INTRODUCTION

Ocean turbulence at all scales is generated by a variety of energy sources that create instabilities. Winds, waves and currents are the commonly recognized sources of turbulent energy in the ocean (Pond & Pickard 1989). Waves at the ocean surface give rise to turbulent energy when they break. Internal waves can become unstable and break up into turbulence as they propagate through vertical density gradients. Surface winds create shear that can lead to instabilities, causing flow to become turbulent. At relatively large scales, the shear instabilities along permanent currents such as the Gulf Stream create geostrophic turbulence in the form of long-lived eddies.

Turbulent energy is transferred from large to small scales via the energy cascade. Large eddies break into smaller eddies, but turbulent energy is not dissipated until the eddy scale becomes small enough to be dominated by molecular viscosity. At this scale, viscous forces overcome the velocity gradients and the kinetic energy of turbulent motion is finally converted to heat.

Marine animals are often viewed as the subjects of turbulence. Rothschild & Osborn (1988) advanced the theory that, at scales of the individual animal, turbulence would enhance prey contact rates and effectively increase food availability. Indeed, feeding by copepods and larval fish is enhanced at moderate levels of turbulence, but diminished at higher levels (Kiørboe & Saiz 1995, MacKenzie & Kiørboe 2000, Visser et al. 2001). Turbulence can alter copepod swimming behavior, inducing changes in the frequency of swimming events and eliciting high-speed escape reactions (Costello et al. 1990, Hwang & Strickler 1994, Caparroy et al. 1998). Microscale turbulence acts similarly on larval fish activity levels (MacKenzie & Kierboe 1995, Dower et al. 1997).
Individual animals are also well recognized as a source of turbulence. Many animals typically swim at speeds that produce turbulent flow, leaving added kinetic energy in their wake (Vogel 1981, Azuma 1992). Modern hydrodynamic analysis of swimming was pioneered almost simultaneously in studies of crustaceans, fishes and cetaceans (Lighthill 1970, Vlymen 1970, Wu 1971). Research was initially focused on elucidating the mechanics of swimming and estimating hydrodynamic characteristics. More recently, the nature of vortex trails created by swimming fishes has come to light through the use of particle image velocimetry and greatly enhanced computational power (Müller et al. 1997, Cheng & Chahine 2001, Videler et al. 2002). However, studies of animal swimming have tended to focus primarily on energetic consequences for the animal rather than on energetic consequences for the fluid medium. Swimming animals transfer energy into the water that must ultimately be dissipated on the scale of the individual. What happens at larger scales? Is it possible, for example, that a school of fish could effectively mix the pycnocline? These questions appear to be unanswered.

In this paper we investigate the proposition that animal kinetic energy is an important source of turbulence in the ocean. We quantify the rate of energy production of individual animals, and show it to be related to body mass. We then estimate energy production rates at scales of social aggregation. Finally, we compare the resultant rate of kinetic energy production with observed rates of turbulent energy dissipation. We consider 4 species in detail: Atlantic bluefin tuna, northern anchovy, Norwegian spring-spawning herring, and Antarctic krill. We identify rules that apply to school dimensions, their packing density, their location in the water column, and the kinetic energy they produce at relevant scales in time and space.

**DATA AND DEFINITION OF TERMS**

We present data on swimming speeds of 98 species in 9 taxonomic categories that include one bacterium, 4 species of protozoans, 24 species of crustaceans, 1 mollusc, 41 species of fishes, 2 species of reptiles, 3 species of birds (penguins), and 22 species of mammals (Appendix 1 at www.int-res.com/journals/suppl/huntley_appendix.pdf). All the empirical constants presented *de novo* in this article, with the exception of those for the relationship between packing density and animal mass, are based on the data summarized in Appendix 1. Table 1 includes the definitions and, where appropriate, dimensions of all variables and constants.

**Swimming speed.** We distinguish between 2 characteristic swimming modes: cruising and escape. Cruising speed is that which can be maintained for long periods of time, or indefinitely, depending upon the species. Escape speed is maintained for only brief periods while an animal escapes a predator or pursues prey; in the fish literature this mode is referred to as burst swimming (e.g. Fish et al. 1991).

The definition of swimming speed depends upon the taxonomic group under consideration. In fishes, cruising speed is best defined as the metabolically optimal swimming speed, at which the work per distance traveled, measured as oxygen consumption in J m⁻¹, is minimal (Videler & Nolet 1990). Few measurements exist of oxygen consumption for swimming mammals, so their cruising speeds are usually known only from direct observations. Swimming of many crustaceans is not continuous, especially at low Reynolds numbers (Re). This is particularly true of microcrustaceans such as copepods; their cruising behavior

<table>
<thead>
<tr>
<th>Variable</th>
<th>Definition</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>Mass-normalized swimming velocity constant</td>
<td>m s⁻¹ kg⁻¹</td>
</tr>
<tr>
<td>A_k</td>
<td>Vertical kinematic eddy viscosity</td>
<td>m² s⁻¹</td>
</tr>
<tr>
<td>C_D</td>
<td>Coefficient of total drag for an individual animal</td>
<td></td>
</tr>
<tr>
<td>D</td>
<td>Total drag caused by a swimming animal</td>
<td>kg m s⁻²</td>
</tr>
<tr>
<td>e_d</td>
<td>Rate of energy utilization to overcome drag</td>
<td>kg m² s⁻³</td>
</tr>
<tr>
<td>e_t</td>
<td>Total rate of energy utilization by an individual animal (in W)</td>
<td>kg m² s⁻³</td>
</tr>
<tr>
<td>E_p</td>
<td>Total rate of animal energy production per unit mass of seawater</td>
<td>W kg⁻¹</td>
</tr>
<tr>
<td>ε</td>
<td>Rate of turbulent energy dissipation</td>
<td>W kg⁻¹</td>
</tr>
<tr>
<td>λ</td>
<td>Swimming velocity exponent of mass</td>
<td></td>
</tr>
<tr>
<td>η</td>
<td>Propulsive efficiency</td>
<td></td>
</tr>
<tr>
<td>L</td>
<td>Animal body length</td>
<td>m</td>
</tr>
<tr>
<td>M</td>
<td>Animal body wet mass of an individual animal</td>
<td>kg</td>
</tr>
<tr>
<td>N</td>
<td>Number of animals</td>
<td></td>
</tr>
<tr>
<td>N/V</td>
<td>Abundance of animals: number of animals per unit volume of seawater</td>
<td>m⁻³</td>
</tr>
<tr>
<td>v</td>
<td>Kinematic molecular viscosity of seawater</td>
<td>m² s⁻¹</td>
</tr>
<tr>
<td>Re</td>
<td>Reynolds number (µLV)</td>
<td></td>
</tr>
<tr>
<td>ρ</td>
<td>Density of seawater</td>
<td>kg m⁻³</td>
</tr>
<tr>
<td>S_w</td>
<td>Wetted surface area of an individual animal</td>
<td>m²</td>
</tr>
<tr>
<td>u_c</td>
<td>Cruising speed</td>
<td>m s⁻¹</td>
</tr>
<tr>
<td>u_e</td>
<td>Escape speed</td>
<td>m s⁻¹</td>
</tr>
<tr>
<td>V</td>
<td>Volume of seawater</td>
<td>m³</td>
</tr>
<tr>
<td>W</td>
<td>Animal body width</td>
<td>m</td>
</tr>
</tbody>
</table>
involves a succession of motion events, characterized by an initial period of acceleration as the swimming legs move propulsively, and followed by a coasting period as the legs resume their initial position (Morris et al. 1990). For copepods, therefore, we use average cruising speeds.

We define escape speed operationally, as the greatest recorded speed for a given species. Its sustainability increases with animal size. The cyclopoid copepod *Cyclops scutifer* can maintain an escape velocity of ~20 cm s⁻¹ for only a fraction of a second (Strickler 1975). The threespine stickleback *Gasterosteus aculeatus*, maintains its peak velocity of approximately 35 cm s⁻¹ for 1 min (Whoriskey & Wooton 1987). The gray whale *Eschrichtius robustus* has an escape velocity of 4.4 m s⁻¹ (Gilmore 1956), and can maintain a velocity of 3.6 m s⁻¹ for almost 4 h (Wolman 1985).

**Body mass and body length.** We used wet body weight to scale swimming speeds to body mass. This unit of mass is commonly reported for relatively large animals such as fishes, birds and mammals. For crustaceans, body mass is often reported only in terms of dry weight or total carbon; sometimes the only measure of size is body length. To convert these units to wet weight we used a conversion factor of 5 for dry weight and 12.5 for carbon (Omori & Ikeda 1984); to convert from body length we assumed a length:width ratio of 7:1 (Huntley et al. 1995), approximated shape as a cylinder and assumed a body density equivalent to water (1.0 g cm⁻³). Body weights of protozoans and bacteria were also estimated from body volume, assuming a density of 1.0 g cm⁻³. We followed conventional definitions of body length, employing, for example, prosome length for copepods and fork length for fishes.

**Animal aggregations.** We cite a variety of literature sources regarding the dimensions and behavior of swarms or schools. Dimensions include the average horizontal length scale, aggregation thickness, and the average depth interval occupied by the species; we also present data on maximum dimensions when these have been reported. The data on packing density, or number of individuals per unit volume of seawater, within aggregations is primarily based upon in situ photographic observations where possible, though some acoustic data is included when direct observations were not available.

**RESULTS AND DISCUSSION**

**Swimming speed in relation to body mass**

Over a range of 20 orders of magnitude in body mass, from the bacterium *Escherichia coli* (5.2 × 10⁻¹⁶ kg) to the blue whale *Balaenoptera musculus* (6.4 × 10⁴ kg), swimming speed is described by the power function (m s⁻¹):

\[ u_{c,e} = aM^\lambda \]

where \( u_c \) is the cruising speed (or \( u_e \) the escape speed) and \( M \) is the wet body mass (kg).

Reynolds number in relation to body mass and swimming velocity

Re characterizes the nature of fluid flow as a function of the length scale \( L \) the cruising or escape speed \( (u_{c,e}) \) and the kinematic molecular viscosity \( \nu \) from

\[ \text{Re} = \frac{u_{c,e}L}{\nu} \]

For seawater \( \nu \) has a value of ~1.4 × 10⁻⁶ m² s⁻¹ (Pond & Pickard 1989). At low Re, flow is dominated by viscous forces and is laminar; however, above a transition value of Re ~1000, inertial forces become important and flow becomes increasingly turbulent.

Re is a power function of body mass (Fig. 2), which for cruising speed is described by

\[ \text{Re}_c = 1.46 \times 10^5 M^{0.63} \]

(\( n = 140, r^2 = 0.95 \)), and for escape speed by...
Although the transition to turbulence at cruising speed applies to animals in the size range of small fishes and large crustaceans such as shrimps and crabs ($M \sim 10^{-3}$ kg), at escape speeds the transition occurs at a body mass 2 orders of magnitude smaller ($M \sim 10^{-5}$ kg), equivalent to that of very large copepods (e.g. *Pleuromamma xiphias*), euphausiids (e.g. *Euphausia pacifica*) and larval fish (e.g. *Clupea harengus*).

Regression of log-transformed cruising speed ($u_c$) against Re (Fig. 3) yielded

$$u_c = 2.5 \times 10^{-3} Re^{0.44} \quad (n = 140, r^2 = 0.99)$$

and, for escape speed ($u_e$),

$$u_e = 2.23 \times 10^{-2} Re^{0.35} \quad (n = 40, r^2 = 0.95).$$

In their analysis of optimal swimming speeds for relatively large animals, $>10^{-4}$ kg, Videler & Nolet (1990) found $u_c = 2.00 \times 10^{-3} Re^{0.47}$—almost identical to our finding for cruising speeds (Eq. 5). We find here that this relationship holds for organisms down to $10^{-16}$ kg (Fig. 3). Escape speeds, however, are much greater at a given Re (Eq. 6).

**Contribution of animals to turbulence in the sea**

We focus on the following key questions: (1) How much kinetic energy is produced by animals swimming in the ocean? (2) Is the magnitude of animal-induced turbulence significant by comparison to observed rates of turbulent energy dissipation? (3) What are the relevant time and space scales of animal-induced turbulence?

The mechanism by which turbulence is produced by animal swimming is different from that produced by shear. Swimming-induced turbulence is caused by velocity fluctuations arising from animal motion at relatively small scales rather than by the interaction between Reynolds stress and the shear of the mean flow. Nevertheless, the kinetic energy that is produced ultimately must be dissipated.

The rate of turbulent energy dissipation caused by animals arises from the rate at which they expend energy. Animals consume energy to overcome the drag force created by swimming. The rate of energy expenditure by an individual animal, $e_d$, is the product of its swimming speed and the work it does to overcome drag, i.e.

$$e_d = D u_c \quad (7)$$

where $D$ is the drag force. The total drag ($D$) is primarily caused by flow separation and loss of energy in the wake of the animal, as well as from skin friction. In general, skin friction reflects viscous forces and becomes significantly less important at high Re. The total drag (in N) is written as:

$$D = \frac{1}{2} \rho u^2 S_w C_D \quad (8)$$

where $\rho$ is the density of seawater, $S_w$ is the total wetted surface area, and $C_D$ is the drag coefficient. Here we approximate the wetted surface area as $S_w = W L$, where $W$ is body width and $L$ is body length. Surface area can be more accurately defined for animals that share a common shape (e.g. *Fish 1993*), but this general expression is reasonable for the variety of shapes considered here.

The theoretical drag coefficient, $C_D$, for turbulent flow is given as:

$$C_D = 0.072 Re^{-0.2} \quad (9)$$

(Hoerner 1965), which describes the drag on an ideal flat plane parallel to the flow where the boundary layer...
is turbulent. Animal body shapes are less than ideal in this respect, so Eq. (9) yields a conservative estimate of $C_D$, as can be seen by comparison to actual measurements or models that account for differences in shape (Table 2).

It is reasonable to assume that the body width: length ratio ($W/L$) is, in general, of the order of $10^{-1}$. Substituting $S_w = 2WL$ taking $C_D$ from Eq. (9), and multiplying both sides of Eq. (8) by $(L^2/\nu)$, we obtain (in N)

$$D = 7.2 \times 10^{-3} \rho u_c^2 L^2 Re^{-0.2} = 1.4 \times 10^{-14} \rho Re^{1.8} \quad (10)$$

The rate of energy utilization (in W) to overcome drag is equal to:

$$e_d = 1.4 \times 10^{-14} \rho Re^{1.8} u_c \quad (11)$$

Substituting for the cruising speed as a function of body mass from Eq. (1), and for Re as a function of body mass from Eq. (3) we have

$$e_d = 1.34 \times 10^{-5} \rho M^{1.39} \quad (12)$$

The rate of turbulent energy production by an animal is equal to its total rate of energy utilization for mechanical activity. However, animals are not 100% efficient in their use of energy for propulsion. Part of the energy is used to overcome drag implied by the animal’s observed swimming speed and results in a forward propulsive force. However, the animal needs to expend additional energy to overcome drag forces created by the swimming mechanism itself, and that additional energy is inefficient with respect to propulsion. For example, the accelerating power stroke of a copepod’s swimming leg creates forward thrust; however, in returning to its initial position, the leg decelerates, creating a negative drag force and decreasing the forward thrust (Morris et al. 1985). The force created by the decelerating stroke not only requires the animal to expend additional energy to overcome drag forces, but also introduces additional kinetic energy into the medium. The propulsive efficiency may be expressed as:

$$\eta = \frac{e_d}{e_i} \quad (13)$$

where $e_i$ is the total rate of energy utilization by an individual animal.

Measurements and estimates of $\eta$ vary widely for animals capable of operating at turbulent Re, and generally increase with body mass. Propulsive efficiency of the copepod *Pleuromamma xiphias* increases with swimming speed from 0.30 to 0.35 (Morris et al. 1985). The horse mackerel *Trachurus trachurus* has an efficiency of 0.40 at maximum sustainable swimming speed (Wardle et al. 1996). Fusiform fishes can attain a propulsion efficiency of 0.75 (Lighthill 1970), and some odontocete cetaceans are almost perfect, falling in the range of 0.82 to 0.90 (Fish 1998).

We now have a means of estimating the rate of kinetic energy production by an individual swimming animal, by combining Eqs. (12) & (13). However, to make a comparison with observed rates of turbulent energy dissipation, we need to take into account groups of animals, and we need to express their rates of energy production per unit mass of seawater. The total rate of energy production (W kg$^{-1}$) by a group of animals ($E_p$) is:

$$E_p = e_d \frac{1}{\eta} \frac{N}{V} \quad (14)$$

where $N/V$ is the numerical abundance of the group (numbers m$^{-3}$). Substituting Eq. (12), this simplifies to:

$$E_p = \frac{1.34 \times 10^{-5} M^{1.39}}{\eta} \frac{N}{V} \quad (15)$$

The rate of turbulent energy production by animals will be balanced only by its rate of dissipation ($\varepsilon$) such that:

$$E_p = -\varepsilon \quad (16)$$

Thus, we now have a basis for comparing animal-induced turbulence to observed rates of turbulent energy dissipation.

Table 2. Drag coefficient ($C_D$). Selected measurements (Actual) compared to the theoretical value (Estimate) for turbulent flow across a flat plate parallel to the flow (Hoerner 1965)

<table>
<thead>
<tr>
<th>Species</th>
<th>Mass (kg)</th>
<th>Length (m)</th>
<th>Re</th>
<th>$C_D$ Actual</th>
<th>$C_D$ Estimate</th>
<th>Actual/Estimate</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td><em>Pleuromamma xiphias</em></td>
<td>0.00001</td>
<td>0.006</td>
<td>$3.77 \times 10^3$</td>
<td>0.0220</td>
<td>0.7400</td>
<td>33.7</td>
<td>Morris et al. (1985)</td>
</tr>
<tr>
<td><em>Salmo gairdneri</em></td>
<td>0.25</td>
<td>0.3</td>
<td>$3.00 \times 10^3$</td>
<td>0.0056</td>
<td>0.0150</td>
<td>2.6</td>
<td>Webb (1975)</td>
</tr>
<tr>
<td><em>Pygoscelis adeliae</em></td>
<td>4.0</td>
<td>0.7</td>
<td>$1.10 \times 10^4$</td>
<td>0.0045</td>
<td>0.0360</td>
<td>8.3</td>
<td>Culik et al. (1994)</td>
</tr>
<tr>
<td><em>Eumetopias jubatus</em></td>
<td>141</td>
<td>2.32</td>
<td>$5.50 \times 10^6$</td>
<td>0.0032</td>
<td>0.0046</td>
<td>1.4</td>
<td>Stelle et al. (2000)</td>
</tr>
<tr>
<td><em>Tursiops truncatus</em></td>
<td>225</td>
<td>2.61</td>
<td>$1.30 \times 10^7$</td>
<td>0.0027</td>
<td>0.0076</td>
<td>2.8</td>
<td>Fish (1998)</td>
</tr>
<tr>
<td><em>Pseudorca crassidens</em></td>
<td>487</td>
<td>3.75</td>
<td>$1.80 \times 10^7$</td>
<td>0.0026</td>
<td>0.0046</td>
<td>1.8</td>
<td>Fish (1998)</td>
</tr>
<tr>
<td><em>Delphinapterus leucas</em></td>
<td>671</td>
<td>3.64</td>
<td>$1.20 \times 10^7$</td>
<td>0.0028</td>
<td>0.0130</td>
<td>4.7</td>
<td>Fish (1998)</td>
</tr>
<tr>
<td><em>Orcinus orca</em></td>
<td>1601</td>
<td>4.74</td>
<td>$3.65 \times 10^7$</td>
<td>0.0022</td>
<td>0.0026</td>
<td>1.2</td>
<td>Fish (1998)</td>
</tr>
</tbody>
</table>
It is well known that vision plays a dominant role in the schooling behavior of animals with compound and camera eyes (Hunter & Coyne 1982, Azuma & Iwata 1994, Wiese 1996, Buskey 2000). More importantly, evolved vision enables animals that operate at high Re to maintain highly contagious distributions.

Animal abundance in schools

Schooling behavior occurs in approximately 80% of all fishes (Burgess & Shaw 1979), many species of aquatic mammals (Ridgway & Harrison 1985, 1996), and is common among larger crustaceans (Mauchline 1980, Dall et al. 1990). To understand the potential impact of schooling animals on turbulent mixing in the ocean, we must consider quantitatively both the animals’ abundance within aggregations and the volumes occupied by such aggregations.

The most accurate observations of localized abundance within schools (Table 3) have been gained either by the analysis of photographs (Serebrov 1976, Graves 1977, Hamner 1984, Lutcavage et al. 2000, Hanrahan & Juanes 2001) or targeted sampling of acoustic features (Misund 1993, Lee & Lee 1996, Misund & Coetzee 2000). We emphasize that abundances shown in Table 3 are averages reported by the authors, and that greater abundances do occur. The abundance of Antarctic krill is the maximum reported by Hamner (1984); greater abundances of $5 \times 10^4$ to $6 \times 10^4$ m$^{-3}$ (Ragulin 1969), and greater biomass, up to 15 kg m$^{-3}$ (Nemoto 1962), have been observed, but provided no means to estimate the size of animals involved. The northern anchovy Engraulis mordax has been observed at packing densities as high as 533 m$^{-3}$ (Hewitt 1975), and, although Graves (1977) observed a maximum of 366 m$^{-3}$, we use his mean of 115 m$^{-3}$.

Schools tend to be comprised of animals of similar size (Fréon & Misund 1999). Packing density is inversely proportional to the cube of the minimum nearest neighbor distance (Serebrov 1976), and therefore we expect maximum packing densities (no. m$^{-3}$) to be inversely related to the average mass of the animals in the school. Indeed, we find:

$$\frac{N}{V} = 0.64 M^{-1.2}$$ (17)

(n = 16, $r^2 = 0.99$) (Fig. 5) where $N/V$ is the maximum reported packing density in a school of animals of mass $M$.

Serebrov (1976) compiled photographic data on packing densities of fishes ranging in mass from approximately 0.3 to 5 kg and found that abundance could be described by the relation $N/V = (2.44D)^{-3}$. The data we have compiled (Fig. 5) extends over a much
broad range of animal size—9 orders of magnitude—yet the resulting Eq. (17) accurately describes Serebrov’s (1976) data. Misund (1993, his Fig. 3) showed that Serebrov’s equation reasonably well described the upper bound of packing densities he measured acoustically for 532 schools of herring (Clupea harengus), saithe (Pollachius virens) and sprat (Sprattus sprattus). By contrast, the length-to-packing density relationship proposed by Pitcher & Partridge (1979) overestimated Misund’s observations by approximately 1 order of magnitude; their relationship was based on observations of very small captive schools and may describe an upper limit to packing density not commonly observed in free-ranging animals.

Apart from the photographic observations included in Table 3, estimates of packing densities of krill and fishes are based upon either acoustic measurements or net catches. Both of these methods inherently give rise to underestimates. As Misund (1993, p. 153) points out, ‘most sources of error in connection with the acoustic method will contribute to underestimate the fish density in schools.’ In particular, he cites vessel avoidance reactions and the extinction of sound energy within schools as key factors that lead to underestimates of packing density. Most published reports of biomass based on acoustic measurements are likely to be underestimates. Data from catches in nets and trawls

<table>
<thead>
<tr>
<th>Species</th>
<th>Mass (kg)</th>
<th>Abundance (no. m⁻³)</th>
<th>Biomass (kg m⁻³)</th>
<th>School vol (m³)</th>
<th>Thickness (m)</th>
<th>n</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td><em>Dioithona oculata</em></td>
<td>2.2 × 10⁻⁷</td>
<td>3.5 × 10⁷</td>
<td>7.70</td>
<td>22</td>
<td></td>
<td></td>
<td>Buskey et al. (1996)</td>
</tr>
<tr>
<td><em>Nyciphantes australis</em></td>
<td>1.4 × 10⁻⁵</td>
<td>430 000</td>
<td>6.02</td>
<td>15</td>
<td>1.0</td>
<td>1</td>
<td>O’Brien (1988)</td>
</tr>
<tr>
<td><em>Euphausia superba</em></td>
<td>0.0002</td>
<td>30 000</td>
<td>6.0</td>
<td>4000</td>
<td>4</td>
<td>&gt;8</td>
<td>Hamner (1984)</td>
</tr>
<tr>
<td><em>Engraulis japonicus</em></td>
<td>0.002</td>
<td>1294</td>
<td>2.59</td>
<td>4600</td>
<td>3.3⁴</td>
<td>39</td>
<td>Lee &amp; Lee (1996)</td>
</tr>
<tr>
<td><em>Engraulis mordax</em></td>
<td>0.010</td>
<td>115</td>
<td>1.15</td>
<td>10</td>
<td></td>
<td></td>
<td>Graves (1977)</td>
</tr>
<tr>
<td><em>Engraulis encrasicolus</em></td>
<td>0.027</td>
<td>33.0</td>
<td>0.88</td>
<td>15</td>
<td></td>
<td></td>
<td>Radakov (1973)</td>
</tr>
<tr>
<td><em>Sardinops sagax</em></td>
<td>0.033</td>
<td>29.5</td>
<td>0.97</td>
<td>5²</td>
<td>1131</td>
<td></td>
<td>Misund &amp; Coetzee (2000)</td>
</tr>
<tr>
<td><em>Mallophus villosus</em></td>
<td>0.049</td>
<td>15.7</td>
<td>0.78</td>
<td>7</td>
<td></td>
<td></td>
<td>Zaferman (1973)</td>
</tr>
<tr>
<td><em>Boreogadus saida</em></td>
<td>0.097</td>
<td>13.6</td>
<td>1.32</td>
<td>47</td>
<td></td>
<td></td>
<td>Serebrov (1976)</td>
</tr>
<tr>
<td><em>Gadus morhua</em></td>
<td>0.30</td>
<td>4.7</td>
<td>1.40</td>
<td>47</td>
<td></td>
<td></td>
<td>Serebrov (1976)</td>
</tr>
<tr>
<td><em>Clupea harengus</em></td>
<td>0.30</td>
<td>4.7</td>
<td>1.40</td>
<td>47</td>
<td></td>
<td></td>
<td>Misund (1993)</td>
</tr>
<tr>
<td></td>
<td>0.38⁵</td>
<td>3.2</td>
<td>3.20</td>
<td>7</td>
<td></td>
<td></td>
<td>Lyamin (1966)</td>
</tr>
<tr>
<td><em>Pollachius virens</em></td>
<td>2.30</td>
<td>0.25</td>
<td>0.57</td>
<td>7</td>
<td></td>
<td></td>
<td>Misund (1993)</td>
</tr>
<tr>
<td><em>Macrurus rupestris</em></td>
<td>4.90⁴</td>
<td>0.13</td>
<td>0.64</td>
<td>7</td>
<td></td>
<td></td>
<td>Serebrov (1976)</td>
</tr>
<tr>
<td><em>Thunnus thynnus</em></td>
<td>12</td>
<td>0.023</td>
<td>0.24</td>
<td>8600⁵</td>
<td>5¹</td>
<td>74</td>
<td>Hanrahan &amp; Juanes (2001)</td>
</tr>
<tr>
<td></td>
<td>135</td>
<td>0.001¹</td>
<td>0.14</td>
<td>165 000⁶</td>
<td></td>
<td></td>
<td>Lutcavage et al. (2000)</td>
</tr>
</tbody>
</table>

⁻¹Hamner (1984) does not provide length or mass measurements of the krill, however his observation of sustained swimming speeds of 20 cm s⁻¹ are equivalent to those measured for krill of approximately 33 mm (Kils 1979) with a wet weight of ~200 mg (Zhou et al. 1994)

⁻²School thickness reported for *Engraulis japonicus* was 3.3 m in daytime and 16.3 m at night (Ohshimo 1996)

⁻³Mass (kg) estimated from length (m) in our data set in Appendix 1, i.e. $M = 10.6L^{2.8}$

⁻⁴The echo sounder depth interval in which schools were recorded

⁻⁵Volume based on a typical school size of 200 individuals (Lutcavage et al. 2000), and thickness of the school estimated based on experimental data obtained by Hanrahan & Juanes (2001)

⁻⁶Thickness of the tuna school was estimated indirectly from information provided

⁻⁷Abundance was estimated from the experimental data of Hanrahan & Juanes (2001)

⁻⁸Of the 5 tuna in this weight range (113 to 159 kg), 4 were in schools of approximately 200 individuals each (Lutcavage et al. 2000)

Fig. 5. Abundance or packing density (no. m⁻³) in schooling animals as a function of body mass (kg) for species ranging from copepods to Atlantic bluefin tuna. Data, also provided in Table 3, include those previously reported by Serebrov (1976) (¹)
are also likely to yield significant underestimates, as avoidance behavior to these devices is well known (Fréon & Misund 1999).

We make 3 important assumptions regarding the packing density of schooling animals. First, we assume that direct observations of free-swimming schools provide the best estimates of packing density, and therefore that Eq. (17) is accurate, at least to within 1 order of magnitude. Second, we assume that acoustic data reasonably well describe the spatial dimensions of schools of krill and small fishes. Third, we assume the packing density of large fishes and aquatic mammals can be reasonably estimated from an extrapolation of Eq. (17). The number of animals in groups of bluefin tuna, sharks or baleen whales is usually reported. To estimate their packing density we assume that the nearest-neighbor distance relationship implied by Eq. (17) holds true.

**Magnitude and length scale of turbulent energy production by animal schools**

To assess whether or not animal-induced turbulence is significant in the ocean, we must know not only its magnitude, but also its characteristic spatial and temporal scales.

The kinetic energy production rate for schooling animals of mass $M$ depends not only on their local abundance, but also on their propulsive efficiency (Eq. 13), which can vary significantly among species (Table 4). The crustacean *Euphausia pacifica* exhibits a maximal propulsive efficiency of $\eta = 0.11$ (Torres 1984) if one takes into account a muscle efficiency of 0.25 (Hill 1950). For fishes we estimate propulsive efficiency from:

$$\eta = 0.39 u^2 0.24$$

(Weihs 1977, Wardle et al. 1996), which yields a value of approximately 0.3 for sardines and anchovies and 0.4 for Atlantic bluefin tuna. Odontocete cetaceans attain observed efficiencies in the range of 0.8 to 0.9 (Fish 1998).

We can now calculate the rate of energy production by schools of known packing density from Eq. (15), and by using values of $\eta$ from either direct observation or estimated from Eq. (18). Table 4 shows this result for 11 species of animals, ranging over 8 orders of magnitude in body mass. Interestingly, the estimated rates of kinetic energy production from animal schools are all of the same order, regardless of animal size (Table 4), resulting in $\varepsilon = 10^{-5}$ W kg$^{-1}$.

Scales of animal-induced turbulence will be consistent with the typical length scales of schooling aggregations. A review of thousands of observations on schools of 9 species shows that typical horizontal scales are of the order of $10^1$ to $10^3$ m; the thickness or vertical scale of schools is typically from 5 to 50 m (Table 5).

**Observed rates of turbulent energy dissipation in the ocean**

The rate of turbulent energy dissipation ($\varepsilon$) in the upper mixed layer of the ocean is generally in the range of $10^{-7}$ to $10^{-5}$ W kg$^{-1}$. Within the pycnocline,

<table>
<thead>
<tr>
<th>Species</th>
<th>Mass (kg)</th>
<th>Abundance (no. m$^{-3}$)</th>
<th>Speed (m s$^{-1}$)</th>
<th>$\eta$</th>
<th>$E_p$ (W kg$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td><em>Euphausia superba</em></td>
<td>0.0002</td>
<td>30000</td>
<td>0.05</td>
<td>0.11a</td>
<td>2.64 $\times$ 10$^{-5}$</td>
</tr>
<tr>
<td><em>Engraulis japonicus</em></td>
<td>0.002</td>
<td>1294</td>
<td>0.09</td>
<td>0.22</td>
<td>1.41 $\times$ 10$^{-5}$</td>
</tr>
<tr>
<td><em>Engraulis mordax</em></td>
<td>0.010</td>
<td>115</td>
<td>0.14</td>
<td>0.24</td>
<td>1.06 $\times$ 10$^{-5}$</td>
</tr>
<tr>
<td><em>Sardina sagax</em></td>
<td>0.033</td>
<td>29.4</td>
<td>0.19</td>
<td>0.26</td>
<td>1.31 $\times$ 10$^{-5}$</td>
</tr>
<tr>
<td><em>Clupea harengus</em></td>
<td>0.30</td>
<td>4.7</td>
<td>0.35</td>
<td>0.30</td>
<td>3.90 $\times$ 10$^{-5}$</td>
</tr>
<tr>
<td><em>Pollachiurus virens</em></td>
<td>2.30</td>
<td>0.25</td>
<td>1.05</td>
<td>0.39</td>
<td>2.70 $\times$ 10$^{-5}$</td>
</tr>
<tr>
<td><em>Thunnus albacares</em></td>
<td>77</td>
<td>0.0035</td>
<td>1.59</td>
<td>0.44</td>
<td>4.49 $\times$ 10$^{-5}$</td>
</tr>
<tr>
<td><em>Tursiops truncatus</em></td>
<td>215</td>
<td>0.0010</td>
<td>3.35</td>
<td>0.85c</td>
<td>2.80 $\times$ 10$^{-5}$</td>
</tr>
<tr>
<td><em>Thunnus thynnus</em></td>
<td>318</td>
<td>6.5 $\times$ 10$^{-4}$</td>
<td>1.30</td>
<td>0.48</td>
<td>5.36 $\times$ 10$^{-5}$</td>
</tr>
<tr>
<td><em>Orcinus orca</em></td>
<td>1645</td>
<td>8.9 $\times$ 10$^{-3}$</td>
<td>3.95</td>
<td>0.87c</td>
<td>4.03 $\times$ 10$^{-5}$</td>
</tr>
<tr>
<td><em>Physeter macrocephalus</em></td>
<td>19850</td>
<td>4.5 $\times$ 10$^{-6}$</td>
<td>2.08</td>
<td>0.83a</td>
<td>6.77 $\times$ 10$^{-5}$</td>
</tr>
</tbody>
</table>

aTorres (1984)
bAverage swimming speed of free-swimming saithe schools (Pedersen 2001)

cDirect measurements of cruising speed and propulsive efficiency (Fish 1998)
dRice (1989)
eApproximated from measurements on the white whale *Delphinapterus leucas* (Fish 1998)
where turbulence is suppressed by the strong vertical density gradient, $\epsilon$ decreases to about $10^{-10}$ to $10^{-6}$ (Table 6). The variability of dissipation rate within these layers is very high, but boundary values are quite robust. On a seasonal scale, the surface mixed layer shallows in summer to about 5 to 20 m and deepens in winter to approximately 50 to 70 m as seasonally averaged wind stress increases significantly.

Turbulent energy dissipation rates are notoriously patchy. Daily or hourly variations of $\epsilon$ in the upper mixed layer are well documented, with broad-scale variability of approximately 2 orders of magnitude attributed to nocturnal convection (Brainerd & Gregg 1995) or wind

Table 6. Representative values of turbulent energy dissipation rate ($\epsilon$ [W kg$^{-1}$]) in oceanic regions in the upper mixed layer ($\epsilon_m$) and within the region of maximum stratification ($\epsilon_s$). The mixed layer depth ($Z_m$) is the approximate depth below the surface (m) to the top of the thermocline or pycnocline

<table>
<thead>
<tr>
<th>Region</th>
<th>Season</th>
<th>$Z_m$ (m)</th>
<th>Mixed log $\epsilon_m$ (W kg$^{-1}$)</th>
<th>Stratified log $\epsilon_s$ (W kg$^{-1}$)</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Coastal/Shelf</td>
<td>Georges Bank</td>
<td>Apr–May</td>
<td>10–20</td>
<td>$-7$ to $-6$</td>
<td>Lough &amp; Mountain (1996)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Jul–Aug</td>
<td>5–15</td>
<td>$-7$ to $-6$</td>
<td>Horne et al. (1996)</td>
</tr>
<tr>
<td></td>
<td>California</td>
<td>Oct</td>
<td>40–50</td>
<td>$-8$ to $-5$</td>
<td>Brainerd &amp; Gregg (1995)</td>
</tr>
<tr>
<td></td>
<td>North Sea</td>
<td>Oct</td>
<td>40–50</td>
<td>$-7$ to $-5$</td>
<td>Visser et al. (2001)</td>
</tr>
<tr>
<td></td>
<td>Black Sea</td>
<td>Oct</td>
<td>20</td>
<td>$-9$ to $-8$</td>
<td>Lozovatsky et al. (1999)</td>
</tr>
<tr>
<td>Open ocean</td>
<td>Equatorial</td>
<td>Feb–Mar</td>
<td>60–70</td>
<td>$-7$ to $-5$</td>
<td>Brainerd &amp; Gregg (1995)</td>
</tr>
<tr>
<td></td>
<td>Pacific</td>
<td>Nov–Dec</td>
<td>20–30</td>
<td>$-7$ to $-5$</td>
<td>Menthis et al. (1983)</td>
</tr>
<tr>
<td></td>
<td>Nov</td>
<td>50</td>
<td></td>
<td></td>
<td>Mikhalev et al. (1981), Dahlheim et al. (1982)</td>
</tr>
</tbody>
</table>
forcing (Visser et al. 2001). On a vertical scale of the order of 1 m, ε may vary by 2 orders of magnitude (Brainerd & Gregg 1995). Similar variations have been observed on horizontal scales of the order of $10^2$ m (Horne et al. 1996). Repeated microstructure profiles typically show little coherence in small-scale variability.

The observed scales of variability in turbulent energy dissipation rates—order of 1 m in the vertical, $10^3$ m in the horizontal, and hours in time—are consistent with the scales of animal-induced turbulence. Small scales of variability may be attributed to a wide variety of factors, such as wind events, rainfall, nocturnal convection, or even to natural variability (Moum et al. 1995, p. 353). We suggest that animal schools could reasonably account for some of that natural variability.

### Animal-induced turbulence

**Atlantic bluefin tuna**

*Thunnus thynnus* ranges throughout the North Atlantic Ocean, breeding in the Gulf of Mexico and in the Mediterranean. It moves northward to rich feeding grounds during summer and fall, and is capable of making rapid transatlantic crossings (Block et al. 2001). Adults can attain a mass >650 kg and a length of >3 m (Magnuson et al. 1994).

Bluefin schools typically arrive in coastal and continental shelf waters of the northwest Atlantic Ocean during summer, when the seasonal thermocline has been well established and stratification is at an annual maximum. Average group size is approximately 100 animals, and schools of >1000 are not uncommon (Lutcavage & Kraus 1995). Schools of more than 40 to 50 tend to be organized in up to 5 layers, thus covering a depth range of approximately 10 m (Hanrahan & Juanes 2001). At observed packing densities, 300 kg animals in a school of average size will occupy $1.2 \times 10^4$ m$^2$; the largest observed schools of >5000 (Lutcavage et al. 2000) will cover more than $5.0 \times 10^3$ m$^2$.

Free-ranging bluefin in the Gulf of Maine in summer typically consist of animals in the 100 to 300 kg size-class. Extensive telemetry data show that these animals have sustained swimming speeds $>2.5$ m s$^{-1}$, can maintain speeds of up to 3.6 m s$^{-1}$ for about 45 min, and may swim at $>7$ m s$^{-1}$ for brief periods (Lutcavage et al. 2000). During feeding bouts, which involve relatively large schools, tuna behavior appears violent, being described as ‘pushing, milling and smashing’ (Mather 1962). Like many tuna species, bluefin commonly feed in convergence zones or frontal regions where density gradients are high (Olson et al. 1994). More than 70% of the time being divided about equally between the upper 3 to 4 m and occasional dives to a limit of the 8 to 9$^\circ$ isotherm (Lutcavage et al. 2000, Brill et al. 2002).

As a source of turbulent energy in the ocean, we can characterize bluefin tuna as follows. During the several-month period of maximum seasonal stratification in shelf and coastal waters off North America, the average bluefin tuna school cruises continuously, generating $5 \times 10^{-5}$ W kg$^{-1}$ on a length scale of the order of 100 m (Table 4). Turbulent energy is created precisely where density gradients are greatest—with the seasonal thermocline and in frontal zones—where typical energy dissipation rates are $10^1$ to $10^3$ times lower (Table 6). The resultant coefficient of vertical eddy viscosity, $A_v$, is of the order of $10^{-1}$ m$^2$s$^{-1}$. A school of average size will impact about 20 km$^2$ daily; large schools will affect an area well in excess of 100 km$^2$.

**Herring**

*Clupea harengus*, the North Atlantic herring, provides the basis for one of the world’s most productive fisheries, with key areas of concentration distributed across coastal waters of the temperate North Atlantic from the Gulf of Maine to Georges Bank to the North Sea (FAO 1997). Similar species form important fisheries in the North Pacific (*Clupea pallasi*) and off the coast of Chile (*Strongomera bentincki*).

The Norwegian herring stock was heavily fished after World War II, and during the 1960s plummeted to about 1% of its post-war stock size. By the mid-1990s the population had reached its high historic levels of about 10 million t or $5 \times 10^9$ individuals, and is now distributed over large areas of the Norwegian Sea (Fréon & Misund 1999). The entire spring-spawning population makes an extended feeding migration to the central Norwegian Sea in summer, then returns primarily to a single coastal fjord (e.g. Tysfjord in 1983, Vestfjord in 1991 year class) in September where it overwinters until the following spring spawning season (Huse et al. 2002).

As herring enter the fjord region in September, animals are typically organized in schools 10 to 20 m thick centered at a depth ranging from 10 m to 40 m (Misund et al. 1992, Misund 1993). The average school covers an area of approximately $1 \times 10^3$ m$^2$; the largest of 407 schools observed by Misund et al. (1992) reaching $1.0 \times 10^4$ m$^2$. Average abundance in schools of 25 to 30 cm herring is 2 to 5 animals m$^{-3}$, but small-scale patches within schools may be 10 times greater. Free-ranging schools tend to have approximately the same swimming speed whether they are migrating, spawning, feeding or searching (Nøttestad et al. 1996). Like other clupeoids, schools tend to disperse at night and become more compact during the day (Pitcher 1986).
Clupea harengus schools may have significant impact on regional-scale ocean turbulence. At typical observed abundances and cruising speeds, herring schools provide energy input of approximately $4 \times 10^{-5}$ W kg$^{-1}$ (Table 4). In summer in the Norwegian Sea, as the ocean reaches its peak seasonal stratification, the Norwegian spring spawning population covers a total area of the order of $10^3$ km$^2$, cruising in a 10 to 20 m thick layer through the region of maximal density gradients where dissipation rates are typically orders of magnitude lower. The entire population then migrates to highly stratified fjords along the central Norwegian coastline, concentrating its turbulent energy production over a much smaller area than during summer.

**Anchovy**

Often ranking as the world’s number one fishery (FAO 1997), anchovy of different species inhabit temperate coastal regions off southern Europe and the Mediterranean, South Africa, Chile, Peru, Japan and California. Schools of Engraulis mordax, the northern anchovy, were studied extensively in the 1970s when the California fishery was still reasonably active. In a survey of approximately 23,000 schools, more than 80% were in the range of 10 to 30 m in diameter, with the largest ranging up to almost 400 m (Mais 1974). A school group as large as 10 km in diameter has been reported (Smith 1970). Subsequent acoustic surveys showed that E. mordax schools are typically 4 m thick, and centered almost exactly at the depth of the maximal thermal gradient regardless of season (Holliday & Larsen 1979). Similar schooling characteristics have been observed for Engraulis japonicus (Lee & Lee 1996, Ohshimo 1996) and Engraulis encrasicolus (Massé et al. 1996).

The central California stock of Engraulis mordax is concentrated primarily in the Southern California Bight, where it spawns year-round, with a peak from February to April and a minimum from August to October (Lasker & Smith 1977). The spawning population, comprising individuals of mass $M \geq 1.0 \times 10^{12}$ kg, reached an estimated peak of almost $5 \times 10^{12}$ kg in the mid-1960s (Vrooman & Smith 1972). Assuming a packing density of 115 fish m$^{-3}$ (Graves 1977) and the observed school thickness of 4 m (Holliday & Larsen 1979), the central California spawning population would have occupied an area of the order of $10^4$ km$^2$. By analogy, the spawning population of Peruvian anchoveta Engraulis ringens which reached an estimated peak of $2 \times 10^{13}$ kg (Csirke 1980), would have occupied an area of approximately $4.0 \times 10^4$ km$^2$ of coastal South American waters before the fishery’s collapse in the late 1970s.

Anchovy again generates of the order of $10^{-5}$ W kg$^{-1}$ (Table 4), and is vertically situated on the maximum thermal gradient where rates of turbulent energy dissipation are commonly $10^{-9}$ to $10^{-7}$ W kg$^{-1}$ (Brainerd & Gregg 1995). Historically large populations would have occupied large areas within their coastal ocean habitat.

**Krill**

The Antarctic krill Euphausia superba has a circum-continental distribution but is most abundant in coastal shelf regions of the Antarctic Peninsula (Marr 1962, Guzmán 1983). The reported average horizontal length scale of swarms ranges from 17 m ($n = 1576$) in the Indian Ocean sector, 34 m ($n = 166$) in the Prydz Bay region (Miller & Hampton 1989), 94 m ($n = 5624$) in the West Atlantic sector (BIOMASS 1986); to 307 m ($n = 38$) around Elephant Island, near the Antarctic Peninsula (Ricketts et al. 1992). Average thickness of these aggregations likewise varies from 6 to 15 m in the Indian Ocean, Prydz Bay and West Atlantic areas (Miller & Hampton 1989) to more than 50 m, particularly where larger swarms have been observed (Ricketts et al. 1992, Zhou et al. 1994). Aggregations with a horizontal length scale of $>10^3$ m are not uncommon (Kalinowski 1983, Zhou et al. 1994); and the largest ever reported was a superswarm of the order of $2.0 \times 10^3$ m, or 450 km$^2$, with greatest abundances generally distributed in a layer of 40 to 50 m (Macaulay et al. 1984).

Euphausia superba performs diel vertical migration and, like many species of euphausiids, tends to be diffusely distributed within 10 to 20 m of the surface at night, and concentrated around 35 to 50 m depth during daytime (Demer & Hewitt 1995, Watkins & Murray 2000). However, significant seasonal changes in day-length at high latitudes render these vertical distributions rather invariant during summer and winter. The mean depth of summer krill aggregations ($n = 4830$) in the West Atlantic sector is 36 m (Miller et al. 1993). Daytime depth distributions in summer tend to coincide with regions of the maximal temperature gradient, which in the Scotia Sea and waters of the coastal Antarctic Peninsula is centered between 30 to 50 m (Foster & Middleton 1984, Niiler et al. 1991).

The abundance of krill in schools or swarms is a somewhat contentious issue. Photographic and visual observations place abundances in the order of $5.0 \times 10^4$ m$^{-3}$ (Ragulin 1969, Hamner 1984), which is consistent with previous estimates compiled by Mauchline (1980), and less than implied by biomass estimates of up to 15 kg m$^{-3}$ (Nemoto 1962). Acoustic estimates have generally failed to validate these abundances...
(Watkins & Murray 2000). However, a correction for target strength recommended by Everson et al. (1990) would increase historical estimates by up to one order of magnitude, and place previous high averages for the West Atlantic sector at a level of approximately 5 kg m$^{-3}$ (Macaulay et al. 1984, BIOMASS 1986). Analysis of 1766 aggregations in the Indian Ocean and Prydz Bay regions revealed that inter-aggregation distance followed a Poisson distribution, with a mean of 2.1 km (Miller & Hampton 1989). This pattern agrees with observations in the West Atlantic sector, although aggregations there tend to be significantly larger (Kalinowski 1983).

Coastal waters of the Antarctic Peninsula are a principal locus of krill abundance and an important source of recruitment to the population of the Scotia Sea region (Marr 1962, Hunley & Brinton 1991). To a distance of more than 200 km offshore, the summer thermocline shoals to near 20 m depth (Mitchell & Holm-Hansen 1991, Niiler et al. 1991). The average krill aggregation, covering an area in the range of 10$^4$ to 10$^5$ m$^2$, would be expected to generate turbulent energy of the order of 2 $\times$ 10$^{-5}$ W kg$^{-1}$ (Table 4) over a depth interval of approximately 50 m that encompasses the seasonal thermocline. At the average inter-aggregation distance of 2.1 km, the contribution to turbulent mixing could be significant.

The impact of summer krill aggregations on ecosystem dynamics at horizontal length scales of 10$^3$ to 10$^5$ m could be especially important in critical recruitment areas near the Antarctic Peninsula. Here the first spring bloom significantly reduces the concentration of macronutrients in the upper mixed layer (Holm-Hansen & Mitchell 1991, Dore et al. 1992). However, productivity can remain very high with frequent bloom formation over several months following the initial bloom and nutrient depletion (Karl et al. 1992, Holm-Hansen et al. 1993). Constant erosion of the nitracline at scales of krill-induced mixing would provide a supply of nutrients that could be important to the observed rates of continued high primary productivity. Even at average abundance of 0.1 to 1 kg m$^{-3}$, the rate of kinetic energy production by krill aggregations would still be of the order of 10$^{-6}$ W kg$^{-1}$. This is substantially greater than expected rates of turbulent energy dissipation within the thermocline (Table 6).

### CONCLUSIONS

Animals can be an important source of turbulent energy in the ocean at typical scales of social aggregation. The rate of turbulent energy production by schooling animals, from krill to whales, is 10$^{-5}$ to 10$^{-4}$ W kg$^{-1}$, regardless of species. By comparison, the rate of turbulent energy dissipation in the upper 10 m resulting from a wind of 5 m s$^{-1}$ is 1.7 $\times$ 10$^{-7}$ W kg$^{-1}$, and from a wind of 20 m s$^{-1}$, 8.5 $\times$ 10$^{-6}$ W kg$^{-1}$ (MacKenzie & Leggett 1993). Horizontal length scales of wind-induced turbulence are substantially greater than typical animal assemblages, which are generally 10$^3$ to 10$^4$ m. However, the horizontal length scales of animal schools are consistent with commonly observed fine-scale variability in $\varepsilon$ (e.g. Brainerd & Gregg 1995). Many animal species prefer to swim and feed within the zone of maximum vertical stratification, where their rate of turbulent energy production is several orders of magnitude greater than average dissipation rates.

Bluefin tuna schools may not challenge storms in the Gulf of Maine as a regional-scale source of turbulent energy, but they are not the only schooling animals in the region, just as herring are not the only fish in Norwegian fjords, nor are anchovy the only animals in the Southern California Bight. The cumulative impact of all schooling animals in any region is far beyond our ability to estimate. The data simply do not exist.

We do not suggest that animal aggregations are more important than purely physical forces as a source of turbulent energy production. However—particularly in coastal regions, where schooling animals are most abundant, and especially in summer when seasonal stratification is greatest—the mixing energy introduced by swimming animals may have a significant effect not only on local physics, but also on the chemistry and biology of the ocean.

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