Half-saturation constant for food intake	ki	240 ⁱ	µgC l ⁻¹
Half-saturation constant for curve K2	kk2	1	µgC ind. ⁻¹ bottle ⁻¹ d ⁻¹
Respiration rate at 0°C during P1	res1	0.005	d ⁻¹
Size ratio between house diameter and trunk length	rl	3.846 ^j	Wd
10th root of Q ₁₀ coefficient	t10	1.1084 ^c	Wd
Food concentration threshold for maintenance	tf	1	µgC l ⁻¹
Threshold for deployment of a new house (fraction of the sum SB _C + G _C)	th	0.2376 ^c	Wd
Maximum trunk length at 23°C	t1m	740 ^c	µm
Threshold to enter period P3 (fraction of the maximum trunk length)	t1l	0.8	Wd

Sources: ^aAcuña & Kiefer (2000); ^bBochdansky et al. (1999); ^cGorsky (1980); ^dMoloney & Field (1989); ^eGorsky et al. (1988); ^fAllredge (1976); ^gFlood et al. (1990); ^hTouratier et al. (1999); ⁱHansen et al. (1997); ^jFlood & Deibel (1998)

Table 3. *Oikopleura dioica*. Model connectivity matrix for all carbon and nitrogen flows (in $\mu\text{g} \times \text{ind.}^{-1} \text{ bottle}^{-1} \text{ d}^{-1}$, where x stands for C or N; ●: continuous flows, ▲: discrete flows). Flows are defined as follows: [D→OD]_x: detritus rejection; [F→HF]_x: food intake; [F→D]_x: accumulation of food on the inner wall of the house; [G→E]_x: release of gametes; [H→OH]_x: house rejection; [HF→FP]_x: production of fecal pellets; [HF→SB]_x: construction of structural biomass; [HF→G]_x: construction of gonads from food; [HF→R]_x: respiration/excretion from food; [HF→HR]_x: construction of house rudiment from food; [HF→D]_x: accumulation of fecal pellets on the inner wall of the house; [HR→H]_x: deployment of the house rudiment; [SB→G]_x: construction of gonads from structural biomass; [SB→R]_x: respiration/excretion from structural biomass; [SB→HR]_x: construction of house rudiment from structural biomass; [G→R]_x: respiration/excretion from gonads

Fig. 3. *Oikopleura dioica*. Variables and processes used to model Period P1 of the life cycle. Symbols and units are described in Tables 1–3

simulate this period are shown in Fig. 3. Just after hatching, the carbon weight of the animal (SB_C ; see Table 1) is initialised to that of the egg, whereas all other state variables in the model (Table 1) are set to zero. The carbon weight of the egg ($0.013 \mu\text{gC}$) is estimated assuming a diameter of $100 \mu\text{m}$ (range: 60 to $107 \mu\text{m}$; Fenaux et al. 1986, Hopcroft & Roff 1995, Fenaux 1998b), and we then use the carbon weight–trunk length relationship provided by King et al. (1980) for *Oikopleura dioica*: $\log_{10}(\text{weight}, \mu\text{gC}) = 2.6270 \log_{10}(\text{trunk length}, \mu\text{m}) - 7.1348$.

We assume that the hypothesis of strict homeostasis is valid for appendicularians (i.e. their elemental composition remains constant despite variable quality of the ingested food), as it has been shown to be the case in many other zooplankton groups such as copepods and cladocerans (see Touratier et al. 1999, 2001 and references therein). This assumption, which is partly justified by the absence of lipid storage in oikopleurids (Gorsky & Palazzoli 1989, Deibel et al. 1992), considerably reduces the number of state variables and highlights the structure of the present model. For instance, during Period P1 (see Fig. 3), variables SB_N and HR_N (Table 1) are not state variables since we assume that ratios $SB_C:SB_N$ and $HR_C:HR_N$ remain constant. These 2 ratios are parameters cnb and cnh in the model, respectively (Table 2). The value $cnb = 5.3 \mu\text{gC} \mu\text{gN}^{-1}$ was measured by Gorsky et al. (1988) for *Oikopleura dioica* and does

not differ much from that of other zooplankton groups such as copepods and euphausiids. Houses of appendicularians are primarily composed of mucopolysaccharides (Körner 1952) with a very small nitrogen content relative to the carbon (Alldredge 1976). This means that parameter cnh is expected to be much higher than cnb . Alldredge (1976) determined the C:N ratio of 12 houses newly secreted by *O. rufescens*, and she found a mean value for cnh of $250 \mu\text{gC} \mu\text{gN}^{-1}$, which we use in the present study (Table 2). The large difference between cnb and cnh prevents the utilisation of a single C:N ratio for the entire animal, as it is usually done when modelling other zooplankton groups. To describe the nitrogen compounds involved during Period P1, the state variable R_N (Fig. 3, Table 1) is the quantity of excreted products (mostly ammonium; Gorsky 1980, Gorsky et al. 1987).

C and N flows during P1 are of 2 types (Fig. 3): construction of the house rudiment from structural biomass (symbolized by $[SB \rightarrow HR]_x$), and respiration or excretion (i.e. $[SB \rightarrow R]_x$), where the subscript x stands for C or N unit (Table 3). All flows during P1 are continuous (Table 3) and their parameterisation is shown in Table 4. Respiration $[SB \rightarrow R]_C$ (see Eq. 1 in Table 4) during Period P1 depends on the ambient temperature (T), following a Q_{10} of 3.51 (Gorsky 1980) of which the 10th root is computed (parameter t_{10} in Table 2). The construction of the house rudiment in carbon or $[SB \rightarrow HR]_C$ (see Eq. 2, Table 4) follows similar rules of parameterisation. To ensure that the C:N ratio of the house rudiment will be equal to cnh , the nitrogen flow for construction of the house rudiment $[SB \rightarrow HR]_N$ must be $[SB \rightarrow HR]_C$ divided by cnh (Eq. 4 in Table 4). Ammonium excretion $[SB \rightarrow R]_N$ must then be constrained by parameters cnb and cnh , as shown in Eq. (3) (Table 4), in order to satisfy the nitrogen mass conservation.

Modelling positive growth in Period P2

The carbon weight of the animal (W_C) is defined here as the sum of the structural biomass (SB_C) and the gonads (G_C):

Table 4. *Oikopleura dioica*. Carbon and nitrogen flows for period P1 (x stands for C or N). Variables, parameters and flows are defined in Tables 1–3

Flow	Carbon	Nitrogen
$[SB \rightarrow R]_x$	$\text{res1 } t_{10}^T SB_C \quad (1)$	$\left[\frac{\text{res1}}{cnb} + \text{chr1} \left(\frac{1}{cnb} - \frac{1}{cnh} \right) \right] t_{10}^T SB_C \quad (3)$
$[SB \rightarrow HR]_x$	$\text{chr1 } t_{10}^T SB_C \quad (2)$	$\frac{\text{chr1 } t_{10}^T SB_C}{cnh} \quad (4)$

$$W_C = SB_C + G_C \quad (1)$$

A different definition could have been chosen (e.g. by adding to W_C the weight of the house rudiment and/or that of the working house, which can be considered as elements of the body), but W_C is preferred for 3 reasons: (1) it corresponds to most measurements found in the literature for appendicularian individual weights; (2) at small timescales (h), W_C is much less variable than $W_C + HR_C$; and (3) W_C is the input variable of the trunk length (TL; in μm) relationship provided by King et al. (1980):

$$TL = 10^{\left[\frac{\log_{10}(W_C) + 7.1348}{2.6270} \right]} \quad (2)$$

The *Oikopleura dioica* individual enters Period P2 as soon as the house weight of the house rudiment (HR_C) reaches a critical weight ($th\ W_C$), where parameter th (Table 2) represents a fraction of W_C . For *O. dioica*, Gorsky (1980) found that the house represents as much as 19.2% of the animal's overall carbon content, i.e. $th = 0.2376$ (Table 2); Deibel (1986 1988) found 10 to 36% for *O. vanhoeffeni*, and Alldredge (1976) gave a range of 20 to 40%. When $HR_C \geq th\ W_C$, the house rudiment HR_C is deployed around the animal to become a working house called H_C (Table 1, Fig. 4). As specified in Table 3, the deployment of a new house [$HR \rightarrow H$] $_X$ is a discrete event that occurs within the time step dt during model implementation, as follows:

if $\text{HR}_C \geq (\text{th } W_C)$ then

$$H_C^{t+dt} = HR_C^t \quad (3)$$

$$\text{HR}_C^{t+\text{dt}} = 0 \quad (4)$$

As for the house rudiment, the C:N ratio of the working house is kept constant ($H_C:H_N = \text{cnh}$).

The C and N quantities of the food available in the medium are F_C and F_{N_i} , respectively (Fig. 4, Table 1). The volume of seawater in the experimental bottle (V ; in l) is used to compute the concentrations of food ($F_C \cdot V$ and $F_{N_i} \cdot V$). When a new house is deployed, we assume that food concentrations inside and outside the house are the same. To compute the C and N weights of the food inside the house (HF_C and HF_{N_i} ; Eq. 8 and Fig. 4), the volume unoccupied by the animal inside the house (VH) must be estimated. The house length HL (in μm ; Eq. 5) is first deduced from TL (Eq. 2) assuming a constant size ratio $rl = HL:TL$ of 3.846 (Table 2; see Flood & Deibel 1998). Considering that the shape of the house is spherical, we then compute its volume HS (in μm^3 ; Eq. 6), from which VH is deduced (in l; Eq. 7) using parameter fv (i.e. the fraction of HS unoccupied by the organism; Table 2) deduced from Flood et al. (1990) on *Oikopleura vanhoeffeni*.

Fig. 4. *Oikopleura dioica*. Variables and processes used to model positive growth in Period P2 of the life cycle. Symbols and units are described in Tables 1–3

$$\text{HL} = \text{TL}_{\text{rl}} \quad (5)$$

$$\text{HS} = \frac{4\pi(\text{HL} / 2)^3}{3} \quad (6)$$

$$V_H = H_S \text{ fV } 10^{-15} \quad (7)$$

$$\text{HF}_C = \frac{F_C \text{ VH}}{V} \quad \text{and} \quad \text{HF}_N = \frac{F_N \text{ VH}}{V} \quad (8)$$

As soon as the first house is deployed, seawater filtration, food processing, and positive growth become possible. These processes depend largely on external conditions (food quantity and quality, temperature, etc.). All processes of the model during Period P2 are illustrated in Fig. 4. The maximum food intake rate (I_m ; d^{-1}) is computed from the following allometric equation:

$$\text{Im} = a(W_C 10^6)^b t 10^T \quad (9)$$

where parameters a and b are deduced from Acuña & Kiefer (2000), and Moloney & Field (1989), respectively (Table 2). The filtration rate F (l ind.⁻¹ d⁻¹) is then given by:

$$\text{if } E = 0 \text{ then } F = 0 \quad (10)$$

$$\text{if } E \neq 0 \text{ then } F = \text{Im} \frac{W_C}{k i + (E_C / V)} \quad (11)$$

where E is the food retention efficiency of the pharyngeal filter (the possible range of E is 0 to 1). When $E = 0$, the food cannot be retained by the pharyngeal filter and filtration is suspended (Eq. 10); when $0 < E \leq 1$ the food may be partially or totally captured by the pharyngeal filter and filtration is computed using Eq. (11). The half-saturation constant for food intake ($k_i = 240 \mu\text{gC l}^{-1}$; Table 2) is from Hansen et al. (1997). This value agrees with the experimental work of Acuña & Kiefer (2000), who studied the functional responses of *Oikopleura dioica*. The food intake FI_C ($\mu\text{gC ind.}^{-1} \text{d}^{-1}$) is deduced from the filtration rate as follows:

$$FI_C = F \frac{F_C}{V} \quad (12)$$

Once the food is inside the house, it can remain in suspension, be ingested by the animal or it can accumulate on the inner wall of the house. The food which is effectively ingested by the animal (I_C ; $\mu\text{gC ind.}^{-1} \text{d}^{-1}$) is calculated from the food intake FI_C :

$$I_C = FI_C \text{ ffi} \left[E + (1 - E) \frac{(HF_C / VH)}{k_e + (HF_C / VH)} \right] \quad (13)$$

where parameter ffi (Table 2) represents the fraction of the food intake available for ingestion. In the model, ffi = 0.95, which means that 95% of the food intake is available for ingestion, whereas the remaining 5% accumulates on the inner wall of the house. Gorsky (1980) and Gorsky & Palazzoli (1989) found that 25 to 37% of the material collected by appendicularians accumulate as detritus on the inner wall of the house; these higher percentages are explained by the fact that measurements were made on abandoned houses, in which the quantity of accumulated material (including feces) is largest.

From Eq. (13), 3 different cases may arise depending on the value of the retention efficiency E : (1) when $E = 1$, all filtered food (fraction ffi) is ingested since $I_C = FI_C$ ffi; (2) when $E = 0$, $I_C = 0$ since $FI_C = 0$ (see Eqs. 10 & 12); and (3) when $0 < E < 1$, the food concentration inside the house (HF_C / VH) increases since $I_C > FI_C$ ffi. According to Morris & Deibel (1993) and Acuña et al. (1996), the increasing concentration of food inside the house could favour the aggregation of particles, and thus result in an increase of the retention efficiency. In Eq. (13), we attempt to simulate this effect by using a Michaelis-Menten function where the food concentration affects the global retention efficiency (the term in brackets) through the difference $(1 - E)$.

The respiration for maintenance (RB_C ; in $\mu\text{gC ind.}^{-1} \text{d}^{-1}$) follows the parameterisation proposed by Touratier et al. (1999) for copepods:

$$RB_C = \text{Im} \frac{tf}{k_i + tf} W_C \text{ ac} \quad (14)$$

where tf is the food concentration threshold for maintenance (Table 2). Its value ($1 \mu\text{gC l}^{-1}$) was deduced

during model calibration. Ranges found in the literature for the carbon assimilation coefficient (ac , Table 2) are quite large: 0.17 to 0.88 for *Oikopleura dioica* (Gorsky 1980), and 0.42 to 0.83 for *O. vanhoeffeni* (Bochdansky et al. 1999). From the latter, a mean value of 0.67 is used. In the present section, growth must be positive, i.e. the carbon contained in assimilated food must exceed the metabolic requirements for maintenance ($I_C ac > RB_C$).

The parameterisation used for the C and N flows that characterise Period P2 when growth is positive (Fig. 4) is listed in Table 5. The nitrogen food intake (Eq. 9, Table 5) is computed from its carbon equivalent (Eq. 1, Table 5) by using the food C:N ratio ($CNF = F_C:F_N$). The food that accumulates as detritus (D_C and D_N) on the inner wall of the house is computed from Eqs. (2) & (10) (Table 5). The fraction ffp (Table 2) of the fecal pellets (FP_C and FP_N) produced by the animal is released to the medium (Eqs. 3 & 11, Table 5), whereas the remaining part $(1 - \text{ffp})$ accumulates as detritus on the inner wall of the house (Eqs. 8 & 16, Table 5). To compute the nitrogen flows, the nitrogen assimilation coefficient (an , Table 2) is set to 0.72 (Bochdansky et al. 1999).

Once assimilated, the food is used for production of new biomass and for respiration/excretion. The parameterisation of these processes is based on the stoichiometric approach developed by Touratier et al. to simulate the influence of food quantity and quality on copepod growth (for details, see Touratier et al. 1999), with the following parameterisation for appendicularians.

Since $ac \neq an$, the C:N ratio for assimilated food (CNA) differs from that for ingested food (CNF). The relationship between the 2 ratios is given by $CNA = CNF(ac:an)$. The net growth efficiency $K2$, defined as the ratio of production over assimilation when $CNA = cnb$, is computed as follows:

$$K2 = k2m \frac{I_C ac - RB_C}{k2 + I_C ac - RB_C} \quad (15)$$

Variable $K2$ reaches a maximum value $k2m$ when ingestion I_C becomes saturating, and it is null when $(I_C ac) = RB_C$. There is no estimate of $k2m$ for appendicularians, so that we chose a value typical of copepods, 0.44 for $k2m$ (Table 2) (Touratier et al. 1999).

During Period P2, the production of new biomass is the sum of 3 processes: production of (1) structural biomass SB (Eqs. 4 & 12, Table 5); (2) gonads G (Eqs. 5 & 13, Table 5); and (3) house rudiment HR (Eqs. 7 & 15, Table 5). The contribution of each process to total production is computed using the fractions $fsb2$, $fg2$ and fhr , which are equal to 0.25, 0.1 and 0.65, respectively (Table 2). These parameters are adjusted during model calibration, and 2 conditions must be satisfied concern-

Table 5. *Oikopleura dioica*. Carbon and nitrogen flows for Period P2 when growth is positive ($I_C \text{ ac} > \text{RB}_C$) (x stands for C or N). Variables, parameters and flows are defined in Tables 1–3

Flow	Carbon		Nitrogen	
$[\text{F} \rightarrow \text{HF}]_x$	$\text{FI}_C \text{ ffi}$	(1)	$\frac{\text{FI}_C \text{ ffi}}{\text{CNF}}$	(9)
$[\text{F} \rightarrow \text{D}]_x$	$\text{FI}_C (1 - \text{ffi})$	(2)	$\frac{\text{FI}_C (1 - \text{ffi})}{\text{CNF}}$	(10)
$[\text{HF} \rightarrow \text{FP}]_x$	$I_C (1 - \text{ac}) \text{ ffp}$	(3)	$\frac{I_C (1 - \text{an}) \text{ ffp}}{\text{CNF}}$	(11)
$[\text{HF} \rightarrow \text{SB}]_x$	$I_C \text{ ac K2} \frac{\text{cnb}}{\text{CNA}} \text{ fsb2}$	(4)	$\frac{I_C \text{ an K2 fsb2}}{\text{CNF}}$	(12)
$[\text{HF} \rightarrow \text{G}]_x$	$I_C \text{ ac K2} \frac{\text{cnb}}{\text{CNA}} \text{ fg2}$	(5)	$\frac{I_C \text{ an K2 fg2}}{\text{CNF}}$	(13)
$[\text{HF} \rightarrow \text{R}]_x$	$I_C \text{ ac} \left(1 - \text{K2} \frac{\text{cnb}}{\text{CNA}}\right)$	(6)	$\frac{I_C \text{ an}}{\text{CNF}} \left[1 - \text{K2} \left(\text{fsb2} + \text{fg2} + \frac{\text{cnb}}{\text{cnh}} \text{fhr}\right)\right]$	(14)
$[\text{HF} \rightarrow \text{HR}]_x$	$I_C \text{ ac K2} \frac{\text{cnb}}{\text{CNA}} \text{ fhr}$	(7)	$I_C \text{ an K2} \frac{\text{cnb}}{\text{CNF cnh}} \text{fhr}$	(15)
$[\text{HF} \rightarrow \text{D}]_x$	$I_C (1 - \text{ac}) (1 - \text{ffp})$	(8)	$\frac{I_C (1 - \text{an}) (1 - \text{ffp})}{\text{CNF}}$	(16)

ing their values: (1) mass conservation must be respected ($\text{fsb2} + \text{fg2} + \text{fhr} = 1$), and (2) the gain in carbon weight of the house rudiment (HR_C) must be higher than that of the individual's carbon weight (W_C ; see Eq. 1) since the deployment of a new house depends on the comparison between HR_C and W_C (see above). This is done by choosing $\text{fhr} > (\text{fsb2} + \text{fg2})$.

Respiration and excretion are simulated using Eqs. (6) & (14) (Table 5), respectively. Mass conservation for C and N after assimilation must be satisfied: by summing Eqs. (4) to (7) for the carbon cycle, and Eqs. (12) to (15) for the nitrogen cycle (Table 5), we obtain the assimilation of carbon ($I_C \text{ ac}$) and that of nitrogen ($I_C \text{ an:CNF}$), respectively. An important characteristic of appendicularians, however, is that $\text{cnh} \gg \text{cnb}$ (Table 2). In order to respect these ratios, it is assumed that the organism uses 250 (i.e. cnh) times less N than C during the construction of the house rudiment (compare Eqs. 7 & 15, Table 5). It follows that the resulting excess of N must be excreted to satisfy mass conservation (Eq. 14, Table 5).

The deployment of a new house consists in a sequence of discrete events that occurs as often as the house rudiment C content (HR_C) reaches a threshold defined by the product ($\text{th } W_C$):

$$\text{if } \text{HR}_C \geq (\text{th } W_C) \text{ then}$$

$$\text{OH}_C^{t+\text{dt}} = \text{OH}_C^t + \text{H}_C^t \quad (16)$$

$$\text{OD}_C^{t+\text{dt}} = \text{OD}_C^t + \text{D}_C^t; \quad \text{OD}_N^{t+\text{dt}} = \text{OD}_N^t + \text{D}_N^t \quad (17)$$

$$\text{D}_C^{t+\text{dt}} = 0; \quad \text{D}_N^{t+\text{dt}} = 0 \quad (18)$$

The full sequence of events consists of Eqs. (16) to (18), then followed by Eqs. (3) & (4) (see above). When a new house is being deployed by the animal, the old house (H_C) and the detritus (D_C and D_N) are abandoned. They accumulate in the medium as old houses (OH_C) and old detritus (OD_C and OD_N), as parameterized in Eqs. (16) & (17) (see also Fig. 4). When the house rudiment (HR_C) is deployed to become a working house (H_C ; see Eqs. 3 & 4), there is no detritus (D_C and D_N are initialized to 0; Eq. 18).

In the model, *Oikopleura dioica* enters Period P3 when trunk length TL (Eq. 2) reaches a size threshold called TL_{MGON} , computed as follows:

$$\text{TL}_{\text{MGON}} = [\text{atl}(\text{T} - 23) + \text{tlm}] \text{ttl} \quad (19)$$

Threshold TL_{MGON} decreases with increasing temperature. This effect is represented by a negative slope (atl ; Table 2). Values for parameters atl and tlm (the maximum trunk length at 23°C) were estimated from the experimental work of Gorsky (1980). Since the maximum TL of an individual (tlm) is observed just before the release of gametes, a fraction ttl (0.8, Table 2) is used to compute threshold TL_{MGON} (Eq. 19).

Modelling positive growth in Period P3

Period P3 is characterized by development of gonads. The parameterisation used to simulate the processes involved during Period P3 (Table 6; see also Fig. 5) is similar to that used during Period P2, but with the following 3 differences:

(1) The C and N used for production of structural biomass during Period P2 (Eqs. 4 & 12; Table 5) is utilised for production of gonads during Period P3 (Eqs. 4 & 12 in Table 6 are the sum of Eqs. 4 & 5, and Eqs. 12 & 13 in Table 5, respectively).

(2) Autolysis phenomena of oikoplastic and digestive cells have been observed during Period P3, indicating that some materials of the structural biomass are re-invested into the gonads. This new process is parameterised by Eqs. (8) & (16) (Table 6). During Period P3

and positive growth, the structural biomass SB always decreases, whereas the individual weight W_C ($SB_C + G_C$) always increases.

(3) Release of gametes is a discrete process (E_C , the carbon content of the gametes, is released from the gonads G_C ; see Table 1 and Fig. 5) that occurs as soon as the trunk length of *Oikopleura dioica* reaches threshold TL_{RG} , which is defined as follows:

$$TL_{RG} = atl(T - 23) + tlm \quad (20)$$

Table 6. *Oikopleura dioica*. Carbon and nitrogen flows for Period P3 when growth is positive ($I_C ac > RB_C$) (x stands for C or N). Variables, parameters and flows are defined in Tables 1–3

Flow	Carbon		Nitrogen	
$[F \rightarrow HF]_x$	$FI_C ffi$	(1)	$\frac{FI_C ffi}{CNF}$	(9)
$[F \rightarrow D]_x$	$FI_C (1 - ffi)$	(2)	$\frac{FI_C (1 - ffi)}{CNF}$	(10)
$[HF \rightarrow FP]_x$	$I_C (1 - ac) ffp$	(3)	$\frac{I_C (1 - an) ffp}{CNF}$	(11)
$[HF \rightarrow G]_x$	$\frac{I_C ac K2 cnb (fg2 + fsb2)}{CNA}$	(4)	$\frac{I_C an K2 (fg2 + fsb2)}{CNF}$	(12)
$[HF \rightarrow R]_x$	$I_C ac \left(1 - K2 \frac{cnb}{CNA}\right)$	(5)	$\frac{I_C an}{CNF} \left[1 - K2 \left(fsb2 + fg2 + \frac{cnb}{cnh} fhr\right)\right]$	(13)
$[HF \rightarrow HR]_x$	$\frac{I_C ac K2 cnb}{CNA} fhr$	(6)	$I_C an K2 \frac{cnb}{CNF cnh} fhr$	(14)
$[HF \rightarrow D]_x$	$I_C (1 - ac) (1 - ffp)$	(7)	$\frac{I_C (1 - an) (1 - ffp)}{CNF}$	(15)
$[SB \rightarrow G]_x$	$cg3 t10^T SB_C$	(8)	$\frac{cg3 t10^T SB_C}{cnb}$	(16)

Table 7. *Oikopleura dioica*. Carbon and nitrogen flows for Periods P2 and P3 when growth is zero or negative ($I_C ac \leq RB_C$) (x stands for C or N). Variables, parameters and flows are defined in Tables 1–3

Flow	Carbon		Nitrogen	
$[F \rightarrow HF]_x$	$FI_C ffi$	(1)	$\frac{FI_C ffi}{CNF}$	(8)
$[F \rightarrow D]_x$	$FI_C (1 - ffi)$	(2)	$\frac{FI_C (1 - ffi)}{CNF}$	(9)
$[HF \rightarrow FP]_x$	$I_C (1 - ac) ffp$	(3)	$\frac{I_C (1 - an) ffp}{CNF}$	(10)
$[HF \rightarrow R]_x$	$I_C ac$	(4)	$\frac{I_C an}{CNF}$	(11)
$[HF \rightarrow D]_x$	$I_C (1 - ac) (1 - ffp)$	(5)	$\frac{I_C (1 - an) (1 - ffp)}{CNF}$	(12)
$[SB \rightarrow R]_x$	$[RB_C - I_C ac] \frac{SB_C}{SB_C + G_C}$	(6)	$[RB_C - I_C ac] \frac{SB_C}{(SB_C + G_C) cnb}$	(13)
$[G \rightarrow R]_x$	$[RB_C - I_C ac] \frac{G_C}{SB_C + G_C}$	(7)	$[RB_C - I_C ac] \frac{G_C}{(SB_C + G_C) cnb}$	(14)

Fig. 5. *Oikopleura dioica*. Variables and processes used to model positive growth in Period P3 of the life cycle. Symbols and units are described in Tables 1–3

When $TL \geq TL_{RG}$, the sequence of discrete events is given by Eqs. (16) to (18) above, followed by Eqs. (21) to (23). The old house and the associated detritus are abandoned, but there is no new house (Eq. 21) as most oikoplasmic cells are empty due to the autolysis.

$$H_C^{t+dt} = 0 \quad (21)$$

$$E_C^{t+dt} = G_C^t \quad (22)$$

$$G_C^{t+dt} = 0 \quad (23)$$

Modelling zero or negative growth in Periods P2 and P3

When food concentration is very low, growth can be zero or negative. In the model, this occurs when the quantity of assimilated carbon is equal to or lower than maintenance requirements ($I_C \text{ ac} \leq RB_C$). This is simulated using equations of Table 7 that parameterise processes appearing in Fig. 6.

Food intake (Eqs. 1 & 8; Table 7), accumulation of food (Eqs. 2 & 9; Table 7) and fecal pellets (Eqs. 5 & 12; Table 7) on the inner wall of the house, and production of fecal pellets (Eqs. 3 & 10; Table 7) are parameterised in the same way as during positive growth (see Tables 5 & 6).

The priority of metabolism is to satisfy the costs of maintenance, and we assumed that respired or excreted products may originate from food, structural biomass, and/or gonads (Fig. 6).

When the carbon contained in the assimilated food exactly meets the metabolic requirements of the animal ($I_C \text{ ac} = RB_C$), growth is zero and respiration is computed using Eq. (4) of Table 7. All assimilated nitrogen must then be excreted in the medium to maintain the stoichiometry constant (Eq. 11, Table 7). Note also that respiration and excretion using C and N from structural biomass and gonads are all zero in this case (Eqs. 6, 7, 13, & 14; Table 7).

For negative growth (i.e. $RB_C > I_C \text{ ac} > 0$), all assimilated C and N from food is required for respiration and excretion (Eqs. 4 & 11, Table 7). There is not enough carbon, however, to meet all metabolic requirements, so that the organism must use carbon from its structural biomass and gonads, the contribution of each compartment being proportional to their weight (Eqs. 6 & 7, Table 7). The sum of Eqs. (4), (6) & (7) (Table 7) is equal to the respiration for maintenance (RB_C). To maintain the stoichiometry of SB and G constant, excretion is computed from respiration divided by ratio cnb (Eqs. 13 & 14, Table 7).

When food assimilation is zero ($I_C \text{ ac} = 0$), respiration and excretion using C and N from food are zero (Eqs. 4 & 11, Table 7). In this case, growth is still lower and the costs of maintenance must entirely be sustained by the C and N of SB and G (Eqs. 6, 7, 13 & 14; Table 7).

Fig. 6. *Oikopleura dioica*. Variables and processes used to model zero or negative growth in Periods P2 and P3 of the life cycle. Symbols and units are described in Tables 1–3

An important consequence of negative growth is that construction of the house rudiment is stopped. This means that as long as growth is zero or negative, the animal cannot deploy a new house. Another consequence of negative growth is that release of gametes cannot occur since individual weight (and hence trunk length) is decreasing.

The system of differential equations for the model is shown in Table 8. This system is resolved using the Runge Kutta 4th order method with a variable time step procedure.

RESULTS

Behaviour of the model

The overall behaviour of the model was explored by choosing a set of 5 experimental conditions defined as 'standard simulation': (1) volume of the experimental bottle $V = 0.04$ l; (2) carbon weight of the food $F_C = 26$ μgC ; (3) nitrogen weight of the food $F_N = 4.57$ μgN ; (4) temperature $T = 23^\circ\text{C}$; and (5) food retention efficiency of the pharyngeal filter $E = 1$. This set of experimental conditions (Expt 5, Table 9) was used by Gorsky (1980) to study the influence of temperature on trunk length of *Oikopleura dioica*. Among the 36 sets of experimental conditions that we used later to test the model (Table 9), Expt 5 was chosen as the standard simulation, because growth of *O. dioica* is maximized (one of the shortest generation times: 3.23 d from

hatching to release of gametes). Expt 5 is characterised by C and N food concentrations of 650 $\mu\text{gC l}^{-1}$ and 114.25 $\mu\text{gN l}^{-1}$, respectively, and $\text{CNF} = 5.68$ $\mu\text{gC } \mu\text{gN}^{-1}$, which is the Redfield ratio. The model is designed to simulate the growth of only 1 individual contained in an experimental bottle. In permanent routine cultures of appendicularian species (e.g. Fenaux & Gorsky 1985, Gorsky et al. 1987), animals are usually moved to a new bottle (at least once a day) where initial food levels are restored. To keep track of products released or abandoned by the animal, our simulated individual was maintained in the same bottle, but the food level was reinitialised every day at the first time step after midnight. The simulation assumes that products that accumulate in the bottle (old houses and detritus, CO_2 , NH_4^+) do not affect growth conditions.

In standard simulation the duration of the life cycle from hatching to death is 3.23 d. The individual spends 4.1, 77.1, and 18.8% of its life in Periods P1, P2 and P3, respectively (Fig. 7). Similar percentages of 6.5, 80.4, and 13.1% were estimated by Fenaux & Gorsky (1983) for *Oikopleura longicauda*, despite different experimental conditions.

Each day, larger quantities of food are filtered by the growing *Oikopleura dioica* (F_C , Fig. 7a), but food quantity is never limiting. The carbon weight of fecal pellets (FP_C) accumulates continuously in the bottle, reaching ca. 8 μgC at the end of P3 (Fig. 7a). Both the structural biomass (SB_C) and the gonads (G_C) increase during P2 (Fig. 7b). During P3, the construction of gonads is accelerated, whereas the structural biomass slowly decreases due to autolysis. At the end of P3, all gametes are released in the medium from the gonads and $G_C = 0$.

The deployment of the house rudiments is illustrated in Fig. 7c. The carbon contained in the house rudiment (HR_C) is regularly transferred to a new working house (H_C). Each time, HR_C becomes zero and H_C increases by a step. Both HR_C and H_C increase proportionally to the individual weight, whereas the frequency of house renewal decreases. Detritus (D_C) accumulates on the inner wall of the working house (H_C) as soon as the new house is deployed (Fig. 7d). The abandoned houses and their associated detritus sink to the bottom of the experimental bottle to accumulate as old houses (OH_C) and old detritus (OD_C ; Fig. 7e).

The respiration R_C of the individual generates CO_2 that accumulates in the bottle (Fig. 7f). The individual weight W_C (Fig. 7g) is defined as the sum of SB_C and G_C (Fig. 7b), but in practice the individual weight measured in laboratory may include the weight of the house rudiment and sometimes that of the house. $\text{TW}_C (= W_C + \text{HR}_C + H_C)$ represents the upper boundary for the individual weight (Fig. 7g). Consequently, the

Table 8. Differential equations of the growth model of *Oikopleura dioica*

$$\begin{aligned}
 d(D_C)/dt &= [F \rightarrow D]_C + [HF \rightarrow D]_C - [D \rightarrow OD]_C \\
 d(D_N)/dt &= [F \rightarrow D]_N + [HF \rightarrow D]_N - [D \rightarrow OD]_N \\
 d(E_C)/dt &= [G \rightarrow E]_C \\
 d(F_C)/dt &= -[F \rightarrow HF]_C - [F \rightarrow D]_C \\
 d(F_N)/dt &= -[F \rightarrow HF]_N - [F \rightarrow D]_N \\
 d(\text{FP}_C)/dt &= [HF \rightarrow \text{FP}]_C \\
 d(\text{FP}_N)/dt &= [HF \rightarrow \text{FP}]_N \\
 d(G_C)/dt &= [HF \rightarrow G]_C + [\text{SB} \rightarrow G]_C - [G \rightarrow R]_C - [G \rightarrow E]_C \\
 d(H_C)/dt &= [\text{HR} \rightarrow H]_C - [H \rightarrow \text{OH}]_C \\
 d(\text{HF}_C)/dt &= [F \rightarrow HF]_C - [\text{HF} \rightarrow \text{FP}]_C - [\text{HF} \rightarrow \text{SB}]_C - [\text{HF} \rightarrow G]_C \\
 &\quad - [\text{HF} \rightarrow R]_C - [\text{HF} \rightarrow \text{HR}]_C - [\text{HF} \rightarrow D]_C \\
 d(\text{HF}_N)/dt &= [F \rightarrow HF]_N - [\text{HF} \rightarrow \text{FP}]_N - [\text{HF} \rightarrow \text{SB}]_N - [\text{HF} \rightarrow G]_N \\
 &\quad - [\text{HF} \rightarrow R]_N - [\text{HF} \rightarrow \text{HR}]_N - [\text{HF} \rightarrow D]_N \\
 d(\text{HR}_C)/dt &= [\text{HF} \rightarrow \text{HR}]_C + [\text{SB} \rightarrow \text{HR}]_C - [\text{HR} \rightarrow H]_C \\
 d(\text{OD}_C)/dt &= [D \rightarrow \text{OD}]_C \\
 d(\text{OD}_N)/dt &= [D \rightarrow \text{OD}]_N \\
 d(\text{OH}_C)/dt &= [H \rightarrow \text{OH}]_C \\
 d(R_C)/dt &= [\text{HF} \rightarrow R]_C + [\text{SB} \rightarrow R]_C + [G \rightarrow R]_C \\
 d(R_N)/dt &= [\text{HF} \rightarrow R]_N + [\text{SB} \rightarrow R]_N + [G \rightarrow R]_N \\
 d(\text{SB}_C)/dt &= [\text{HF} \rightarrow \text{SB}]_C - [\text{SB} \rightarrow G]_C - [\text{SB} \rightarrow R]_C - [\text{SB} \rightarrow \text{HR}]_C
 \end{aligned}$$

Table 9. Experiments used to validate the individual growth model of *Oikopleura dioica*. The 5 experimental conditions required to run the model are: V, volume of seawater containing 1 individual (l); F_C , carbon weight of the food (μgC); F_N , nitrogen weight of the food (μgN); T, temperature ($^{\circ}\text{C}$); E, capture efficiency of the pharyngeal filter (without dimension). Other data shown: F_C/V , food concentration ($\mu\text{gC l}^{-1}$); F_C/F_N , C:N ratio of the food ($\mu\text{gC } \mu\text{gN}^{-1}$)

Study	Expt	V	F_C	F_N	T	E	$\frac{F_C}{V}$	$\frac{F_C}{F_N}$	Source
Influence of food level on TL	1	0.1 ^a	26 ^b	4.57	23 ^a	1	260	5.68	Gorsky (1980)
	2	0.05 ^a	13 ^b	2.28	23 ^a	1	260	5.68	Gorsky (1980)
	3	0.02 ^a	5.2 ^b	0.91	23 ^a	1	260	5.68	Gorsky (1980)
	4	0.005 ^a	1.3 ^b	0.22	23 ^a	1	260	5.68	Gorsky (1980)
Influence of T on TL and generation time	5	0.04 ^{aa}	26 ^b	4.57	23 ^a	1	650	5.68	Gorsky (1980)
	6	0.04 ^{aa}	26 ^b	4.57	20 ^a	1	650	5.68	Gorsky (1980)
	7	0.04 ^a	26 ^b	4.57	13 ^a	1	650	5.68	Gorsky (1980)
	8	4	2563.2	451.42	5	1	640.8	5.68	Simulation ^c
	9	4 ^b	2144 ^b	377.59	7.5 ^a	1	536	5.68	Paffenhöfer (1976)
	10	4 ^b	3424 ^b	603.06	12 ^a	1	856	5.68	Paffenhöfer (1976)
	11	4 ^b	2563.2	451.42	16 ^a	1	640.8	5.68	Paffenhöfer (1976)
	12	4 ^b	2563.2	451.42	18 ^a	1	640.8	5.68	Paffenhöfer (1976)
	13	4	2563.2	451.42	20	1	640.8	5.68	Simulation ^c
	14	4	2563.2	451.42	25	1	640.8	5.68	Simulation ^c
Influence of food quality (C:N ratio) on TL	15	0.1 ^a	44.98 ^b	7.06	17 ^a	1	449.8	6.37	Nin (1997)
	16	0.1 ^a	44.98 ^b	4.49	17 ^a	1	449.8	10	Nin (1997)
Influence of TL on the filtration rate	17	0.125 ^a	12.525 ^b	2.20	23.5 ^a	1	100.2	5.68	Allredge (1981)
	18	1	52.5 ^b	13.12	13.5 ^a	0.2	52.5	4	King et al. (1980)
	19	0.05 ^a	26 ^b	4.57	17 ^a	1	520	5.68	Gorsky (1980)
	20	1 ^b	53.92 ^b	9.49	13 ^a	1	53.92	5.68	Paffenhöfer (1976)
Influence of T and TL on respiration	21	0.25 ^a	17.5 ^b	3.08	15 ^a	1	70	5.68	Gorsky et al. (1987)
	22	0.25 ^a	17.5 ^b	3.08	20 ^a	1	70	5.68	Gorsky et al. (1987)
	23	0.25 ^a	17.5 ^b	3.08	24 ^a	1	70	5.68	Gorsky et al. (1987)
Influence of T and TL on excretion	24	0.1 ^a	7 ^b	1.23	15 ^a	1	70	5.68	Gorsky et al. (1987)
	25	0.1 ^a	7 ^b	1.23	20 ^a	1	70	5.68	Gorsky et al. (1987)
	26	0.1 ^a	7 ^b	1.23	24 ^a	1	70	5.68	Gorsky et al. (1987)
Influence of T and TL on the house production rate	27	0.035	26	4.57	5	1	742.8	5.68	Simulation ^c
	28	0.035	26	4.57	10	1	742.8	5.68	Simulation ^c
	29	0.035 ^a	26	4.57	14 ^a	1	742.8	5.68	Fenaux (1985)
	30	0.035 ^a	26	4.57	16 ^a	1	742.8	5.68	Fenaux (1985)
	31	0.035 ^a	26	4.57	18 ^a	1	742.8	5.68	Fenaux (1985)
	32	0.035 ^a	26	4.57	20 ^a	1	742.8	5.68	Fenaux (1985)
	33	0.035 ^a	26	4.57	22 ^a	1	742.8	5.68	Fenaux (1985)
	34	0.035	26	4.57	25	1	742.8	5.68	Simulation ^c
	35	1	136.1 ^a	21.36	13 ^a	1	136.1	6.37	Gorsky (1980)
	36	1	136.1 ^a	21.36	20 ^a	1	136.1	6.37	Gorsky (1980)

^aData originates directly from the referenced paper
^bData originates from the referenced paper, but a conversion factor is used to adapt the units to the present study
^cSimulations used to increase the range of temperature tested with the model

measured individual weights should be somewhere between W_C and TW_C , depending on the presence/absence of the house rudiment and house around the animal.

Food C:N ratio (CNF) is kept constant at $5.68 \mu\text{gC } \mu\text{gN}^{-1}$ during the standard simulation; fecal pellets have a higher C:N ratio of $6.69 \mu\text{gC } \mu\text{gN}^{-1}$ (Fig. 7h), since $a_n > a_c$ (Table 2). C:N ratios for detritus ($D_C:D_N$) and old detritus ($OD_C:OD_N$) are equal (ca. $5.9 \mu\text{gC } \mu\text{gN}^{-1}$; Fig. 7i). Since detritus originates from food and fecal pellets, its C:N ratio mirrors their relative contributions. During P1, the C:N ratio for respired over

excreted products is very low with $R_C:R_N = 0.17 \mu\text{gC } \mu\text{gN}^{-1}$ (Fig. 7j). The construction of the house rudiment during P1 is a predominant process (Fig. 3 and Table 4) responsible for the extremely low value of $R_C:R_N$. Relative to respiration, ammonium excretion is increased (excess N is eliminated) to maintain a constant cnh ratio in the house rudiment. Thereafter, during Periods P2 and P3, $R_C:R_N$ increases to about $3.5 \mu\text{gC } \mu\text{gN}^{-1}$ due to the beginning of feeding large quantities of high quality food (i.e. CNF ratio). Nutrition affects respiration, excretion, and their ratios. The elemental composition of the structural biomass, of the gonads (i.e. cnb ;

Fig. 7. *Oikopleura dioica*. Results of the model for the standard simulation: (a) carbon weight of food (F_C) and fecal pellets (FP_C) in the medium; (b) carbon weight of the structural biomass (SB_C) and gonads (G_C); (c) carbon weight of the house rudiment (HR_C) and of the working house (H_C); (d) carbon weight of detritus accumulated on the inner wall of the working house (D_C); (e) carbon weight of abandoned houses (OH_C) and of detritus accumulated on their inner wall (OD_C); (f) carbon weight of respired products (R_C); (g) individual carbon weights (W_C and TW_C); (h) C:N ratio of food ($F_C:F_N$) and fecal pellets ($FP_C:FP_N$) in the medium; (i) C:N ratio of detritus accumulated on the inner wall of the working house ($D_C:D_N$) and of abandoned houses ($OD_C:OD_N$); (j) C:N ratio of respired to excreted products ($R_C:R_N$), and C:N ratio of the individual ($TW_C:TW_N$); (k) filtration rate (F); (l) carbon food intake (FI_C), carbon assimilation ($I_{C\text{ ac}}$) and respiration for maintenance (RB_C); (m) individual growth rate; (n) house production rate.

Horizontal bars above the upper panels denote Periods P1, P2, and P3

Table 2), and hence that of the individual (i.e. ratio $W_C:W_N$) remain constant. Ratio $TW_C:TW_N$, defined as $(W_C + HR_C + H_C) : (W_N + HR_N + H_N)$, ranges from cnb to ca. 7.3 (Fig. 7j). This variability is induced mainly by the weight of the house rudiment (HR_C ; Fig. 7c) that changes the relative contribution of cnh within $TW_C:TW_N$.

The filtration rate F (Fig. 7k) computed from Eqs. (10) & (11) increases with W_C (Fig. 7g). The jumps of F at the beginning of Days 2 and 3 are due to the daily restoration of the food level (Fig. 7a). The sudden variation in the food level also affects food intake (FI_C) and assimilation of carbon (I_C ac), as shown in Fig. 7l. Growth is negative during Period P1, but it is positive during Periods P2 and P3 (Fig. 7m) since assimilated carbon always exceeds largely maintenance needs (I_C ac > RB_C ; Fig. 7l). Just after Period P1, the growth rate reaches a maximum of ca. 11 d^{-1} . It then decreases slowly to a minimum of ca. 2 d^{-1} with the increasing individual weight.

During the first day of the life period, 18 houses are produced by the animal (Fig. 7n). The rate is then lowered to 13 and 8 houses during Days 2 and 3, respectively.

From the standard simulation, a carbon budget can be drawn for the individual. From the $25.38 \mu\text{gC}$ of food filtered by the organism during the 3.23 d of its lifetime, 5.8% ends as detritus (OD_C), 14% is in the form of old houses (OH_C), 36% is respired (R_C), 30% is ejected as faecal pellets, and 6.42% is invested into the eggs. The remaining 7.8% represents the cadaver of the individual. A considerable amount of carbon is lost through respiration, but 58% of the carbon ingested by an individual may sink in the water column as large particles.

Comparison between observations and model output

Several experimental data sets for *Oikopleura dioica* were used to test the response of the individual growth model. Experimental conditions and results of Gorsky (1980), Paffenhöfer (1976), Nin (1997), Alldredge (1981), King et al. (1980), Gorsky et al. (1987), and Fenaux (1985) are available to study (1) the influence of the food level on individual trunk length (TL); (2) the influence of temperature (T) on TL and generation time; (3) the influence of food quality on TL; (4) the influence of TL on filtration rate; (5) the influence of T and TL on respiration; (6) the influence of T and TL on excretion; and (7) the influence of T and TL on house production rate (see Table 9). Each of the 36 experiments in Table 9 is characterized by a set of 5 experimental conditions (V, F_C , F_N , T, and E) often derived from the source paper. Table 2 provides the values for all parameters of the model.

Influence of food level on trunk length

Expts 1 to 4 in Table 9 analyse the influence of the food level on TL. The primary goal of Gorsky (1980) was to determine the minimum food level required to allow positive growth and maturation of gonads. Results of these experiments are also presented by Gorsky & Palazzoli (1989). Seawater filtered by $50 \mu\text{m}$, originating from the Bay of Villefranche (French Mediterranean coast), was used for the cultures. In the 4 bottles containing 1 l of seawater each, 10, 20, 50, and 200 individuals (selected just after the shift of the tail) were cultured. Since the growth of only 1 individual is simulated by the model, the volume of seawater per individual varies accordingly (V, Table 9). The original units of the food level used by Gorsky (1980) are ' μm^3 food particles $\text{ind.}^{-1} \text{ d}^{-1}$ ', which need to be transformed into carbon equivalents. This is done by using a conversion factor of $200 \mu\text{gC mm}^{-3}$ proposed by Mullin et al. (1966) for phytoplankton. Since the food supplied each day by Gorsky (1980) consisted of a mixture of phytoplankton species, we apply this factor to estimate the carbon weight of the food (F_C , Table 9). From Expts 1 to 4, it must be noted that both V and F_C decrease, but that food concentration $F_C:V$ remains constant (Table 9). The nitrogen weight of the food (F_N) is also required to implement the model, but it cannot be estimated from the source paper. The Redfield C:N ratio of $5.68 \mu\text{gC } \mu\text{gN}^{-1}$ is applied to compute F_N . We thus assume that healthy phytoplankton was supplied in the cultures. The temperature (T) is kept constant at 23°C during the experiments, and we consider that all food particles could efficiently be retained by the pharyngeal filter ($E = 1$; Table 9).

The results of the simulations are shown in Fig. 8. As observed in the cultures, generation time increases with decreasing food levels. Observed and simulated maximum TL remain constant however (ca. $750 \mu\text{m}$). When simulating Expt 4 with the model, the individual was not able to reach threshold TL_{RG} . This indicates that the food quantity of $1.3 \mu\text{gC}$ supplied each day was not enough to trigger the release of gametes. It is similar to the conclusions of Gorsky (1980) and Gorsky & Palazzoli (1989) that the food level used during Expt 3 ($26 \times 10^6 \mu\text{m}^3$ food particles $\text{ind.}^{-1} \text{ d}^{-1}$, which corresponds to $5.2 \mu\text{gC ind.}^{-1} \text{ d}^{-1}$ in the present study) was the minimum required to induce the release of gametes.

Influence of temperature on trunk length and generation time

The experimental data sets originated from Gorsky (1980) and Paffenhöfer (1976). Simulations corresponding to those of Gorsky (1980) use Expts 5 to 7 as

Fig. 8. *Oikopleura dioica*. Comparison between experimental observations and model simulations: influence of food level on individual trunk length. Experimental conditions are listed in Table 9

experimental conditions (Table 9), where only the temperature T varies (23, 20, and 13°C, respectively). Similar conversion factors (volume of food particles to carbon, and C:N ratio; see above) were used to estimate F_C and F_N . In these experiments, food concentration was much higher ($F_C \cdot V = 650 \mu\text{gC l}^{-1}$). Increasing the food concentration is a good strategy to obtain saturation of ingestion, since $F_C \gg k_i$, and thus to focus on the effect of temperature on growth only. The results of the 3 simulations are shown in Fig. 9a–c. When temperature decreases, generation time and maximum trunk length TL_{RG} increase. Although these characteristics are well reproduced by the model, it is clear that the model overestimates generation time and threshold TL_{RG} in Expt 7. This may indicate that either the slope at_l (Table 2) used in Eqs. (19) & (20) is underestimated, or that the life cycle of the cultured individuals (10 individuals in 0.4 l) was not yet completely finished, as discussed by Gorsky (1980).

Using seawater from the North Sea filtered through a 180 μm mesh, Paffenhöfer (1976) measured the gen-

Fig. 9. *Oikopleura dioica*. Comparison between experimental observations and model simulations: influence of temperature on individual trunk length. Experimental conditions are listed in Table 9

eration time of *Oikopleura dioica* cultured under various conditions of temperature (from 7.5 to 18°C). These data provide a good opportunity to test the behaviour of the present model, but many uncertainties exist on the conditions F_C and F_N to apply in the model. From the chlorophyll *a* (chl *a*) concentrations given by Paffenhöfer (1976), we estimate F_C by using a POC:chl *a* ratio of 400 $\mu\text{gC} (\mu\text{g chl } a)^{-1}$. The utilisation of these data is complicated by the fact that the exact number of individuals in the cultures is unknown. These uncertainties would be of less importance if the food levels were saturating. We cannot affirm it, but we assume it is true, given the large quantities of carbon present in the food, as deduced from the above approximations.

The range of temperature used by Paffenhöfer (1976) was analysed using Expts 9 to 12, characterised by temperatures of 7.5, 12, 16, and 18°C, respectively. Since *Oikopleura dioica* is a species with worldwide

distribution, it is interesting to extend the range of temperatures tested with the model. The effect of temperatures as low as 5°C (Expt 8) and as high as 20 and 25°C (Expts 13 and 14, respectively) on the generation time were thus analysed. Results of the 7 simulations corresponding to Expts 8 to 14 and Paffenhöfer's data are presented in Fig. 9d. The simulated generation times do not differ significantly from those observed by Paffenhöfer (1976). Given the very large range of temperatures tested (5 to 25°C), the simulated generation times may vary between approximately 2 and 40 d.

Influence of food quality (C:N ratio) on trunk length

The influence of the elemental composition of substrates assimilated by bacteria or ingested by zooplankton, and the consequences on the overall structure of food webs, are debated in the recent literature (e.g. Urabe et al. 1995, Brussaard & Riegman 1998, Touratier et al. 2001). The sole data available on this topic for appendicularians are those measured by Nin (1997) in G. Gorsky's laboratory at Villefranche sur Mer. Twenty *Oikopleura dioica* individuals cultured in a bottle filled with 2 l of filtered seawater were fed with the small flagellate *Isochrysis galbana* cultured either under nitrate unstarved or starved conditions. Expts 15 and 16 (Table 9) are designed to simulate the results of Nin (1997). The food quantity F_C was estimated using a specific conversion factor of $346 \mu\text{gC mm}^{-3}$ provided by Gorsky (1980) for *I. galbana*. Surprisingly, the food C:N ratios for both starved and unstarved *I. galbana* are not available for these experiments. Consequently, for nitrate unstarved *I. galbana* we assume a C:N ratio of $6.37 \mu\text{gC } \mu\text{gN}^{-1}$, as recommended by Gorsky (1980). For nitrate starved cells, we assume that a C:N ratio of $10 \mu\text{gC } \mu\text{gN}^{-1}$ is an appropriate choice. The food quantities F_N for Expts 15 and 16 were computed from F_C and these ratios (Table 9).

Simulated results are compared to the observations in Fig. 10. The data of Nin (1997) show that when food quality decreases (i.e. increasing C:N ratio), the generation time increases and TL_{RG} is lowered. The model predicts that the generation time increases in response to a poor quality of the food, but unrealistic outputs are generally obtained: TL_{RG} remains constant and the predicted generation times are much longer than observed. To improve the overall quality of the simulated results, we changed the value of the 2 parameters a and k_i in the model (Table 2) to be more representative of the specific prey (*Isochrysis galbana*). The experimental work of Acuña & Kiefer (2000) suggests that values of $a = 49.51 \text{ pgC}^{0.25} \text{ d}^{-1}$ and $k_i = 38.9 \mu\text{gC l}^{-1}$ could be more appropriate to simulate the influence of this alga on growth of *Oikopleura dioica*. Better results

Fig. 10. *Oikopleura dioica*. Comparison between experimental observations and model simulations: influence of food quality (C:N ratio) on individual trunk length. Experimental conditions are listed in Table 9

are obtained with the model using this specific set of parameters (Fig. 10), but the difference remains important. Concerning the generation time, it must be noted, however, that Nin's data (Fig. 10a) are not always coherent with those of Paffenhöfer (1976): Fig. 9d shows that the generation time at 17°C (i.e. the temperature of Nin's experiments) should be 8 or 9 d instead of ca. 5 d as in Fig. 10a. The reason for such a disagreement between the 2 studies is unknown.

Influence of the trunk length on the filtration rate

The data sets of Alldredge (1981), King et al. (1980), Gorsky (1980), and Paffenhöfer (1976) were used to test the response of the present model to the filtration rate (Expts 17 to 20 in Table 9). Only the regression curves available from the original papers instead of the data themselves are presented here.

The *in situ* filtration rates of *Oikopleura dioica* were estimated by Alldredge (1981) in the surface waters of the Gulf of California during July 1979. The volume of the feeding chamber containing 1 *O. dioica* was 0.125 l (V of Expt 17 in Table 9). The averaged food concentration (POC) during the experiments was $120 \mu\text{gC l}^{-1}$, but according to the author a mean of 83.5% passed through the incurrent filters of the house (see Alldredge 1981 for details). The food concentration available for growth was thus $100.2 \mu\text{gC l}^{-1}$, which translates to $F_C = 12.5 \mu\text{gC}$ (see Table 9). The quantity F_N

Fig. 11. *Oikopleura dioica*. Comparison between experimental observations and model simulations: influence of individual trunk length on filtration rate. Experimental conditions are listed in Table 9

was computed assuming that the C:N Redfield ratio is representative of the available food. The average temperature during the experiments was 23.5°C. The regression curve determined by Alldredge (1981) and the simulated results are presented in Fig. 11a. It must be noted, however, that in the experiments conducted by Alice Alldredge, several individuals of different sizes were enclosed separately in the chamber for the duration of the measurement only. The life history of these individuals is thus completely unknown, whereas the model simulates the development of an individual whose life history is completely known. The trunk length of individuals used by Alldredge (1981) was generally larger (600 to 1300 μm) than that computed with the model (<715 μm). Among the factors analysed above (food level, temperature, and food quality), only the temperature could explain the difference, since T and TL are inversely correlated (see 'Influence of temperature on trunk length and generation time', and Fig. 9a–c). From this, we suspect that

the life history of the individuals used by Alldredge (1981) could have been marked by cold periods. Interestingly, the regression curve of Alldredge (1981) is in continuity with that computed by the model, which indicates that the simulated filtration rates could be realistic for small-sized individuals.

One objective of King et al. (1980) was to estimate the filtration rate of *Oikopleura dioica* when it was fed with natural assemblages of free-living bacteria at Saanich Inlet, Canada. We assumed that the volume of 10 μm filtered seawater placed in the bottle was 1 l; this information is not given by King et al. (1980). The mean bacterial biomass reached 52.5 $\mu\text{gC l}^{-1}$, and thus $F_C = 52.5 \mu\text{gC}$ (see Expt 18 in Table 9). F_N was estimated from F_C using a bacterial C:N ratio of 4 $\mu\text{gC } \mu\text{gN}^{-1}$ (Lancelot & Billen 1985). The temperature during the experiments was maintained at 13.5°C. The capture efficiency E of the pharyngeal filter is roughly estimated at 0.2 (Table 9) from the particle size retention spectra proposed by Acuña et al. (1996) for *O. vanhoeffeni*, considering that the size of bacterial cells ranges from 0.2 to 2 μm (Painting 1989). As previously, the history of the individuals is unknown, but the simulated results are coherent with the observations (Fig. 11b).

Gorsky (1980), using 50 μm filtered seawater from the Bay of Villefranche sur Mer, also provided estimates of the filtration rates for *Oikopleura dioica*, as represented by the linear regression in Fig. 11c. Using the experimental conditions of Expt 19 (Table 9), the simulated results are in the range of the experimental data.

Finally, the filtration rates estimated by Paffenhöfer (1976) were simulated using the conditions of Expt 20 (Table 9) and seawater cultures of 4 l. We assumed that 4 individuals (the exact number is unknown) were used in each bottle, i.e. $V = 1 \text{ l}$. The factor of Mullin et al. (1966) previously used to convert the volume of food particles into carbon equivalents was also applied to the original data, and $F_C = 53.92 \mu\text{gC}$ (Table 9). F_N was deduced from F_C using the Redfield C:N ratio. The temperature was 13°C and E was set to 1. The difference between the observed and the simulated rates is obvious, and it increases with body size. We suspect, however, that the present model is more realistic than Paffenhöfer's data, since (1) the results of the present model are coherent with 3 other independent data sets (Fig. 11a–c); (2) King et al. (1980) and Gorsky (1980) already pointed out the overestimated filtration rates obtained by Paffenhöfer (1976), especially because the number of individuals present in the cultures could have been underestimated; and (3) it is unnatural that the maximum filtration rates obtained by Alldredge (1981) and Paffenhöfer (1976) should be similar (compare Fig. 11a,d) considering a difference in temperature of 10.5°C between the 2 experiments (Table 9).

Influence of temperature and trunk length on respiration rate

Respiration of *Oikopleura dioica* was analysed by Gorsky et al. (1987). The animals were first maintained in culture, and individuals of various sizes were introduced into beakers of 0.25 l containing 30 μm filtered seawater for 4 to 8 h to determine their respiration rates. A volume of food particles equivalent to 70 $\mu\text{gC l}^{-1}$ (conversion factor of Mullin et al. 1966) was added to the medium as soon as the individuals were incubated. This food concentration corresponds to $F_C = 17.5 \mu\text{gC}$, and F_N was computed using the Redfield C:N ratio. E was set to 1. Temperatures differed among the 3 experiments (15, 20 and 24°C for Expts 21 to 23 in Table 9, respectively). In the model, the respiration rate (R_C) is computed in terms of carbon. To compare them to the experimental data of Gorsky et al. (1987), the simulated results were converted into oxygen units using a respiratory quotient ($\text{CO}_2:\text{O}_2$) of 0.87, as calculated by Gorsky (1980). Results of the simulation are shown in Fig. 12. The respiration rates increase with both TL and T, 2 characteristics that are well reproduced with the model. For $T \geq 20^\circ\text{C}$, some experimental points (where TL is maximum) could not be resolved with the model. This could be due to the experimental procedure adopted by Gorsky et al.

Fig. 12. *Oikopleura dioica*. Comparison between experimental observations and model simulations: influence of temperature and individual trunk length on respiration rate. Experimental conditions are listed in Table 9

(1987) that does not consider the life history of individuals prior to the experiments. The oscillations in the respiration rate result from the food level that becomes more and more limiting with the increase of the individual weight.

Influence of temperature and trunk length on excretion rate

Another goal of the Gorsky et al. (1987) study was to measure excretion rates using animals of different sizes, and at various temperatures. The overall experimental procedure followed that adopted to determine respiration rates (see details in Gorsky et al. 1987). However, the volume of the beakers was smaller (0.1 l), and F_C was consequently reduced to 7 μgC (see Expts 24 to 26 in Table 9). The outputs of the model and the experimental data are compared in Fig. 13. Excretion rate also increased with both TL and T. This is reproduced by the model, but simulated results corresponding to the highest temperature are slightly overestimated. The amplitude of the oscillations increases with TL, especially when the temperature is low.

Influence of temperature and trunk length on house production rate

During appendicularian bloom events, abandoned houses may represent a large fraction of the total carbon export (Fortier et al. 1994). This effect is accentuated by the high potential of houses to aggregate around suspended particles. It is therefore interesting to evaluate the house production rate of appendicularians, which is largely affected by temperature and individual trunk length. The experimental studies of Fenaux (1985) and Gorsky (1980) on *Oikopleura dioica* provide a nice opportunity to test the ability of the present model to approach such measurements.

Using filtered seawater originating from the Bay of Villefranche sur Mer, Fenaux (1985) measured the house production rate of individuals maintained at 5 temperatures (14, 16, 18, 20 and 22°C) whose trunk length ranged from 500 to 600 μm (see Expts 29 to 33 in Table 9). Prior to the measurements, the individuals were first cultured at 18°C and then adapted to the experimental temperature during a period of 24 h. Fenaux (1985) used beakers of 0.35 l, with 10 individuals per beaker ($V = 0.035 \text{ l}$, Table 9). Neither the quantity of food nor its quality were specified by Fenaux (1985). We hypothesize that (1) food level was at saturation ($F_C = 26 \mu\text{gC}$; food concentration is thus 742.8 $\mu\text{gC l}^{-1}$, Table 9); (2) the food supplied each day into the beakers was of high quality (i.e. the Redfield

Fig. 13. *Oikopleura dioica*. Comparison between experimental observations and model simulations: influence of temperature and individual trunk length on excretion rate. Experimental conditions are listed in Table 9

C:N ratio was used to calculate F_N from F_C , Table 9); and (3) all food particles were efficiently captured by the pharyngeal filtering apparatus (i.e. $E = 1$). In the model, as during the experiments, house production rates were computed when individuals had trunk lengths of 500 to 600 μm . Three additional temperatures are tested with the model (5, 10 and 25°C ; Expts 27, 28, and 34 of Table 9). Although they are slight overestimates, the simulated results are in agreement with the observations (Fig. 14a). Clearly, house production rate increases with temperature. Concerning the range of temperature (14 to 22°C) experimentally tested by Fenaux (1985), one of his conclusions was that the relationship between house production rate and temperature could be adequately fitted by a straight line, but that it should actually be sigmoid. The simulated curve (Fig. 14a) is neither linear nor sigmoid, but exponential, which is a direct consequence of the parameterisation adopted to represent the influence of temperature (Q_{10}) on processes of the model (see above).

Individual trunk length also influences the duration of house functioning, as shown by Gorsky (1980). Two experiments (Expts 35 and 36 of Table 9) were designed to evaluate the duration of house functioning during the life time of an individual cultured at either 13°C , or 20°C . The volume V was set to 1 l, and the food concentration used in the model, $F_C:V = 136.1$

$\mu\text{gC l}^{-1}$, was the same as in Gorsky (1980). In fact, approximately 10^4 cells ml^{-1} of *Isochrysis galbana* containing in average $1.3 \cdot 10^{-5} \mu\text{gC cell}^{-1}$ were added each day into the bottles filled with filtered (0.45 μm) sea-water (Gorsky 1980). The observations and the simulated results are compared in Fig. 14b & c. The duration of house functioning increases with individual trunk length, and decreases with increasing temperature. The simulation with the usual set of parameters gave poor results. When the *I. galbana*-specific set of parameters a and k_i (see 'Influence of food quality [C:N ratio] on trunk length') is used, better results are obtained with the model, but they are still far from the observations.

The deployment of a new house takes only a few minutes (Alldredge 1981, Fenaux 1985), the relationship between the duration of the house functioning (DHF) and the house production (HPR) is obvious ($\text{HPR} = 24/\text{DHF}$). This relationship was used to compare the experimental results of Gorsky (1980; Fig. 14b,c) with those of Fenaux (1985; Fig. 14a). At $T = 13^\circ\text{C}$ and $\text{TL} =$

Fig. 14. *Oikopleura dioica*. Comparison between experimental observations and model simulations: influence of temperature and individual trunk length on house production rate. Experimental conditions are listed in Table 9

550 μm (i.e. the mean size of the individuals considered by Fenaux 1985), the duration of the house functioning is ca. 2.5 h (Fig. 14b), for a house production rate of ca. 9.6 houses $\text{ind.}^{-1} \text{d}^{-1}$. At $T = 20^\circ\text{C}$ and $\text{TL} = 550 \mu\text{m}$ (Fig. 14c), the appendicularian house lasts only 1 h, for a house production rate of 24 houses $\text{ind.}^{-1} \text{d}^{-1}$. When these rates are reported on Fig. 14a, the difference between the 2 data sets is striking. The discrepancy noted between these observations could partly explain the low quality of the simulated results which appear in Fig. 14b,c.

DISCUSSION AND CONCLUSIONS

The large spectrum of simulated situations in stable conditions provides a good validation of the model, as modelled growth usually agreed with experimental data. This concerns the influence of food quantity and temperature on generation time and trunk length, influence of temperature and trunk length on respiration and excretion, and on filtration and house production rates.

Nevertheless, 3 main inconsistencies appear between model output and experimental observations: (1) the influence of food quality using the data of Nin (1997), (2) the filtration rate using the data set of Paffenhöfer (1976), and (3) the house production rates using the observations of Gorsky (1980; see Figs. 10, 11d & 14b,c). As mentioned in 'Influence of the trunk length on the filtration rate', the filtration rate measured by Paffenhöfer (1976) differs from the other data sets (i.e. Gorsky 1980, King et al. 1980, Alldredge 1981), and the inconsistency may originate from the data, and not from the model. The same applies to the house production rates measured by Gorsky (1980) and Fenaux (1985). The discrepancy between model output and the data of Nin (1997) concerning the influence of food quality on individual growth cannot be explained without additional experiments. The *Isochrysis galbana*-specific set of parameters (Fig. 10) improved the simulated results, but they are still far from the experimental observations.

Among the 36 experiments listed in Table 9, there is none where all 5 conditions (V , F_C , F_N , T , and E) are obtained directly from a referenced paper. For instance, the volume of seawater or the number of individuals in the culture is sometimes unknown, as in King et al. (1980) and Paffenhöfer (1976), respectively. In most cases, the quantity or concentration of food was determined, but the units (volume of food particles or chl *a*) often necessitate the utilisation of approximate conversion factors in order to obtain the equivalent in terms of carbon, as in Paffenhöfer (1976), Gorsky (1980), and Gorsky et al. (1987). When using

natural seawater to feed appendicularians during their experiments, scientists should determine the concentration of small particles (colloids, viruses, bacteria, and picoplankton) to correctly evaluate the ration of available food. This could help to understand the role of these organisms in their experiment. The C:N ratio of the food is never specified in the experiments, even when the aim of the study was to test the influence of food quality on individual growth (Nin 1997). As a first approximation, the C:N Redfield ratio was widely used to estimate F_N from F_C . The life history of an organism should be accurately known, since it determines a large part of the physiological response during an experiment. As discussed previously, the results obtained by Alldredge (1981) and Gorsky et al. (1987) were affected by the animals' life histories.

For modelling studies, as well as for the overall understanding and interpretation of the physiological responses of individuals during experiments, we recommend a rigorous description of the following experimental conditions: (1) volume of seawater used; (2) exact number of individuals per incubation; (3) food quantity in terms of carbon, nitrogen, and eventually phosphorus; (4) temperature; (5) life history of the experimental organisms; and (6) size spectrum of food particles supplied to the culture, to estimate the animals' capture efficiency. Moreover, given the large range of values on the assimilation efficiencies (AE) of appendicularians published, it would be useful to determine the AE for different prey types.

Especially in the case of P-limited ecosystems such as the Mediterranean Sea (Thingstad & Rassoulzadegan 1995, Thingstad et al. 1998) we strongly recommend to measure the appendicularian compartments (body, house) and processes (ingestion, assimilation, excretion) in terms of phosphorus. This is for the following reasons: (1) there is practically no estimate of P in the literature on appendicularians; (2) the so-called 'growth rate hypothesis' (Sterner 1995, Elser et al. 1996) states that rapidly growing heterotrophs (e.g. appendicularians) have a higher P content (mainly due to ribosomal RNA) than slow-growing organisms (see also Main et al. 1997, Vrede et al. 1999); and (3) heterotrophs with higher P content could favor or accentuate P limitation in ecosystems by sequestering P in their biomass (e.g. Hassett et al. 1997, Touratier et al. 2001).

The overall effect of food quality (elemental composition, size of particles, and protein or lipid content) on growth should be further explored both *in situ* and in the laboratory, and at the individual, population and ecosystem levels.

The experiments conducted during the EC's EURAPP project provide further opportunities to test the structure and behaviour of the present model. The next step

will be to consider experiments with fluctuating food quantity and quality, temperature, and size of nutritive particles, to simulate the natural variability of these parameters. Another step will be to model the population dynamics of *Oikopleura dioica* and other representative appendicularian species to analyse competition among appendicularian species, and between appendicularians and copepods, for instance (see the model proposed by Carlotti & Hirche 1997). However, the high number of state variables (18) in the present individual growth model is a handicap for reaching this level of complexity. Some aggregations of the state variables should be tested in order to reduce their number, speed up the model implementation, and consequently simulate realistically the dynamics of a population.

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