ABSTRACT: Parameters in the photosynthesis–irradiance (P-E) relationship of phytoplankton were measured at weekly to bi-weekly intervals for 20 yr at 6 stations on the Rhode River, Maryland (USA). Variability in the light-saturated photosynthetic rate, $P_{\text{max}}^B$, was partitioned into interannual, seasonal, and spatial components. The seasonal component of the variance was greatest, followed by interannual and then spatial. Physiological models of $P_{\text{max}}^B$ based on balanced growth or photoacclimation predicted the overall mean and most of the range, but not individual observations, and failed to capture important features of the seasonal and interannual variability. $P_{\text{max}}^B$ correlated most strongly with temperature and the concentration of dissolved inorganic carbon (IC), with lesser correlations with chlorophyll $a$, diffuse attenuation coefficient, and a principal component of the species composition. In statistical models, temperature and IC correlated best with the seasonal pattern, but temperature peaked in late July, out of phase with $P_{\text{max}}^B$, which peaked in September, coincident with the maximum in monthly averaged IC concentration. In contrast with the seasonal pattern, temperature did not contribute to interannual variation, which instead was governed by IC and the additional lesser correlates. Spatial variation was relatively weak and uncorrelated with ancillary measurements. The results demonstrate that both the overall distribution of $P_{\text{max}}^B$ and its relationship with environmental correlates may vary from year to year. Coefficients in empirical statistical models became stable after including 7 to 10 yr of data. The main correlates of $P_{\text{max}}^B$ are amenable to automated monitoring, so that future estimates of primary production might be made without labor-intensive incubations.

KEY WORDS: Phytoplankton · Photosynthesis · Primary production · Estuary · Rhode River · Interannual variability
practice of normalizing the rate of photosynthesis to the concentration of chlorophyll a (chl a), which is easily measured and amenable to satellite remote sensing (Platt & Sathyendranath 1988).

Parameters of the P-E curve are typically measured over seasonal cycles in studies from 1 to several years duration (Domingues et al. 2011, Gameiro et al. 2011). \( P_{\text{max}} \) typically displays a seasonal pattern with a winter minimum and summer maximum, driven principally by temperature (Lohrenz et al. 1994, Gameiro et al. 2011). Day-to-day variation in \( P_{\text{max}} \) has also been shown to be substantial (Côté & Platt 1983), as has diurnal cycling (Harding et al. 1982). Interannual variation in P-E parameters has not been widely studied, although Harrison & Platt (1980) mentioned that separate years were statistically indistinguishable in their analysis of 8 yr of data from Bedford Basin, Nova Scotia (Canada).

Several models for estimating \( P_{\text{max}} \) from environmental factors have been derived, incorporating varying degrees of physiological detail (Cullen 1990, Cloern et al. 1995, Behrenfeld et al. 2002, see review by MacIntyre et al. 2002). One widely adopted approach links photosynthesis to phytoplankton growth rate via the cellular chl a to carbon ratio, chl:C, which depends on light, temperature, and nutrients (Cloern et al. 1995). Using an approach based on photo-acclimation, Behrenfeld et al. (2002) parameterized separate light-dependent relationships for relative changes in Calvin cycle capacity and cellular chlorophyll for nutrient-deficient and -sufficient conditions. Models represent hypotheses about the relative strength of controlling factors, and their use with measurements can help reveal the relative importance of different factors in the situation of interest. Moreover, possession of a suitably verified model is the best prospect for obtaining reliable future estimates of P-E parameters in the absence of continuing measurements.

Concerns about climate and atmospheric change indicate that there is a need for long-term measurements of factors governing phytoplankton primary production. Two of the factors of concern, temperature and \( \text{CO}_2 \) concentration, are of direct importance in the photosynthesis process. The objectives of this work were therefore to determine the patterns and controls on the P-E parameters of phytoplankton in a shallow eutrophic estuary, with emphasis on variations in the maximal photosynthesis rate normalized to chl a, \( P_{\text{max}}^{a} \). Presented here are measurements and analysis of \( P_{\text{max}}^{a} \) and environmental correlates from the Rhode River, Maryland (USA), a shallow tributary of Chesapeake Bay, collected at weekly to bi-weekly intervals for 20 yr. The ability of 2 simple physiologically based models to reproduce temporal and spatial patterns in the measurements are examined, and statistical models based on ancillary measurements are derived. In this system, interannual variability is substantial, and appears to be driven more by changes in inorganic carbon concentrations than by temperature.

**MATERIALS AND METHODS**

**Study site**

The Rhode River (38° 52’ N, 76° 31’ W) is a shallow, eutrophic tributary on the western shore in the mesohaline zone of Chesapeake Bay in Maryland (USA). The average tidal range is about 30 cm, although larger changes in depth are driven by atmospheric pressure gradients or strong winds that move water into or out of the main axis of Chesapeake Bay (Jordan et al. 1991a). Salinity varies from 0 at the head following runoff events to nearly 20 at the mouth following prolonged droughts. The system has been the subject of long-term studies of nutrients and chlorophyll (Jordan et al. 1991a,b), phytoplankton blooms and species composition (Gallegos et al. 1997, 2010), and fish and invertebrates (Hines et al. 1990). Average depth of the Rhode River is 2 m and varies from 4 m at the mouth to <1 m in an area of broad subtidal mudflats near the head. The estuary is usually well mixed vertically (Seliger & Loftus 1974), although subsurface peaks in the concentration of chl a are sometimes present near the Secchi depth associated with dinoflagellate blooms (Gallegos et al. 1992).

**Field measurements**

The Rhode River was sampled at 6 stations at weekly to bi-weekly intervals from 1990 to 2009. Sampling period usually ranged from early March through mid-December depending on ice and weather conditions or availability of boats, although in some years sampling continued all year, especially early in the series. Stations are designated by their distance from the mouth (km, positive up estuary) and coincide with those shown by Gallegos et al. (2010), exclusive of Stn 6.2, at which P-E curves were not measured. Measurements on station consisted of profiles of temperature (\( T \)), salinity, and dissolved oxygen with a Hydrolab™ (1990 to 2005) or YSI™ 6600 (April 2005 onwards) datasonde, and cosine-
corrected photosynthetically active radiation (PAR, 400 to 700 nm) with a Li-Cor Li-192 underwater quantum sensor. The diffuse attenuation coefficient for PAR, $K_d$, was determined by regression of the natural log of PAR against depth. Secchi depth was measured on the sunny side of the boat. Samples for depth-averaged chl $a$ concentration were collected by slowly lowering and raising a Labline™ Teflon™ sampler in less time than required to fill. Samples for P-E parameters, discrete chl $a$, and species composition were collected by filling the sampler at the Secchi depth.

**Laboratory measurements**

Subsamples for species identification were preserved immediately in the field using 1% acid Lugol’s solution and stored in 125 ml polyethylene bottles until counting. For counting, 1 to 10 ml were settled (minimum 4 h) and viewed at a magnification of 512× under an inverted microscope. Complete identification, counting, and analysis procedures for phytoplankton species composition are given by Gallegos et al. (2010). Subsamples for chl $a$ analyses were filtered onto Whatman GF/F glass fiber filters immediately upon returning to the laboratory. Filters were extracted in 10 ml of 90% acetone either immediately or after freezing for <2 wk. Extracted chl $a$ was estimated spectrophotometrically using the wavelengths and equations given by Jeffrey & Humphrey (1975).

Phytoplankton photosynthesis was measured as $^{14}$C uptake using the small volume ‘photosynthetron’ method of Lewis & Smith (1983). A 50 ml subsample was inoculated with 0.5 to 2.5 µCi ml$^{-1}$ NaH$^{14}$CO$_3$, depending on phytoplankton biomass. Subsamples of 1 ml were dispensed into 24 lighted and 2 dark 7 ml glass scintillation vials, which were placed in an aluminum block drilled with holes for lighting from below. Samples from 3 stations at a time were incubated for 1 h at a range of light intensities supplied by a Westinghouse 400 W metal halide lamp. These lamps have a wide but irregular spectrum (Bubenheim et al. 1988), but $P^{B}_{\text{max}}$ is expected to be relatively insensitive to spectral energy distribution (Pickett & Meyers 1966, Sathyendranath & Platt 1989, Lorenzo et al. 2004). Incubations were terminated by the addition of 250 µl of 1 N HCl and shaking 1 h to drive off unincorporated $^{14}$C. Rates of $^{14}$C fixation were calculated by the equations of Strickland & Parsons (1972), using an isotope discrimination factor of 1.06. Various instruments were used to measure the concentration of dissolved inorganic carbon (IC): a Shimadzu TOC5000 (1990 to 1997), a Capni-Con 5 Total CO$_2$ Analyzer (Cameron Instruments, 1998 to 2006), and a Li-Cor 7000 (2007 to 2009). Instruments were calibrated to known solutions before each cruise. IC concentrations were determined by titration (Strickland & Parsons 1972) whenever instruments were being repaired.

**Data analysis**

Parameters were estimated in the P-E relationship (Jassby & Platt 1976) as

$$P^{B}(E) = \frac{P_{\text{max}}^{B}}{P_{\text{max}}^{B}} \tanh \left( \frac{\alpha^{B} E}{P_{\text{max}}^{B}} \right) + R^{B}$$

where $P^{B}$ is the $^{14}$C photosynthesis rate normalized to chl $a$, $E$ is the photon flux density measured in the incubation vial, $P_{\text{max}}^{B}$ is the maximal photosynthesis rate at light saturation, $\alpha^{B}$ is the slope of the linear portion of the P-E relationship at low light intensities, and the intercept, $R^{B}$, is allowed to be positive or negative to avoid bias in the calculation of $\alpha^{B}$. Parameters were estimated by minimization of squared residuals, except in 2007, when, due to funding limitations, $P_{\text{max}}^{B}$ was estimated from measurements of $^{14}$C uptake in 5 vials incubated at light intensities previously found to be light-saturating. Typical magnitudes for the coefficients of variation of the parameters were 10% for $P_{\text{max}}^{B}$ and 20% for $\alpha^{B}$. The emphasis of this paper in on analysis of $P_{\text{max}}^{B}$ due to its importance in governing primary production in shallow waters.

Measurements of $P_{\text{max}}^{B}$ and its environmental correlates were analyzed for temporal and spatial variability by general linear modeling (GLM), with month and station as categorical variables, and year was treated both as a categorical variable and as a continuous variable to test for the presence and significance of any long-term trends. Temporal and spatial patterns uncovered by the GLM analysis of measurements were then used as the benchmark for evaluation of physiologically and statistically based models. GLM analyses were performed using the Data Desk 6.1 statistical analysis program.

**Physiological models**

Two physiologically based models were examined, one based on carbon balance and the chl:C ratio, and PhotoAcc by Behrenfeld et al. (2002). The con-
connection between balanced growth rate and photosynthetic rate has been made by several authors (Eppley 1972, Cullen 1990, Cloern et al. 1995) as an energy balance,

$$\frac{\mu + r}{D} = P^B (\text{chl:C}) \quad (2)$$

where $\mu$ (d$^{-1}$) is the carbon-specific growth rate, $r$ (d$^{-1}$) is the carbon-specific respiration rate, $D$ (h d$^{-1}$) is the photoperiod, chl:C is the cellular chl a to carbon ratio, and as before, $P^B$ is the chlorophyll-specific photosynthetic rate. To estimate growth rate of a mixed-species assemblage, $\mu_j$ of the $j$th taxon were calculated from allometric equations with cell carbon (Tang 1995) calculated from phytoplankton counts and volume estimates (Gallegos et al. 2010),

$$\mu_j = a_j C_j^B \quad (3)$$

where $a_j = 2.04$ for dinoflagellates and 3.56 for all other taxa, and $\beta = -0.19$ for all taxa (Tang 1995). $\mu$ for the sample was calculated as the carbon-weighted average of the taxa present and scaled for temperature by an exponential factor with a value of 1 at 20°C and $Q_10$ of 2. Taking this as the balanced growth rate at light-saturation, $P^B_{\text{max}}$ was calculated by re-arrangement of Eq. (9) of Cloern et al. (1995),

$$P^B_{\text{max}} = \frac{(\mu + 0.015)}{0.85D \times \text{chl:C}} \quad (4)$$

where the constants 0.85 (dimensionless) and 0.015 (d$^{-1}$) account for growth rate-dependent and -independent respiratory losses, respectively, and $D$ was taken from a table of daylight hours calculated for the latitude of the Rhode River. Chl:C was calculated from Eq. (15) in Cloern et al. (1995), ignoring the nutrient term,

$$\text{Chl:C} = 0.003 + 0.0154\exp(0.05T)$$

$$\left\{ \exp\left(-0.059 \frac{E_0}{K_a H}\right) \left[1 - \exp(-K_d H)\right] \right\} \quad (5)$$

where $E_0$ is incident irradiance (mol quanta m$^{-2}$ d$^{-1}$) on the day prior to sampling, $T$ is temperature (°C), and $H$ = station depth (m). This is referred to as the basic balanced growth model. Subsequent analysis (see below) revealed that the temperature sensitivity of $P^B_{\text{max}}$ resulted in chl:C that were too low in winter to spring months, resulting in systematic overestimates of $P^B_{\text{max}}$. An adjusted balanced growth model was then considered by standardizing Eq. (5) at 25°C. Behrenfeld et al. (2002) derived the PhotoAcc model from a consideration of the effects of photoacclimation and nutrient limitation on relative changes in cellular chl a concentrations and photosynthetic carbon fixation capacity. Their fitted equation for $P^B_{\text{max}}$ under nutrient-sufficient conditions was given by

$$P^B_{\text{max}} = \left[0.036 + 0.3\exp(-3I_g)\right]^1 \quad (6)$$

where $I_g$ (mol quanta m$^{-2}$ h$^{-1}$) is the growth irradiance for acclimation, which they took to be the irradiance at the bottom of the mixed layer. For nutrient-deficient conditions, Eq. (6) was multiplied by a scalar of 0.4 (Behrenfeld et al. 2002). They considered $P^B_{\text{max}}$ to be insensitive to temperature above 5°C. For application in the shallow Rhode River, $I_g$ was calculated as the hourly averaged light reaching the bottom, $(E_0/24)\exp(-K_d H)$, as is referred to as the basic PhotoAcc model. Subsequent analysis (see below) revealed that the seasonal pattern calculated by the basic PhotoAcc model was dampened and out of phase with measurements due to positive correlation between $E_0$ and $K_d$ as a result of high attenuation coefficients in summer (Gallegos et al. 2005). An adjusted PhotoAcc model was then considered using water column-averaged light intensity, $I_{av}$, in place of the light at the bottom

$$I_{av} = \frac{E_0}{K_d H} \left[1 - \exp(-K_d H)\right] \quad (7)$$

substituting $I_{av}$ for $I_g$ in Eq. (6). Due to the difference in scale between $I_{av}$ and $I_g$, it was necessary in the adjusted version to use the nutrient-limited version of PhotoAcc, which multiplies the right hand side of Eq. (6) by 0.4 (Behrenfeld et al. 2002). Other modeling approaches have been elaborated (e.g. Geider et al. 1998), but these examined here could be applied with data at hand, and the need for more complex photoacclimation models has been questioned (Flynn 2003).

**Statistical models**

Statistical models for the dependence of $P^B_{\text{max}}$ on various environmental correlates were estimated by stepwise linear regression on data transformed to normalize and account for the expected mode of response (Harding et al. 2002). A forward selection procedure was used with a criterion of 2% increment in adjusted $R^2$ to remain, and the order of trial determined by the rank order of the $t$-statistic in an initial analysis that included all available predictors. The winter months were unevenly sampled in different years due to weather conditions and boat availability. Therefore, the data were additionally analyzed for interannual variability and estimated statistical mod-
els using data from the month of September, typically
the month of the annual maximum in this system.
Transformations to achieve normality (Kolmogorov-
Smirnov test) were square root for $P_{B_{\text{max}}}$ and natural
logarithm for $T$, chl $a$, and $K_d$. No transformations
were needed to normalize the IC concentrations or
principal component (PC) scores of species abun-
dances. PC scores were computed on $\ln(1+\text{cells ml}^{-1})$
of counts data. Further details of the PC analysis and
taxa in the species list are given by Gallegos et al.
(2010). PAR values averaged over the water column
for 1 or 3 d prior to sampling were tested but were not
significant correlates of $P_{B_{\text{max}}}$.
The length of the time series and the density of
measurements provide an opportunity to examine
the stability of parameter estimates in the statistical
models. Once the significant predictors were deter-
mined, parameters were estimated for each year, to
compare with parameters estimated by each succes-
sive year cumulatively, and in both 3 and 5 yr group-
ings of the data.

RESULTS

Observed variations

$P_{B_{\text{max}}}$ in the Rhode River ranged from 0.1 to 21.2 mg
C mg$^{-1}$ chl $a$ h$^{-1}$ from 1990 to 2009, and averaged
$3.5 \pm 2.1$ (SD) mg C mg$^{-1}$ chl $a$ h$^{-1}$ (Fig. 1A). The ex-
pected seasonal pattern was repeated each year,
with minimal values in winter and highest values and
the most scatter in summer (Fig. 1A,B), such that the
lowest values in summer usually overlapped the
highest measurements in winter (Fig. 1A). The GLM
analysis of $P_{B_{\text{max}}}$ in terms of year, season, and station
showed that month (i.e. season) accounted for the
greatest amount of the variance (mean square, MS = 370), followed by year (MS = 79), then station (MS = 22). The seasonal expected value of measured $P_{B_{\text{max}}}$
varied approximately sinusoidally over the year, with
a minimum in January and maximum in September
(Fig. 1B). Differences among years were apparent as
well. For example, more values $> 10$ mg C mg$^{-1}$ chl $a$
h$^{-1}$ were observed prior to 1997 (35 of 1419 measure-
ments) compared with the period after 1997 (5 of
1863 measurements; Fig. 1A). Occasional elevated
winter minima are evident, for example in 1997 and
2006 to 2008 (Fig. 1A). Treating year as a continuous
variable in the GLM revealed a significant ($p < 10^{-4}$)
downward trend of $-0.042$ mg C mg$^{-1}$ chl $a$ h$^{-1}$ yr$^{-1}$
(Table 1), which remained statistically significant
($p < 10^{-4}$) at $-0.033$ mg C mg$^{-1}$ chl $a$ h$^{-1}$ yr$^{-1}$ ignoring
the anomalously high year 1996. This trend was even
stronger, $-0.135$ mg C mg$^{-1}$ chl $a$ h$^{-1}$ yr$^{-1}$, when the
data were selected for the more evenly sampled
month of September (Table 1). Spatial variability in measured $P_{B_{\text{max}}}$
was statistically significant (Fig. 1C), though as noted, accounting for less variance than
either seasonal or interannual modes. The spatial
mean was greatest beyond the mouth outside the
Rhode River (km $-1.4$) and lowest 2 km up estuary of
the mouth (Fig. 1C).

Physiological models

The GLM analysis of $P_{B_{\text{max}}}$ calculated by the phys-
iological models in terms of year, season, and station
differed from the analysis of observed $P_{B_{\text{max}}}$, with
Table 1. Slopes and statistics of the measured or modeled light-saturated rate of phytoplankton photosynthesis normalized to chlorophyll a ($P_{\text{max}}^a$) and environmental correlates against year as estimated by general linear modeling analysis treating year as a continuous variable. Units of slope are mg C mg$^{-1}$ chl a h$^{-1}$ yr$^{-1}$ for $P_{\text{max}}^a$, and as given for environmental correlates. T: temperature; IC: inorganic carbon; $K_d$: diffuse attenuation coefficient for photosynthetically active radiation; PC: principal component.

<table>
<thead>
<tr>
<th>Measured or modeled $P_{\text{max}}^a$</th>
<th>Slope</th>
<th>t</th>
<th>p</th>
</tr>
</thead>
<tbody>
<tr>
<td>Measured $P_{\text{max}}^a$, all data</td>
<td>-0.042</td>
<td>-7.85</td>
<td>&lt;10$^{-4}$</td>
</tr>
<tr>
<td>Measured $P_{\text{max}}^a$, September</td>
<td>-0.135</td>
<td>-6.51</td>
<td>&lt;10$^{-4}$</td>
</tr>
<tr>
<td>Basic balanced growth model</td>
<td>-0.024</td>
<td>-3.90</td>
<td>0.003</td>
</tr>
<tr>
<td>Adjusted balanced growth model</td>
<td>-0.013</td>
<td>-1.71</td>
<td>0.088</td>
</tr>
<tr>
<td>Adjusted balanced growth model, lower estuary</td>
<td>-0.006</td>
<td>-0.74</td>
<td>0.459</td>
</tr>
<tr>
<td>Basic PhotoAcc model</td>
<td>0.002</td>
<td>0.33</td>
<td>0.74</td>
</tr>
<tr>
<td>Adjusted PhotoAcc model</td>
<td>0.005</td>
<td>1.17</td>
<td>0.24</td>
</tr>
<tr>
<td>Adjusted PhotoAcc model, lower estuary</td>
<td>0.007</td>
<td>1.78</td>
<td>0.075</td>
</tr>
</tbody>
</table>

**Stepwise regression model, all data**

- ln(T) predictor: 0.003, 2.58, 0.01
- ln(T), IC predictors: -0.010, -4.51, <10$^{-4}$
- All predictors: -0.029, -8.95, <10$^{-4}$

**Stepwise regression model, September**

- IC predictor: -0.068, -6.12, <10$^{-4}$
- All predictors: -0.166, -9.41, <10$^{-4}$
- ln(T) (yr$^{-1}$): 0.0021, 3.26, 0.001
- ln(chla) (yr$^{-1}$): -0.056, -5.91, <10$^{-4}$
- ln(Kd) (yr$^{-1}$): 0.012, 5.73, <10$^{-4}$
- ln(Kd) (yr$^{-1}$): -0.002, -1.69, 0.091
- PC 5 (yr$^{-1}$): -0.002, -0.56, 0.57
- PC 4, September (yr$^{-1}$): 0.004, 0.32, 0.61

station accounting for the greatest amount of variance, followed by month then year for each model. Nevertheless, presentation will follow the order of the analysis of observed data.

**Seasonal variability**

The seasonal variability predicted by both physiologically based models was suppressed relative to measurements (Fig. 2A,B). For the basic balanced growth approach (Fig. 2A) this was found to be due to excessive temperature sensitivity of the chl:C ratio (Fig. 3A). The low values of chl:C predicted by Eq. (5) in spring and winter (Fig. 3A, squares), when substituted into the denominator of Eq. (4), produced excessively high values of $P_{\text{max}}^a$ thereby dampening the overall predicted seasonal variability. Adjustment of the balanced growth model to standardize the temperature at 25°C in Eq. (5) dampened the seasonal variability in chl:C (Fig. 3A, circles) and thereby restored seasonal variability in $P_{\text{max}}^a$, albeit with substantial over-prediction in May and June (Fig. 2A, blue triangles).

In predictions by PhotoAcc, the dampening of predicted seasonality was caused by the seasonal covariation of incident light (photoperiod and maximal noon irradiance) with the light attenuation coefficient (Gallegos et al. 2005), causing calculated $I_a$ (Eq. 6, Fig. 3B, squares) to have a local maximum in March with increasing photoperiod and maximum irradiance, and a local minimum in August due to seasonally high $K_d$. Adjustment of the PhotoAcc calculation to use averaged light in the water column for growth irradiance (Fig. 3B, circles) restored unimodal seasonality in $P_{\text{max}}^a$ with a maximum in June (Fig. 2B, blue triangles), although predictions were substantially out of phase with observations. Additionally, when using water column-averaged light in PhotoAcc, it was necessary to use the nutrient limited form to achieve an appropriate scale in the calculations.

Subsequent analysis of spatial variability (see below) indicated that over predictions by both models could be driven by calculations for the shallow upper estuary stations where shallow depths resulted in lower calculated chl:C (Eq. 5) and higher $I_a$, (Eq. 7). The data were therefore reanalyzed for seasonal and interannual variability based on stations from the lower estuary alone (km < 2.0) (Fig. 2A,B, green triangles). Analyzed in this way, the predictions of monthly mean $P_{\text{max}}^a$ by the adjusted balanced growth approach closely matched monthly means from January through July, but under predicted observed monthly means from August through November (Fig. 2A, green triangles). Restricting analysis of the adjusted PhotoAcc model to the lower estuary stations reduced the degree of over prediction from January through June, but prediction remained out of phase with observations (Fig. 2B, green triangles).

**Interannual variability**

The basic balanced growth model with temperature sensitivity in chl:C overestimated annual mean $P_{\text{max}}^a$ in all years except 1996 (Fig. 2C, red circles). Removal of temperature sensitivity in chl:C reduced the degree of over prediction and resulted in unbiased overall means with respect to measurements (p = 0.30; Fig. 2C, blue triangles). Restriction of the analysis to lower estuary stations slightly lowered the calculated annual means but without introducing significant bias (Fig. 2C, green triangles). There was
Annual means predicted by the basic PhotoAcc model (Fig. 2D, red circles) were higher than measured values in all but 2 years, and years were significantly higher overall (p < 0.001). The adjusted PhotoAcc calculations were closer to observed annual means but mostly higher, though not significantly so (p > 0.1; Fig. 2D, blue triangles). Restricting analysis of the adjusted PhotoAcc model to lower estuary stations brought the level of the predictions closer still to observations (Fig. 2D, green triangles). No version of the PhotoAcc model had a significant slope when treating year as a continuous variable in the GLM analysis (Table 1).

Spatial variability

Both physiologically based models over predicted the degree of variability attributable to location as a result of the gradient in depth and light attenuation coefficient (Fig. 2E,F). Adjustment of the balanced-growth model by removal of the temperature dependence of chl:C reduced the overall overestimation by the basic balanced growth model (Fig. 2E), but systematically underestimated \( P_{\text{max}}^B \) down estuary of km 2.0 and over-estimated at upper stations. With PhotoAcc, the switch from bottom-light to water column-averaged light resulted in a similar systematic deviation as with the balanced growth model (Fig. 2F). In both cases, it is evident from the measurements that longitudinal mixing prevents adaptation of \( P_{\text{max}}^B \) to the local optical depth. The appropriate scale is achieved in the model calculations for the station at 2.0 km.

Neither physiologically based model, even as adjusted and selected for lower estuary stations, produced a good fit with individual measurements (Fig. 4). The adjusted balanced growth model predicted the overall range and mean of measurements (Fig. 4A), but the coefficient of determination was low (\( R^2 = 0.031 \)). The average of the predictions by the adjusted PhotoAcc model matched that of the
measurements (Fig. 4B), but PhotoAcc failed to predict the overall range of measurements and the coefficient of determination was likewise low ($R^2 < 0.001$).

**Statistical models**

**Environmental correlates**

Temperature and IC were the strongest environmental correlates of $P_{\text{max}}^B$, although there was much scatter in both relationships (Fig. 5A,B). An exponential relationship provided an approximate upper bound to the temperature response of $P_{\text{max}}^B$ (Fig. 5A). The stepwise regression of square root-transformed $P_{\text{max}}^B$ against appropriately transformed environmental correlates revealed 5 significant predictors (Table 2), with an overall coefficient of determination of 0.45 (Table 2, Fig. 6A). The same variables were statistically significant ($p < 10^{-4}$) predictors without transformation, but the statistical fit with the transformed variables was superior to the fit with untransformed variables ($R^2 = 0.37$) for reasons given previously (Harding et al. 2002). Temperature and IC explained 40% of the variability, with the remaining 3 factors, ln(chl a), ln($K_d$), and PC5, accounting for another 5%. Selecting the data for September eliminated $T$ as a factor due to the limited range observed in a single month, and resulted in substitution of PC4 species component for PC5 (Table 2). The regression on September data explained 54% of the variance...
overall (Fig. 6B), with IC alone accounting for 27%, and the other 4 variables accounting for more of the remaining variance than in the complete data set. The overall range of values observed in the month of September ranged from the 5th to >99th percentile of all observed values (cf. Fig. 6A,B).

Seasonal variability

The GLM analysis of the stepwise regression model revealed the same relative ranking of the temporal and spatial components as the observations, i.e. seasonal (MS = 671) was the greatest, followed by interannual (MS = 57) and spatial (MS = 6). The regression model with T as the only predictor captured much of the seasonal pattern, except that the prediction peaked between July and August, earlier than the measured maximum (Fig. 7A, crosses). Inclusion of IC moved the modeled maximum to September (Fig. 7A, open circles). Inclusion of the remaining significant predictors made only fine adjustments to the predictions using only T and IC, mostly in the first 2 mo of the year (Fig. 7A, triangles).

Interannual variability

The stepwise regression model with T as the only predictor captured very little of the variability in interannual means, varying only from 2.69 to 2.99 mg C mg⁻¹ chl a h⁻¹ compared with an observed range from 2.5 to 5.8 mg C mg⁻¹ chl a h⁻¹ (Fig. 7B). Treating year as a continuous variable with T as the only predictor yielded a significantly positive slope (Table 1), contrary to measurements. With the exception of 1996, inclusion of IC improved prediction of annual means, with predictions of annual means ranging from 2.08 to 3.56 mg C mg⁻¹ chl a h⁻¹. Including IC in the regression resulted in a negative slope of $P_B^{max}$ against year when treating year as a continuous variable in the GLM (Table 1). Inclusion of all significant predictors further improved predictions of annual means, but no combination of variables predicted the anomalously high values of 1996 (Fig. 7B). Treating year as a continuous variable in the GLM with all significant predictors resulted in a negative slope of $P_B^{max}$ against year when treating year as a continuous variable in the GLM (Table 1). Inclusion of all significant predictors further improved predictions of annual means, but no combination of variables predicted the anomalously high values of 1996 (Fig. 7B). Treating year as a continuous variable in the GLM with all significant predictors resulted in a negative slope of $P_B^{max}$ with year, although the magnitude was about 30% lower than the observed slope (Table 1).

$P_B^{max}$ values averaged for the month of September ranged from 2.62 to 7.97 mg C mg⁻¹ chl a h⁻¹. That is, substantial interannual variability remained in measured $P_B^{max}$ after restricting the analysis to eliminate possible bias due to uneven sampling of winter months (Fig. 7C). IC alone accounted for 46% of the interannual variance in $P_B^{max}$ averaged for September, while inclusion of all significant predictors improved the overall range of predicted September means (2.59 to 7.82 mg C mg⁻¹ chl a h⁻¹) and increased the explained interannual variance to 63% (Fig. 7C).
slope of $P_B^{\text{max}}$ on year, with year treated as a continuous variable in the GLM and data selected for September, was significantly negative with a magnitude about 20% greater than the observed slope (Table 1).

**Spatial variability**

As indicated above, the spatial means of observed $P_B^{\text{max}}$ varied only from 2.7 to 3.3 mg C mg$^{-1}$ chl a h$^{-1}$ (Fig. 1C), and the spatial pattern of that variability was not captured by any combination of tested predictors in the statistical models (not shown).

**Temporal stability of parameters**

The coefficient multiplying ln($T$) in the statistical model on transformed data varied by more than a factor of 6 when the regression was run on individual years (Table 2, Fig. 8A, filled squares). Analyzed by adding successive years to the analysis, the coefficient first came within 10% of its final value after including the 7th year of measurements, and remained within 5% of its final value after the 13th year (Fig. 8A, line). Performing the regressions on data grouped in sequential 3 and 5 yr clusters reduced the range of calculated coefficients, with estimates ranging from 12 to 38% of the final estimate for 3 yr clusters, and 9 to 15% for 5 yr clusters (Fig. 8A).

A similar degree of variability as with the coefficient for ln($T$) was observed in the coefficient multiplying IC when running the regression on individual years (Fig. 8B). The coefficient was within 10% of its final value after 7 yr, and remained within 5% of its final value from 10 yr onwards (Fig. 8B). Estimates obtained from 3 and 5 yr clusters of the data ranged from 1 to 50% and from 1 to 25% of the final value, respectively. Coefficients of determination of the regressions based on individual years ranged from 0.15 to 0.78, with 12 of the 20 years exceeding the cumulative value (Fig. 8C).

**DISCUSSION**

**Physiological models**

A reliable physiologically based model of P-E parameters is desirable for driving ecosystem models, especially in the context of climate change,
wherein the goal of the analysis is to predict the response to altered future conditions from a mechanistic understanding of the dependencies. The 2 physiological models tested here captured the overall average of measured $P_{B_{\text{max}}}$ of the system, but did not successfully predict individual observations (Fig. 4). Nevertheless, insight into factors controlling $P_{B_{\text{max}}}$ may be gained by examining modes of failure and causes of model deficiencies.

PhotoAcc had some computational characteristics that are not appropriate to this system. For example, the minimum $P_{B_{\text{max}}}$ obtainable with PhotoAcc (nutrient-limited formulation) is 1.19 mg C mg$^{-1}$ chl a h$^{-1}$, while many observations were lower than that (Figs. 1A & 4B). Also, the nutrient-limited version has a maximum $P_{B_{\text{max}}}$ of 11.1 mg C mg$^{-1}$ chl a h$^{-1}$, so that some use of the nutrient saturated formulation is needed to capture the whole range of observed values. In some systems, the rate of supply of limiting nutrients may contribute to the prediction of $P_{B_{\text{max}}}$, such as in a stratified ocean in which the distance to the nutrcline is an index of the rate of nitrogen supply (Bouman et al. 2005). Considering that phytoplankton growth depends on internal nutrient stores, and that in a shallow estuary such as the Rhode River episodic nutrient inputs may come from runoff, the atmosphere, or benthic release, the prospect of anticipating transitions from nutrient-limited to nutrient-saturated states in such a complex system is weak.

It is not surprising that the balanced growth approach would not predict individual observations. There is considerable scatter in the allometric relationships used to calculate growth rates from phytoplankton counts (Tang 1995) as well as in the prediction of chl:C (Cloern et al. 1995). Furthermore, in situ growth in highly dynamic systems may frequently be unbalanced (Cullen 1990). Additional uncertainties are associated with phytoplankton counts, assignment of geometric shapes, and carbon conversions (Strathmann 1967, Hillebrand et al. 1999). In spite of these difficulties, the balanced growth approach cap-
tured the overall mean and range of observations (Fig. 4A), and the seasonal pattern for the first half of the year (Fig. 2A).

The tendency for both physiologically based models to over emphasize spatial effects (Fig. 2E,F) demonstrates that longitudinal mixing in the Rhode River is too rapid and distances too short for the phytoplankton to become acclimated to the optical depths at the sampling sites, especially in the upper estuary. Predictions matched the spatial means at 2.0 km (Fig. 2E,F), which has a depth of 3 m and average optical depth ($K_{d,H}$) of 4.1 (dimensionless). Jordan et al. (1991a) estimated that the exchange coefficient between the lower and upper Rhode River was 0.4 d$^{-1}$, suggesting that the time constant for acclimation (Lewis et al. 1984) would be less than this for horizontal mixing to dominate over acclimation.

Failures of the physiologically based models also give some insight into the role of temperature in governing $P_B^{\text{max}}$ in the Rhode River. PhotoAcc ignores temperature effects above 5°C and attributes all acclimation to light and nutrients (Behrenfeld et al. 1994), having an approximate upper bound described by an exponential relationship, and much scatter below the curve, especially at higher temperatures (Fig. 5A). Temperature accounted for very little of the interannual variability in $P_B^{\text{max}}$ (Fig. 7B), and in fact, the trend in the statistical model with $T$ as the only predictor was in the opposite direction of measurements (Table 1). Temperature measured on sampling cruises on the Rhode River has increased at a rate of 0.036°C yr$^{-1}$ (Gallegos et al. 2010), but other factors appear to dominate the effect on $P_B^{\text{max}}$.

Inclusion of IC in the regression model captured the timing of the seasonal maximum in $P_B^{\text{max}}$ (Fig. 7A), much of the interannual variability (Fig. 7B,C), and the direction of the long-term trend (Table 1). There is precedence for the finding that IC was a significant predictor of $P_B^{\text{max}}$ in the Rhode River. Loftus et al. (1979) measured the IC saturation kinetics of natural populations from the Rhode River on 6 occasions and found that the half-saturation constant, $K_a$, averaged 0.55 (range 0.29 to 0.77) mM C (average 6.65 and range 3.48 to 9.24 mg C l$^{-1}$). They found that addition of IC as bicarbonate to incubation bottles stimulated $^{14}$C uptake by up to 2.5-fold (Loftus et al. 1979). For IC concentrations ranging from 1.4 to 26 mg C l$^{-1}$ in the measurements reported here, the factor expressing the limitation of photosynthesis by IC, IC/($K_a$+IC), would have a typical value of 0.68 (dimensionless) and could be as low as 0.13.

Limitation by IC may partially account for values of $P_B^{\text{max}}$ lower than observed at comparable temperatures in some other coastal systems with stronger marine connections than the Rhode River (e.g. Harrison & Platt 1980). In the Rhode River, there was a positive, albeit weak ($R^2 = 0.28$), dependence of IC on salinity, but salinity was not retained in the stepwise regression analysis as an environmental predictor of $P_B^{\text{max}}$. Similarly, there was a weak ($R^2 = 0.18$) negative correlation between annual mean IC and annual mean freshwater flow by the Susquehanna River, the principal freshwater source to upper Chesapeake Bay (Malone et al. 1988, Harding 1994). In a river-dominated estuary there is potential for flow-related variability in IC, apart from atmospheric trends, that would not be expected in a more coastal dominated system.

One advantage of a long record of $P_B^{\text{max}}$ measurements is that it spans periods of suspected changes in climate regimes (Peterson & Schwing 2003), of which marine plankton are sometimes very sensitive indicators (Hays et al. 2005). Climate may also directly affect the environmental correlates of $P_B^{\text{max}}$ identified here, especially those dependent on flow. Previous research in Chesapeake Bay, however, has indicated that synoptic climatology is a more sensitive indicator of regional climate effects than large-scale ocean-atmospheric indices such as the North Atlantic

Environmental covariates

The relationship of $P_B^{\text{max}}$ with temperature in the Rhode River was similar to observations in other estuaries (Pennock & Sharp 1986, Lohrenz et al. 1994), having an approximate upper bound described by an exponential relationship, and much scatter below the curve, especially at higher temperatures. One advantage of a long record of $P_B^{\text{max}}$ measurements is that it spans periods of suspected changes in climate regimes (Peterson & Schwing 2003), of which marine plankton are sometimes very sensitive indicators (Hays et al. 2005). Climate may also directly affect the environmental correlates of $P_B^{\text{max}}$ identified here, especially those dependent on flow. Previous research in Chesapeake Bay, however, has indicated that synoptic climatology is a more sensitive indicator of regional climate effects than large-scale ocean-atmospheric indices such as the North Atlantic.
Oscillation, Pacific Decadal Oscillation, or El Niño-Southern Oscillation (Miller et al. 2006, Miller & Harding 2007), and that patterns in synoptic climatology have been less clear than the large-scale indices. Out of 20 weather patterns shown to predict 54% of the variability in spring flow of the Susquehanna River, only 1 displayed a long-term trend over the period from 1950 to 2002 (Kimmel et al. 2009). Given the magnitude of correlations between flow and IC indicated above and the strength of association with $P_B^{\text{max}}$ considerable time would be required for anticipated effects of increased concentrations of IC through changes in flow to become evident in measurements of $P_B^{\text{max}}$.

An indicator of species composition was retained in the stepwise regression analysis in this study, although the predictive power was low (Table 2). Different species PC scores were retained depending on whether the data were analyzed for the entire year (PC5) or for the month of September (PC4). The eigenvectors for the 2 components share some features in common (Table 3), being negatively weighted predominately by diatoms, and positively weighted by a large summer-dominant dinoflagellate. In this analysis, the negative regression coefficients (Table 2) imply that negative PC scores contribute to higher values of $P_B^{\text{max}}$. Negative PC scores are generated by negative deviations from the mean of large dinoflagellates and positive deviations of the diatoms listed in Table 3. The direction of the effect in each case is therefore consistent with overall size- and taxonomic dependencies observed for phytoplankton growth rates (Banse 1982, Tang 1995). It is possible that a more integrative index based on diagnostic photopigments would be a more robust predictor than these PC scores based on species counts (Bouman et al. 2005). In shorter-term studies, the effect of species composition on $P_B^{\text{max}}$ is sometimes much stronger than observed here (e.g. Côté & Platt 1983, Gallegos 1992). Stronger relationships can be expected when there are clear demarcations between a few fast- versus slow-growing species, whether observed based on spatial distributions (Gallegos 1992) or on the time scale of a single bloom (Côté & Platt 1983). In a longer-term study such as this, the relationship is degraded both by the limited variance in the species composition described by the PC scores (Gallegos et al. 2010), and by noise in the underlying allometric relationships between growth rate and cell size and taxonomic composition (Banse 1982, Tang 1995) noted above for the balanced growth physiological approach. Our expectations for the explanatory value of species composition data for predicting $P_B^{\text{max}}$ values should therefore be tempered by an understanding of the complexity of the species dynamics in the region of interest.

Too much importance should not be ascribed to the observation of a downward trend in $P_B^{\text{max}}$ (Table 1). Note that an increasing trend in chl a was observed over the 20 yr reported here (Table 1), while no such trend was observed in an analysis of a longer time series of chl a in the Rhode River dating back to 1970 (Gallegos et al. 2010). Decadal scale oscillations were apparent in chl a (Gallegos et al. 2010), and it is possible that longer-term observations of $P_B^{\text{max}}$ and IC would reveal similar changes that would eliminate the appearance of a trend.

### Temporal stability of parameter estimates

Most attempts to derive relationships between $P_B^{\text{max}}$ and environmental parameters are based on studies of considerably shorter duration than this one (Pennock & Sharp 1986, Lohrenz et al. 1994, Harding et al. 2002). It is legitimate to ask what was learned from 20 yr of measurements that was not apparent in the first 1 to 3 yr. When regressions were performed on data from individual years, the estimate of the coefficient multiplying ln(T) varied by more than a factor of 6 (Fig. 8A). For the data transformations used, a coefficient value of 0.614 translates to a $Q_{10}$ of 2, the commonly assumed value for enzymatic processes. The coefficient estimates based on analysis of individual years imply $Q_{10}$ factors ranging from 0.36 to 4.5, while the coefficient based on all years, 0.47, implies a $Q_{10}$ of

<table>
<thead>
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<th>PC 5 taxa</th>
<th>Weighting</th>
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<tbody>
<tr>
<td>Thalassiosira sp.</td>
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</tr>
<tr>
<td>Leptocylindrus minimum</td>
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<tr>
<td>Nitschia longissima</td>
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<td>Heterocapsa rotundata</td>
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<td>Pyramimonas sp.</td>
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<tr>
<td>Chlamydomonas sp.</td>
<td>0.274</td>
</tr>
<tr>
<td>Chroomonas sp.</td>
<td>0.247</td>
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</tbody>
</table>

<table>
<thead>
<tr>
<th>PC 4 taxa</th>
<th>Weighting</th>
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</thead>
<tbody>
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<td>Cyclotella glomerata</td>
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<tr>
<td>T. pseudonana</td>
<td>-0.251</td>
</tr>
<tr>
<td>Gyrodinium uncatenum</td>
<td>0.230</td>
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1.2. A $Q_{10}$ smaller than 2 is expected for this system because a curve for $Q_{10} = 2$ provides an approximate upper bound to the data, and the overall response to temperature by the bulk of the data is considerably weaker than the upper bound (Fig. 5A). Statistical models estimated on a single year of data therefore have a high chance of not generally characterizing the response of the system in a multiple-year study, even in cases in which the coefficient of determination indicates a statistically reliable regression (cf. Fig. 8A, C, for 1991). Three and 5 yr groupings of the data reduced the variability in estimated coefficients to within 40 and 15%, respectively, of the final estimates (Fig. 8A). Nevertheless, the time required for parameters in the statistical models to achieve 10% (7 yr) or 5% (13 yr) of their final values is considerably longer than the typical study.

The length of the record reported here and the eventual stability of statistical parameter estimates suggests that unbiased, if not especially precise, estimates of $P_{\text{max}}^B$ may be made in the future from measurements of environmental correlates alone. While an empirical statistical approach lacks the mechanistic foundation of a physiological approach, the fit was better, as was the prediction of seasonal and interannual variations. The 2 predictors accounting for most of the variance are important components of climate change. Additionally, the first 4 predictors, i.e. $T$, $IC$ (Wang et al. 2007), $chl \ a$, and $K_d$ (Moore et al. 1997, 2012), are amenable to long-term in situ monitoring, suggesting that high density and semi-automated estimates of $P_{\text{max}}^B$ may be an eventual possibility.

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