Modelling vegetative growth, gamete production and encystment of dinoflagellates in batch culture

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ABSTRACT: An intriguing case of encystment of the dinoflagellate *Scrippsiella lachrymosa* in culture has recently been presented: cyst concentrations still increased after the abundance of the vegetative cells had decreased to very low numbers. To account for this apparent time lag, and using a model with an encystment rate equation in which vegetative growth and encystment rates were coupled, the calculated growth and encystment rates had to be 8 to 12 d⁻¹, values which were considered 'not biologically meaningful'. Here a new model of dinoflagellate growth and encystment is presented in which the mitotic cycle (vegetative growth) is coupled quantitatively to the sexual cycle (cyst formation) by having 4 gametes emanate from 1 vegetative cell, but without directly coupling the rates of vegetative growth and encystment. Calibrated on literature data of *S. lachrymosa* cultured in f/4 medium, this model satisfactorily describes motile cell (vegetative cells and gametes) and cyst development with correlations between log-transformed model and experimental data of $r^2 = 0.80$ (motile cells) and $r^2 = 0.94$ (cysts) and with typical maximum rates in the exponential growth phase of $\mu_{cell} = 0.55$ d⁻¹ (gross vegetative cell rate), $\mu_{gamete+cell} = 0.38$ d⁻¹ (net motile cell growth rate), $\varepsilon = 0.42$ d⁻¹ (encystment rate). All these rates declined in the stationary growth phase. Sample sonication is suggested as the cause for low motile cell concentrations in the original experiment when cyst production was high. Inorganic carbon limitation due to low inorganic carbon to nitrogen concentrations in the growth media is probably the reason why cysts in f/4 medium stopped making calcite covers in later stages of the experiment and why cyst yield in f/2 medium was not double the yield in f/4. A new method for measuring *in situ* encystment rates of dinoflagellate populations with a phased sexual cycle is proposed.

KEY WORDS: Dinoflagellate · Vegetative growth · Sexual cycle · Gametes · Cysts · Model

INTRODUCTION

The complex life cycle of many non-parasitic, autotrophic dinoflagellates contains haploid vegetative cells in the water column and diploid benthic resting stages called cysts or hypnozygotes (Fig. 1) (Dale 1983, Coats et al. 1984, Pfiester & Anderson 1987, Pollingher 1988, Blackburn et al. 1989, Gao et al. 1989, Tomas et al. 1989, Giacobbe & Yang 1999, Elbrächter 2003). Haploid vegetative dinoflagellate growth by binary fission is regulated in the mitotic cycle, which consists of 4 phases: Gap 1, Synthesis of DNA and Gap 2 + Mitosis (G1, S, G2M). Mitosis yields 2 haploid vegetative cells (Fig. 1). If the population is growing in phase, the growth rate can be modelled using the length of the S- and or G2M-phases as so-called terminal events (McDuff & Chisholm 1982, Carpenter & Chang 1988). The sexual cycle starts when haploid vegetative cells produce gametes, but there is insufficient information on quantitative aspects of this process such as the number of gametes produced per cell and the proportion of the vegetative cell population forming gametes as well as the proportion of gametes that mate successfully (Lewis 2002). Furthermore, life cycle variations occur between species (Pollingher 1988, Elbrächter 2003). Generally, one vegetative cell is triggered into transforming into 4 gametes after 2 successive divisions (Coats et al. 1984, Tomas et al. 1989, Cetta & Anderson 1990, Giacobbe & Yang 1999), although in some cases 1 or 3 successive divisions lead to 2 or 8
gametes (von Stosch 1973, Pfiester 1975). Although gametes and vegetative cells may be morphologically similar in some species (Dale 1983, Blackburn et al. 1989, Gao et al. 1989, Elbrächter 2003, Figueroa & Bravo 2005), the simple transformation of a haploid vegetative cell into a gamete has not yet been considered (Lewis 2002). Two gametes fuse to form a diploid planozygote (f), which encysts (g). After a mandatory resting period excystment takes place (h) and a diploid planomeiocyte emerges that produces 4 haploid vegetative cells after 2 consecutive meiotic divisions (i). 1C = nuclear DNA content in G1, 2C = double nuclear DNA content, 1n = haploid, 2n = diploid.

The formation of 4 gametes by 2 asexual divisions has been observed for the dinoflagellates *Gyrodinium uncatenum, Ceratium tripos, C. schrannki* and *Alexandrium taylori* (Coats et al. 1984, Tomas et al. 1989, Cetta & Anderson 1990, Giacobbe & Yang 1999), and 2 arguments are presented here to justify the application of this process (Eq. 1a) in *Scrippsiella lachrymosa*. Firstly, the data from the f/4-medium experiment where nearly all cells encysted (Olli et al. 2004) make clear that the ultimate cyst concentration (51.689 ml⁻¹, when the cell concentration has become low), is close to twice (2.2) the maximum vegetative cell number on Day 16 (23.186 ml⁻¹), when the cyst concentration is still low. When accounting for the cysts already present on Day 16 (8.118 ml⁻¹), the cell:cyst ratio is 1:1.9. In other words, the cell:cyst ratio measured (Olli et al. 2004) is in accordance with the ratio 1:2 in the proposed life cycle (Fig. 1).

Secondly, particle-size measurements have shown that the small cell or gamete of *Scrippsiella lachrymosa* has a median spherical equivalent diameter (sed) of
12 µm and the vegetative cell has a medium sed of 19 µm (Olli 2002). In terms of volume the vegetative:gamete ratio is 3591 µm²:904 µm³ = 4:1 and in accordance with the proposed life cycle (Fig. 1, Eq. 1). It is assumed here that large vegetative cells produce large cysts in the early stages of batch culture growth (Olli & Anderson 2002) but that the smaller sized cysts in older cultures are due to limited resource availability, i.e. all cysts are produced from 2 gametes regardless of their size.

**Calculation of rates and concentrations.** In order to calculate all relevant rates and life cycle stage concentrations, a computer model was constructed that includes batch culture growth with 1 limiting nutrient (Fig. 2). The vegetative cell growth rate is calculated using a Monod-type equation. Although the N:P ratio of f/4 culture medium is 24, the suggested N:P uptake using a Monod-type equation. Although the N:P ratio includes batch culture growth with 1 limiting nutrient where \( \text{NO}_3^- \text{max} \) is the rate-determining nutrient:

\[
\mu_t = (\mu_{\text{max}} \times [\text{NO}_3^-]_{t-1})/K_{\text{n}, \text{NO}_3^-} + [\text{NO}_3^-]_{t-1} \quad (2a)
\]

\( \mu_t \) is the growth rate (d⁻¹) at Day = t, \( \mu_{\text{max}} \) is the maximum growth rate (d⁻¹) under nitrate saturating conditions, \([\text{NO}_3^-]_{t-1}\) is the nitrate concentration (mol m⁻³) at the end of the previous day (Day = t-1) and \( K_{\text{n}, \text{NO}_3^-} \) (mol m⁻³) is a constant: the nitrate concentration at which \( \mu = 0.5 \mu_{\text{max}} \).

The nitrate concentration is calculated daily by subtracting the cumulative number of vegetative cells produced (Σ) from the initial nitrate concentration (0.44 mol m⁻³ in f/4 culture medium):

\[
[\text{NO}_3^-]_t = [\text{NO}_3^-]_{t-0} - \Sigma (\text{new cells})_t \times Q_N \quad (2b)
\]

where \([\text{NO}_3^-]_t\) and \([\text{NO}_3^-]_{t-0}\) are the nitrate concentration at Day = 0 and Day = t, \( \Sigma (\text{new cells})_t \) is the cumulative amount of newly produced vegetative cells on Day = t (total minus inoculum) and \( Q_N \) in mol cell⁻¹ is the N-quotra for vegetative cells. The nitrogen quota is 9 pmol cell⁻¹ (Olli & Anderson 2002), and according to Eq. (1b) vegetative cells have \( Q_N = 18 \) pmol cell⁻¹.

The growth rate \( \mu_t \) from Eq. (2a) is used to calculate the concentration of vegetative cells at t (Cellₜ) from the concentration of vegetative cells the previous day (Cellₜ₋₁). The concentration of vegetative cells (Cellₜ₋₁) has, however, declined during 24 h due to the formation of gametes (which are assumed not to grow). Therefore, Cellₜ₋₁ has to be corrected by subtracting the vegetative cells that produced gametes:

\[
\text{Cell}_t = (\text{Cell}_{t-1} - \text{Cell}_{t-1} \times f_{\text{cell-gam}}) \times e^{\mu_t} \quad (2c)
\]

where \( f_{\text{cell-gam}} \) [0,1] is the fraction of vegetative cells producing gametes.

A problem is that the fraction of vegetative cells producing gametes, i.e. the rate of gamete production, is unknown. Because cysts, and therefore gametes, were produced throughout the *Scrippsiella lachrymosa* experiment (Olli & Anderson 2002), it is assumed for practical reasons that the rate of gamete production \( f_{\text{cell-gam}} \) was constant. However, the model can be extended to make the rate of gamete production dependent on the biomass limiting nutrient concentration or on vegetative cell concentration (Peperzak unpubl.).

The number of gametes on Day = t is:

\[
\Sigma _t = \Sigma (\text{Cells})_{t-1} \times f_{\text{cell-gam}} \times r_{\text{cell-gam}} \quad (2d)
\]

where \( \Sigma _t \) is the number of gametes (m⁻³) produced at Day = t, \( \Sigma (\text{Cells})_{t-1} \) is the cumulative amount of vegetative cells on the previous day and \( r_{\text{cell-gam}} \) is the cell:gamete ratio, which is 4 (Eq. 1a).

The cumulative amount of gametes on Day = t is:

\[
\Sigma (\text{Gam1})_t = \Sigma (\text{Gam1})_{t-1} + \Sigma _t \quad (2e1)
\]

A second problem is that the cumulative amount of gametes at Day = t also has to be corrected because a number of them will have produced planozygotes and cysts. Because planozygotes were never observed in large numbers and encystment in *Scrippsiella lachrymosa* was always fast (<24 h) (Olli & Anderson 2002), it will be assumed that cyst formation can be modelled as occurring instantaneously, i.e. planozygote formation (Fig. 1, Eq. 1a) is skipped and 2 gametes directly produce 1 cyst in the model. As with gamete production, the rate of cyst formation is not known a priori. It will be assumed that there is a constant fraction of gametes transforming into cysts, and, because cysts in the *S. lachrymosa* experiment were produced continuously (Olli & Anderson 2002), the gamete-to-cyst fraction will also be assumed constant throughout the experiment.

The corrected cumulative amount of gametes on Day = t is:

\[
\Sigma (\text{Gam2})_t = \Sigma (\text{Gam1})_{t-1} - \Sigma (\text{Gam1})_{t-1} \times f_{\text{gam-cyst}} \times r_{\text{gam-cyst}} \quad (2f1)
\]

where \( f_{\text{gam-cyst}} \) [0,1] is the fraction of gametes producing cysts.

The cyst production is:

\[
\Sigma (\text{Cyst})_t = \Sigma (\text{Gam1})_{t-1} \times f_{\text{gam-cyst}} \times r_{\text{gam-cyst}} \quad (2f1)
\]

where \( \Sigma (\text{Cyst})_t \) is the number of cysts (m⁻³) produced at Day = t and \( r_{\text{gam-cyst}} \) is the gamete:cyst ratio, which is 0.5 (Eq. 1a).

The cumulative amount of cysts on Day = t is:

\[
\Sigma (\text{Cyst})_t = \Sigma (\text{Cyst})_{t-1} + \Sigma (\text{Cyst})_t \quad (2f2)
\]

Because the data of the *Scrippsiella lachrymosa* experiment are provided as cyst and ‘motile cell’ concentrations (Olli et al. 2004), the model calculates an extra variable, the sum of vegetative cells and gametes:

\[
\text{Motile cell}_t = \text{Cell}_t + \text{Gam}_t \quad (2g)
\]
Model calculations. The data used to calibrate the model (Fig. 2) are the motile cell and cyst concentrations in an f/4 culture medium experiment in which 24 test tubes with 10 ml culture medium each was inoculated with exponentially growing *Scrippsiella lachrymosa* cells and incubated for a maximum of 52 d (Olli et al. 2004). Counts were made 8 times after simultaneously sacrificing 3 tubes, first at 4 d intervals but later at longer intervals. The tubes were probe sonicated for a few seconds to agitate the cysts that had settled to the bottom, and the samples were preserved with Utermöhöhl solution. Full details can be found in Olli & Anderson (2002). The outcome of a comparable experiment in f/2 culture medium (Olli et al. 2004) was used to validate the model.

The calculations (Eqs. 2a–g) were made with time steps of 1 d in a spreadsheet program (Excel) allowing direct computational and graphical evaluation of model outcome against experimental data. Model input variables (Table 1) were changed to optimise the linear correlation coefficients between model output and experimental data of log-transformed motile cell and cyst concentrations respectively.

The model was first tested by changing the input variables $\mu_{\text{max}}$ and $K_{\mu, \text{NO}_3}$ (Table 1). If experimental growth rates from Day 0 to Day 12 in both f/4 and f/2 medium are averaged, a lower $\mu_{\text{max}} = 0.47 \text{ d}^{-1}$ is obtained (Olli et al. 2004). $K_{\mu, \text{NO}_3}$ is unknown, and therefore a value one third the $K_{s, \text{NO}_3}$ of *Peridinium cinctum* was used (Pollingher 1988). Secondly, the cell-gamete ($r_{\text{cell-gam}}$) fraction was varied. Thirdly, the number of gametes produced by a vegetative cell ($r_{\text{cell-gam}}$) was reduced from 4 (Eq. 1a) to 1 (a cell behaving functionally as a gamete). Because a reduction in $r_{\text{cell-gam}}$ changes the ratio of vegetative cells:cysts (Eq. 1b), the N-quota has to be changed accordingly as:

- 1 cell = 4 gametes = 2 cysts (= 2 × 9 pmol N) ⇒ 1 cell = 18 pmol N (2h1)
- 2 cells = 2 gametes = 1 cyst (= 9 pmol N) ⇒ 1 cell = 4.5 pmol N (2h2)

This means a reduction of $Q_N = 18$ ($r_{\text{cell-gam}} = 4$) to $Q_N = 4.5$ ($r_{\text{cell-gam}} = 1$). The game:cyt ratio ($r_{\text{gam-cyst}}$) was kept constant at 0.5 in all calculations because the only feasible way to form a diploid cyst is by fusion of 2 haploid gametes (Fig. 1).

The encystment percentage ($E\%$) is calculated from the ratio of the cumulative concentrations of vegetative cells and cysts:

$$E\% = 100 \times \frac{\Sigma (\text{Cyst})_{t=52}}{\Sigma (\text{vegetative cells})_{t=52}} \quad (2i)$$

RESULTS

The results or model output, obtained by changing the input variables of the model (Table 1), are shown in Table 2. In each run, one input variable was changed to observe the effect on the timing and maximum concentrations of motile cells and cysts and the correlation between the modelled values and those observed experimentally (Olli et al. 2004). A reduction of $\mu_{\text{max}}$ from 0.56 to 0.47 d$^{-1}$ (run 2) and an increase of $K_{\mu}$ from 0.01 to 0.03 (run 3 and 4) resulted in lower correlation...
Table 1. Input variables for run 1 of model calibration of Scrippsiaella lachrymosa growth, gamete formation and cyst production in f/4 culture medium

<table>
<thead>
<tr>
<th>Variable</th>
<th>Value</th>
<th>Source/Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nitrate at t = 0</td>
<td>([\text{NO}<em>3])</em>{t = 0} = 0.442 \text{ mol m}^{-3}</td>
<td>Olli &amp; Anderson (2002)</td>
</tr>
<tr>
<td>Maximum growth rate (\mu_{\text{max}})</td>
<td>0.56 \text{ d}^{-1}</td>
<td>Calculated for Days 0–8 (n = 3) (r^2 = 0.96), Table 1 (Olli et al. 2004)</td>
</tr>
<tr>
<td>Half saturation constant for growth (K_{\mu,\text{NO}_3})</td>
<td>0.01 mol m(^{-3})</td>
<td>1/3 of (K_{\mu,\text{NO}_3}) Peridinium cinctum (Pollinger 1988)</td>
</tr>
<tr>
<td>N quota (Q_N)</td>
<td>18 pmol N cell(^{-1})</td>
<td>9 pmol N cyst(^{-1}) (Olli &amp; Anderson 2002)</td>
</tr>
<tr>
<td>Cells at t = 0</td>
<td>(C_{\text{cell}}_{t = 0}) = 1 \times 10^8 \text{ m}^{-3}</td>
<td>Olli et al. (2004)</td>
</tr>
<tr>
<td>Daily fraction of vegetative cells producing gametes (f_{\text{cell-gam}})</td>
<td>0.1</td>
<td>Range: 0–1</td>
</tr>
<tr>
<td>Vegetative cell:gamete ratio (r_{\text{cell-gam}})</td>
<td>4</td>
<td>See 'Methods'</td>
</tr>
<tr>
<td>Daily fraction of gametes producing cysts (f_{\text{gam-cyst}})</td>
<td>0.5</td>
<td>Range: 0–1</td>
</tr>
<tr>
<td>Gamete to cyst ratio (r_{\text{gam-cyst}})</td>
<td>0.5</td>
<td>See 'Methods'</td>
</tr>
</tbody>
</table>

coefficients, and therefore the following runs were made with \(\mu_{\text{max}} = 0.56\) and \(K_{\mu} = 0.01\). Changing the daily fraction of vegetative cells that produced gametes from 0.0 to 0.4 (runs 5 to 11) led to a modelled cyst concentration ranging from 0 to 1.3 \times 10^{10} with a maximum of 4.9 \times 10^{10} cysts m\(^{-3}\) reached at \(f_{\text{cell-gam}} = 0.15\) (run 8). The maximum motile cell and cyst concentrations in the experiment were 2.3 \times 10^{10} and 5.2 \times 10^{10} m\(^{-3}\) (Olli et al. 2004); 105% and 95% of these numbers were reached in run 8. Therefore, \(f_{\text{cell-gam}} = 0.15\) was used in ensuing calculations.

Changing the daily fraction of gametes that produced cysts from 0.0 to 1.0 (runs 12 to 16) led to a combined correlation coefficient ranging from 0.01 to 1.73–1.74; the maxima were reached at \(f_{\text{gam-cyst}} = 0.75–1.0\) (runs 15 and 16). The calculated maximum motile cell concentration decreased from 9.8 \times 10^{10} m\(^{-3}\) (426%, Day 48, run 12) to 1.7 \times 10^{10} m\(^{-3}\) (74%, Day 14, run 16). The maximum cyst concentration in the experiment was 5.2 \times 10^{10} m\(^{-3}\) on Day 52; 4.9 \times 10^{10} cysts m\(^{-3}\) on Day 51 (94%) were calculated in runs 15 and 16. Run 16 had the highest correlation coefficients between calculated and measured motile cell and cyst concentrations (\(r^2 = 0.80\) and \(r^2 = 0.94\)) (Fig. 3). In run 16 nitrate became depleted on Day 14; at that time 25% of the total cyst yield had already been produced.

Next, the ratio of vegetative cells producing gametes \(f_{\text{cell-gam}}\) was reduced from 4 to 1 in runs 17 and 18 with the other input variables as in run 8 \(f_{\text{gam-cyst}} = 0.5\) and run 16 \(f_{\text{gam-cyst}} = 1.0\) and with N quota at 25% (Eq. 2h2). This led to spurious maximum motile cell concentrations in both runs 17 and 18 of more than 3 \times the concentrations measured in the experiment (Fig. 4, Table 2). On the other hand, the calculated maximum cyst correlation was still 94% of measured values (Table 2).

As expected, rerunning the model for run 16 with f/2 instead of f/4 nitrate concentrations in run 19 doubled both motile cell and cyst maximum concentrations to 3.7 \times 10^{10} m\(^{-3}\) and 9.8 \times 10^{10} m\(^{-3}\) (Table 2). However, in contrast to expectations, the measured cyst yield in f/2 was lower than in f/4 medium (Olli et al. 2004). Although the model accurately calculated the maximum motile cell concentration (100%), the maximum concentration of the cysts appeared to be overestimated (272%, Table 2).

Fig. 3. Scrippsiaella lachrymosa. Model results for run 16: (a) development of motile cell (vegetative cell and gamete) and cyst concentrations in f/4 batch culture growth. Symbols = measured values, lines = model results. According to the model, nitrate became depleted on Day 14 (not shown); (b) linear regression of modelled concentrations over experimental data (cells \(r^2 = 0.80\), cysts \(r^2 = 0.94\))
DISCUSSION

The new model to calculate the growth and encystment of *Scripsiella lachrymosa* in batch culture (Fig. 2) gives adequate quantitative results (Fig. 3, Table 2) despite the "poor counting statistics" (Olli et al. 2004) and a number of assumptions that had to be made (Table 1). To calculate vegetative cell growth, a maximum growth rate had to be estimated from experimental 'motile cell' counts. The growth rate $\mu$ in Olli et al. (2004) is in fact not a vegetative cell growth rate but a 'motile cell' rate calculated from the rate of change in the combined vegetative cell and gamete concentrations (Olli & Anderson 2002). The maximum growth rate used in the model ($\mu_{\text{max}}$, Table 1) was calculated from the first 3 available 'motile cell' counts (Olli et al. 2004), assuming that gamete concentrations then were still low and negligible. A lower growth rate ($\mu = 0.47 \, \text{d}^{-1}$) calculated from both the f/4 and f/2 experiments did not improve model output (Table 2, run 2). The difference between the modelled gross vegetative and the net 'motile cell' growth rates was $0.17 \, \text{d}^{-1}$ (–31%, Table 3). Therefore, in future quantitative studies of the sexual cycle of dinoflagellates, vegetative cells and gametes should preferably be counted separately, not together as 'motile cells'. Because vegetative cells and gametes may be difficult to discern, there is a need for molecular tools that enable rapid identification and enumeration of dinoflagellate life cycle stages (Garces et al. 2002). The application of molecular tools can also lead to the much desired wish to increase the number of quantitatively described dinoflagellate life cycles (Lewis 2002).

The half saturation constant $K_{\text{v}}$, which is needed to calculate vegetative cell growth rate between exponential and stationary growth phase, i.e. under and stationary growth phase, i.e. under...
species. However, changing $K_{\mu,\text{NO}_3}$ derived from several sources in the literature (Fig. 1) is more important in vegetative cell:gamete production (Coats et al. 1984) and between micro- and mesoflagellates—presumed gametes—and diploid non-flagellated cells in the life cycle of Gyrodinium uncatenum between predision vegetative cells and gametes (Coats et al. 1984) and between vegetative cells:gamete volumes in dinoflagellates may range from a factor of 2 to 5 (Coats et al. 1984, Pollinger 1988). Third, the choice of $r_{\text{cell-gam}} = 4$ led to calculated maximum motile (vegetative + gamete) cell concentrations comparable to the counts in f/4 medium (Table 2, runs 1 to 9). The alternative, reducing $r_{\text{cell-gam}}$ from 4 to 1, tripled the calculated maximum motile cell concentrations (runs 17 to 18, Table 2, Fig. 4b). At first, this appears contradictory because when vegetative cells produce fewer gametes, fewer motile cells are expected. However, according to Eqs. (2h1) & (2h2), the cell-cyst stoichiometry has to change too. Because a cyst contains 9 pmol N (Olli & Anderson 2002) and a diploid cyst is formed from 2 haploid gametes, each containing 4.5 pmol N, a vegetative cell also has a $Q_N = 4.5$ pmol N if one gamete emanates from one vegetative cell. In effect, the decrease in cell $Q_N$ from 18 to 4.5 pmol N means that from the initial nitrate concentration (0.442 mol m$^{-3}$) 4 times as much vegetative cells can be produced.

As shown in Fig. 4b, the assumption of 1 cell producing only one gamete leads to motile cell concentrations from day 12 onwards that appear spuriously high compared to measured, as well as to modelled motile cell concentrations using $r_{\text{cell-gam}} = 4$ (Fig. 4a). Modelling the encystment of other dinoflagellate species with little or no morphological differences between vegetative cells and gametes, or with gametes that have a very short lifetime, will provide an additional, numerical method of investigating if the cell:gamete ratio of 4 is appropriate in those species too.

The optimum daily fraction of vegetative cells producing gametes ($f_{\text{cell-gam}} = 0.15$, run 8, Table 2) is a value intermediate to no gamete production ($f_{\text{cell-gam}} = 0.0$, run 5, Table 2) and a gamete production rate that nearly equals the growth rate of the vegetative cells ($f_{\text{cell-gam}} = 0.4$, run 11, Table 2). In the first case, no cysts were produced.

<table>
<thead>
<tr>
<th>Gross vegetative cell growth rate, d$^{-1}$</th>
<th>Net motile cell growth rate, d$^{-1}$</th>
<th>Encystment rate, d$^{-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Exponential</td>
<td>0.55</td>
<td>0.38</td>
</tr>
<tr>
<td>Stationary</td>
<td>0.00</td>
<td>-0.16</td>
</tr>
</tbody>
</table>

and references in the introduction). A gamete:cyst ratio of 0.5 is generally believed to be correct (Olli & Anderson 2002) because the plausible way in which the diploid cyst is produced is from 2 fusing haploid gametes with the diploid planozygote as intermediate. There are 3 arguments for why a cell:gamete ratio of 4 is appropriate in the case of Scrippsiella lachrymosa. First, it was calculated on the basis of the approximate vegetative cell:cyt ratio (2:1) in the f/4 experiment (Olli et al. 2004). Second, the volume of 4 gametes equals that of 1 vegetative cell (Olli 2002). A similar volume ratio has been found in the sexual cycle of Gyrodinium uncatenum between predision vegetative cells and gametes (Coats et al. 1984) and between micro- and mesoflagellates—presumed gametes—and diploid non-flagellated cells in the life cycle of the prymnesiophyte Phaeocystis globosa (Peperzak et al. 2000). However, this volume argument is not decisive: vegetative cell:gamete volumes in dinoflagellates may range from a factor of 2 to 5 (Coats et al. 1984, Pollinger 1988). Third, the choice of $r_{\text{cell-gam}} = 4$ led to calculated maximum motile (vegetative + gamete) cell concentrations comparable to the counts in f/4 medium (Table 2, runs 1 to 9). The alternative, reducing $r_{\text{cell-gam}}$ from 4 to 1, tripled the calculated maximum motile cell concentrations (runs 17 to 18, Table 2, Fig. 4b). At first, this appears contradictory because when vegetative cells produce fewer gametes, fewer motile cells are expected. However, according to Eqs. (2h1) & (2h2), the cell-cyst stoichiometry has to change too. Because a cyst contains 9 pmol N (Olli & Anderson 2002) and a diploid cyst is formed from 2 haploid gametes, each containing 4.5 pmol N, a vegetative cell also has a $Q_N = 4.5$ pmol N if one gamete emanates from one vegetative cell. In effect, the decrease in cell $Q_N$ from 18 to 4.5 pmol N means that from the initial nitrate concentration (0.442 mol m$^{-3}$) 4 times as much vegetative cells can be produced.

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are produced. In the latter case, gametes are produced so quickly that vegetative cells have no time to enter the mitotic cycle and divide by binary fission (Fig. 1). In other words, the rate of gamete production then severely limits vegetative growth rate so that insufficient new vegetative cells, and hence gametes and cysts, are produced. This is reflected in the model output first as a breakdown of the correlation coefficient between observed and modelled motile cell concentrations and, second, by low cyst concentrations (Table 2, run 11). In batch cultures with encysting dinoflagellates, \( f_{\text{cell-gam}} \) is in fact the loss factor that reduces gross vegetative cell growth rate to a net growth rate. If, however, the encystment rate is taken as the direct loss factor (Olli et al. 2004), the intermediate gamete stage with its own kinetics (Fig. 2) is incorrectly omitted from population dynamics.

In the stationary growth phase, any increase in cyst concentration and encystment rate at low vegetative cell concentrations (Olli et al. 2004) must then be accounted for by an equivalently high growth rate, which is unrealistic because nutrients have been depleted. In the present model (Fig. 2), vegetative cells constantly form a ‘reservoir’ of gametes that continuously produces cysts, even after Day 14 when nitrate has been depleted (Fig. 3, Table 3). This means that cyst production can continue without the need for vegetative cell growth, as apparently was the case in the * Scrippsiella lachrymosa * 1/4 batch culture.

The coupling of encystment rate with growth rate is probably not the only cause of the extremely high values (>8 d\(^{-1} \)) of the calculated growth rates in the equation by Olli et al. (2004). Low motile cell counts in the stationary growth phase may have been caused by the probe sonication that was applied to agitate the cysts that had settled to the bottom of the culture tubes. Using an ultrasonic cleaning bath, mild 1 min sonication of natural samples containing vegetative cells and gametes of * Scrippsiella trochoidea* destroyed 10% of the vegetative cells and 30% of the gametes (Peperzak unpubl. data). Furthermore, a longer probe sonication of 1 min has been used purposely to destroy motile cells in cyst-containing * Alexandrium tamarense* cultures (Anderson et al. 1984). Therefore, it is likely that probe sonication in the * S. lachrymosa* samples destroyed a considerable number of motile cells, thereby lowering the cell counts and hence, in order to numerically compensate for this loss, leading to an overestimation of growth rates.

The final step in the encystment process, the formation of cysts from gametes, could be modelled optimally at values of \( f_{\text{gam-cyst}} = 0.75 \) to 1.0 (Table 2, runs 8 and 16). Such a high daily fraction of gametes that produces cysts also means that the intermediate stage, the planozygote, has a short life span (<1 d). This is in accordance with the low numbers of * Scrippsiella lachrymosa* planozygotes that were observed in the experiment and corroborates the suggestion that this stage has a short duration (Olli 2002). In addition, apparently no observations of fusing gametes were made in the experiment. This may be due to the altogether rapid transformation of gametes into cysts, but it may also be emphasized by the possibility that gamete fusion only takes place during a certain, relatively short, period in the diel cycle (Pfiester 1975, Coats et al. 1984) that is not sampled.

The model, which assumes constant gamete and cyst formation (Fig. 2), can be extended to account for the timing of cyst formation that appears to be several days early compared to measured cyst concentrations (Figs. 3a & 4a). Such an extension could be based on the perception that gametes are formed below a certain nutrient concentration (Anderson et al. 1984) or above a threshold vegetative cell concentration (Peperzak unpubl.) or that encystment simply begins at the peak of exponential growth (Dale 1983). Experiments at ecologically relevant nutrient concentrations and cell abundances are needed to determine the mechanisms that induce gamete formation, gamete fusion and transformation of the planozygote into a cyst. In addition, modelling of the dinoflagellate sexual cycle may prove more difficult than in * Scrippsiella lachrymosa* if encystment is regulated by a complex interplay of nutrient concentration with several other factors such as day length and temperature (Sgrosso et al. 2001). Furthermore, several dinoflagellate species are capable of forming asexual resting spores (hynospores) which are very similar to hypnozygotes (van den Hoek et al. 1995). Because hynospores are haploid, the present model for hypnozygotes will probably not function appropriately and should be adapted.

If indeed gamete fusion and planozygote and cyst formation take place during defined time windows in the sexual cycle (Coats et al. 1984), the possibility of measuring the encystment rate becomes possible, even in the sea (in situ) and without bottle incubations. In the mitotic cycle (Fig. 1) the specific fraction of the population that is going to divide increases its DNA content during S-phase and has a double DNA content in the G2M phase. The duration of both phases can be used as terminal events, key variables that form the basis of modelling in situ vegetative growth rates (McDuff & Chisholm 1982, Carpenter & Chang 1988, Chang & Carpenter 1988). Likewise, a phased transition in the sexual cycle, haploid gametes forming diploid planozygotes and planozygotes forming cysts, provides a possibility of measuring in situ encystment rates. This means identification of individual cells, quantification of their DNA content, enumeration of the different stages and use of the duration of the
planozygote stage as a terminal event. Besides a phased transition, another condition would be that all diploid stages, fusing gametes, the planozygote, the cyst and the vegetative cell in G2M phase must be readily distinguishable from each other. Besides differences in pigmentation and the extra ‘trailing flagellum’, planozygotes are 1 to 2 times larger in size than vegetative cells, and gametes are 1 to 2 times smaller in size than vegetative cells (Coats et al. 1984, Blackburn et al. 1989, Giacobbe & Yang 1999). However, in several species such differences in length or width may not exist or are difficult to measure and to use in the identification of the sexual stages. Furthermore, there may be large intraspecific ranges in each stage’s size (Coats et al. 1984). In such cases there is a need for specific molecular probes that label, for instance fluorescently, the different stages in the vegetative and sexual cycles (Garces et al. 2002). Cysts are morphologically very distinct from motile cells (Dale 1983), and their formation may be used to define the end of the planozygote terminal event. Although the measurement of the in situ encystment rate appears to be a challenging task, because encystment is a key step in dinoflagellate ecology the feasibility of the technique deserves further study.

After testing the model input variables (Table 1, Fig. 2) that were inherent to the *Scrippsiella lachrymosa* vegetative and sexual cycles and comparing the output with the experimental results in f/4 medium (Table 2), the model was validated on data obtained in f/2, a medium with added nutrient concentrations double that of f/4 (Olli & Anderson 2002). Unfortunately, the measured cyst yield in f/2 was lower than in f/4 (Olli et al. 2004). The model correctly predicted motile cell concentrations double that of f/4 (Olli & Anderson 2002). The model correctly predicted motile cell concentrations in f/2 (3.7 × 10^10 m^-3) and a final cyst concentration twice that in f/4 (9.8 × 10^10 m^-3, Table 2, run 19). In fact, the model accurately calculated the cyst yield (10^11 m^-3) of *Scrippsiella lachrymosa* in f/2 medium when grown in culture plate wells (Olli & Anderson 2002) instead of culture tubes (Olli et al. 2004).

Coupled with the observation that the calcareous (CaCO3) cover of the cysts was only formed in the initial stages of culture growth (Olli & Anderson 2002), it can be hypothesised that inorganic carbon was a second limiting nutrient in the tubes. Assuming a seawater inorganic carbon concentration of 2.3 mol m^-3 (Stumm & Morgan 1996), the C:N ratios in f/4 and f/2 medium are 5.2 and 2.6 respectively. The carbon content of a vegetative *Scrippsiella lachrymosa* (V = 3591 µm^-3, see ‘Methods’) is 10^3.94 × log V – 0.6/12 (Smayda 1978) = 46 pmol C cell^-1. Combined with an N quota of 18 pmol cell^-1 (Eq. 2h1), the vegetative cells of *S. lachrymosa* have a C:N = 2.6, which is exactly the C:N of f/2 medium. This would mean that f/4 medium (C:N = 5.2) contains a sufficient initial inorganic carbon concentration but that f/2 medium contains the precise initial inorganic carbon concentration to yield the amount of vegetative cells that was observed experimentally and calculated by the model (Table 2). However, the formation of larger and CaCO3-covered cysts in the early stages of the cultures (Olli & Anderson 2002) means that relatively more inorganic carbon is needed for cyst formation than for vegetative cells alone. In f/2 medium this could well lead to carbon limitation of cyst production, especially if the diffusion of CO2 from the atmosphere into the culture medium is hampered, as in closed tubes (Olli et al. 2004). Culture wells in plates have a large surface:volume ratio that may sustain CO2 diffusion, increasing overall C:N in time, leading to complete encystment even in f/2 medium (Olli & Anderson 2002). Clearly, inorganic carbon limitation of dinoflagellates, especially those producing calcareous cysts in culture media with high N and P concentrations as f/2, should be considered as one of the causes for the often observed low encystment percentages in batch cultures (Anderson et al. 1984).

The model calculations (Fig. 2) depended on experimental quantification of the motile cells and the cysts of *Scrippsiella lachrymosa* in batch culture. Although the authors stressed that their counting statistics were poor (Olli et al. 2004), their data were sufficient to simulate motile cell and cyst development as well as the high encystment success in f/4 medium. In addition, the model permitted the calculation of meaningful *S. lachrymosa* vegetative cell growth and encystment rates. The model should be tested with other species of dinoflagellates, especially those producing calcareous cysts in culture media with high N and P concentrations as f/2, should be considered as one of the causes for the often observed low encystment percentages in batch cultures (Anderson et al. 1984).

In contrast to batch cultures, net cell growth rates as well as encystment rates in the sea cannot be measured accurately from counts due to dispersion, sedimentation and natural losses such as grazing. The measurement of gross in situ growth rates by measuring the fraction, not the cell concentrations, of the population undergoing mitosis gets around such complications (McDuff & Chisholm 1982, Carpenter & Chang 1988, Chang & Carpenter 1988, 1990, 1991, Antia et al. 1990). If the stages of the sexual cycle can be identified properly, the cohort of encysting planozygotes could possibly be used as a means of measuring the in situ encystment rate of a dinoflagellate. However, this encystment rate should not be considered as a direct loss factor of the growth rate (Olli et al. 2004) but as a loss factor of the vegetative cell population. Furthermore, encystment probability is the chance that a planozygote will transform into a cyst and is dependent on the probability of 2 gametes fusing to form a
planozygote, which is a function of their size, swimming speed and concentration (Peperzak unpubl.), Encystment success or encystment yield should not be calculated from rates but from the cumulative fraction of the population of dinoflagellates that, in the course of days to months, has formed cysts. Encystment success will therefore remain a difficult variable to measure in situ.

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